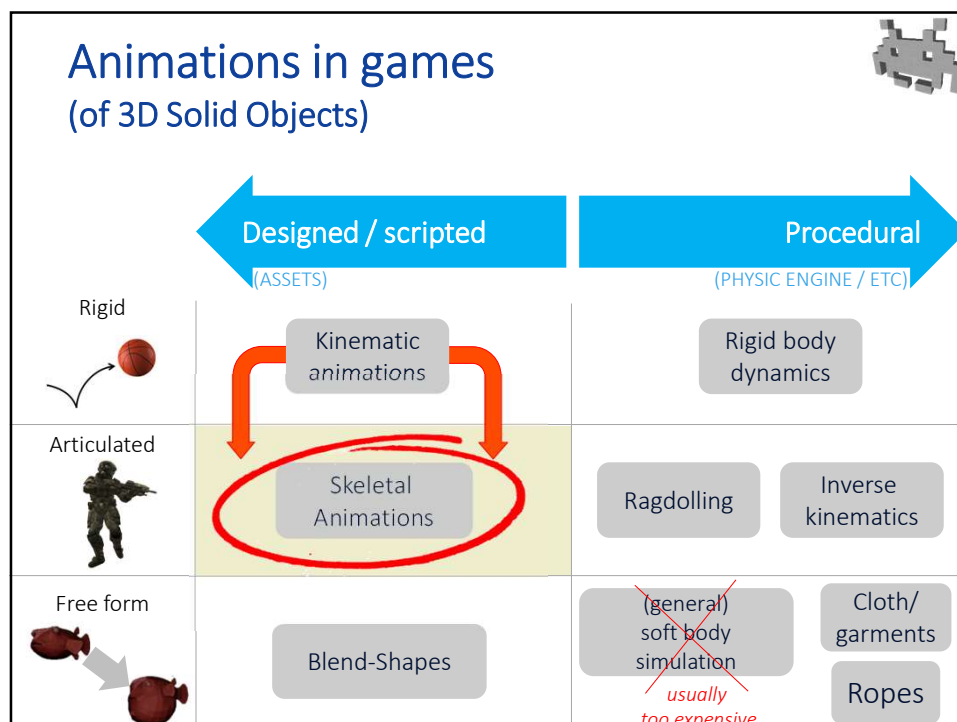
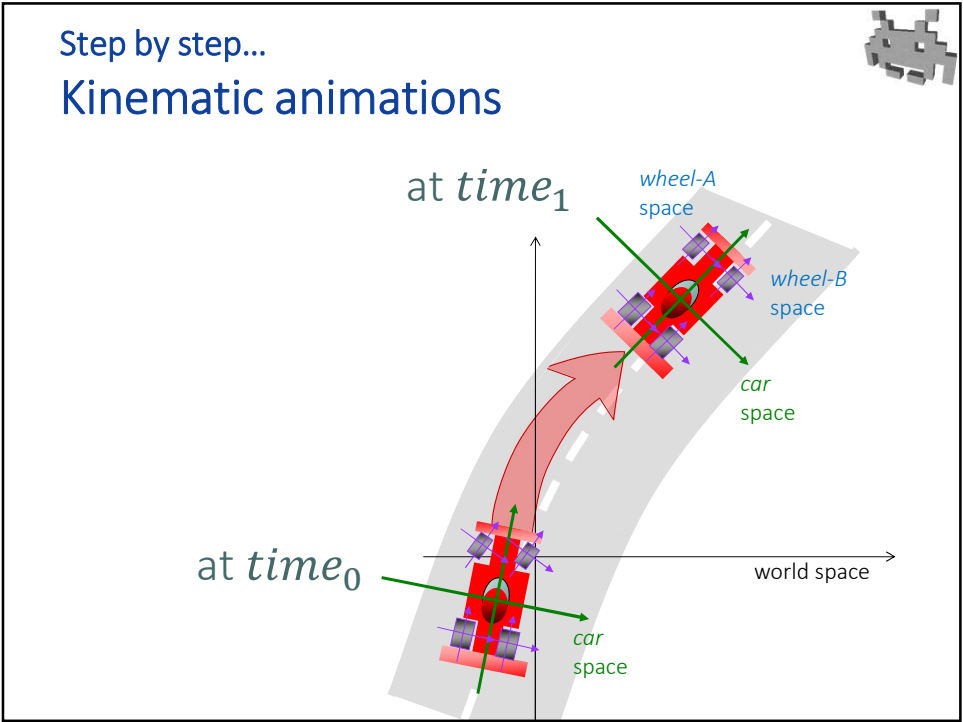


| Course Plan                                   |           |
|---|-----------|
| lec. 1: Introduction                          | ●         |
| lec. 2: Mathematics for 3D Games              | ●●●●●     |
| lec. 3: Scene Graph                           | ●         |
| lec. 4: Game 3D Physics                       | ●●● + ●●● |
| lec. 5: Game Particle Systems                 | ▶         |
| lec. 6: Game 3D Models                        | ●●        |
| lec. 7: Game Textures                         | ▶●        |
| lec. 8: Game 3D Animations                    | ●●●       |
| lec. 9: Game 3D Audio                         | ●         |
| lec. 10: Networking for 3D Games              | ●         |
| lec. 11: Artificial Intelligence for 3D Games | ●         |
| lec. 12: Game 3D Rendering Techniques         | ●●        |

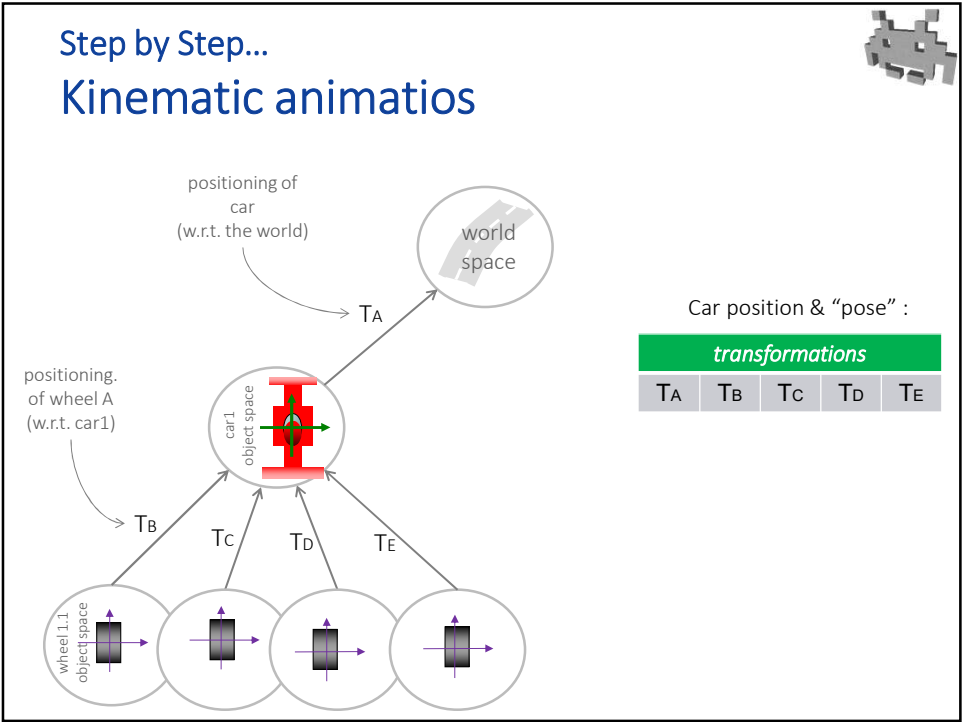
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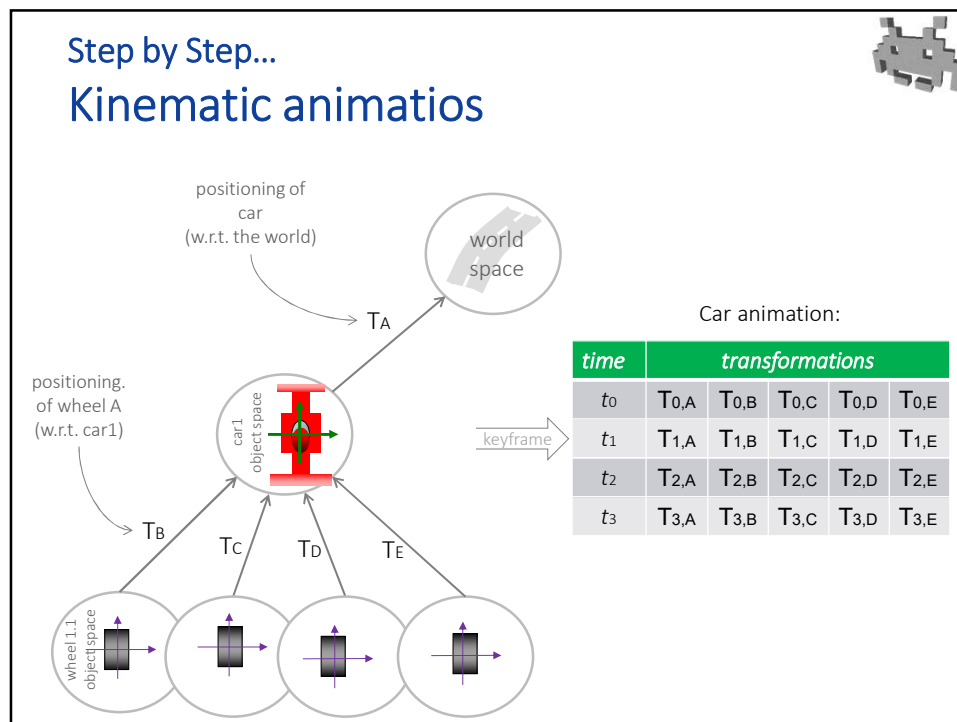
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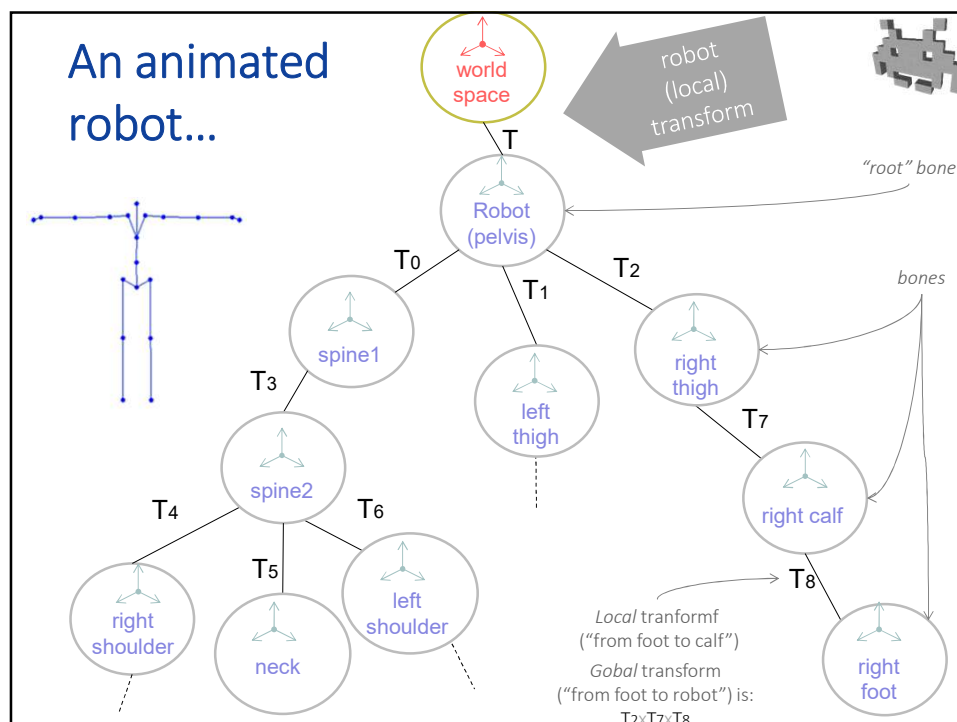
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### Step by step...

## From a bunch of pieces...



- So far: one mesh in each “bone”
  - (e.g., car-cockpit, car-wheel)
- Ok, for simple structure
  - (like a car, a windmill...)
- What about a humanoid “robot” with 25-60 “bones”?
  - Individual meshes for arms, forearms, legs...  
three meshes for each finger?
  - Possible, but...
    - inefficient to render (lots of “draw calls”)
    - uneasy to manage (lots of files?)
    - a nightmare to design / author  
 (“sculpt me a nice looking calf”)
    - and... looks right only for robots (each object rigid!)

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## ... to articulated models...

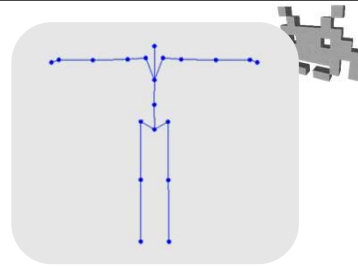


- Idea: one **mesh**, but **skinned**
  - 1 mesh per the entire character
  - a new attribute per vertex: *index of bone*
  - the 3D model can now be animated!
- Orthogonality models / animations!
  - that is:
    - one skinned mesh: runs with any animations
    - one skeletal animation: can be applicable to any model
  - (as long as they use the same RIG – set of bones)
  - → 500 models + 500 animations = 1000 things in GPU RAM
    - not: 500x500 combinations
- The tasks required from digital artists:
  - “**rigging**”: define the **skeleton** inside the mesh (riggers)
  - “**skinning**”: define vertex-to-bone links, i.e. the skinning (skinners)
  - “**animation**”: define the actual animations (animators)

“**Skinning**”  
of the mesh  
(1<sup>st</sup> version).

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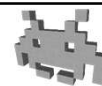
## Rig (or skeleton): data structure 1/2



- A tree of **bones**
- **bone**:
  - **Vectorial frame (space)** used to express pieces of the animated model
  - eg, for a humanoid: *forearm, calf, pelvis, ...*
  - (rigging bone != biological bones)
- Space of the **root bone** =(def)= **object space** (of the entire character)
- How many bones in a skeleton of a humanoid:  
at least: 22-24 (typically)  
reasonable: ~40 bones.  
very high: few 100s

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## Pose: data structure



One **transformation**  
for each **bone  $i$**

- **Local transform**: (of bone  $i$ )
  - **from**: space of one  $i$
  - **to**: space of bone father of  $i$

often, only the  
rotation  
component

("fixed length bones":  
translations defined  
once and for all  
by the skeleton)

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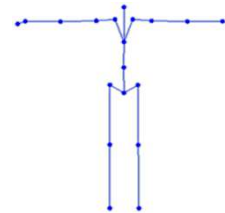
## Rig (or skeleton): data structure 2/2

### 1. Hierarchy (tree) of bones

- a **root bone** on top

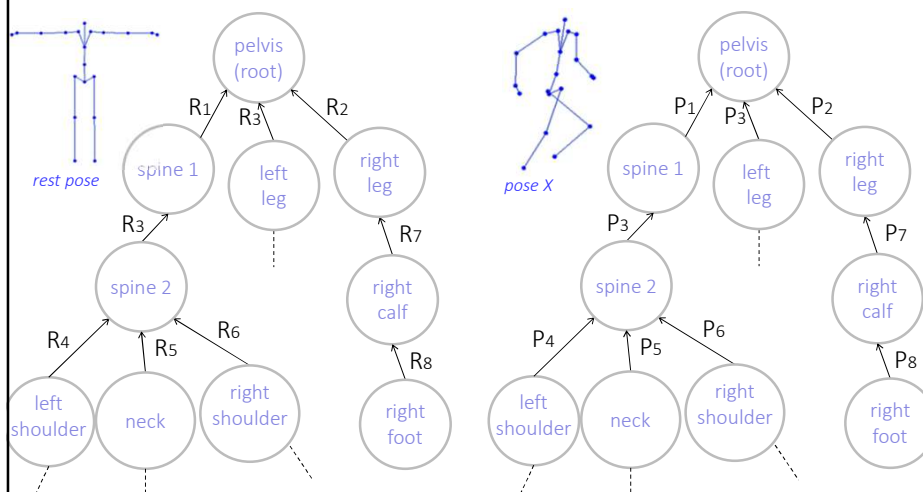
### 2. A special **pose** «rest pose»

- 3D models are to be modelled in this pose
- also: «T-pose», «T-stance»,
  - same reason why T-shirts are called T-shirts ;)
- also: «A-pose», when arms are bent down

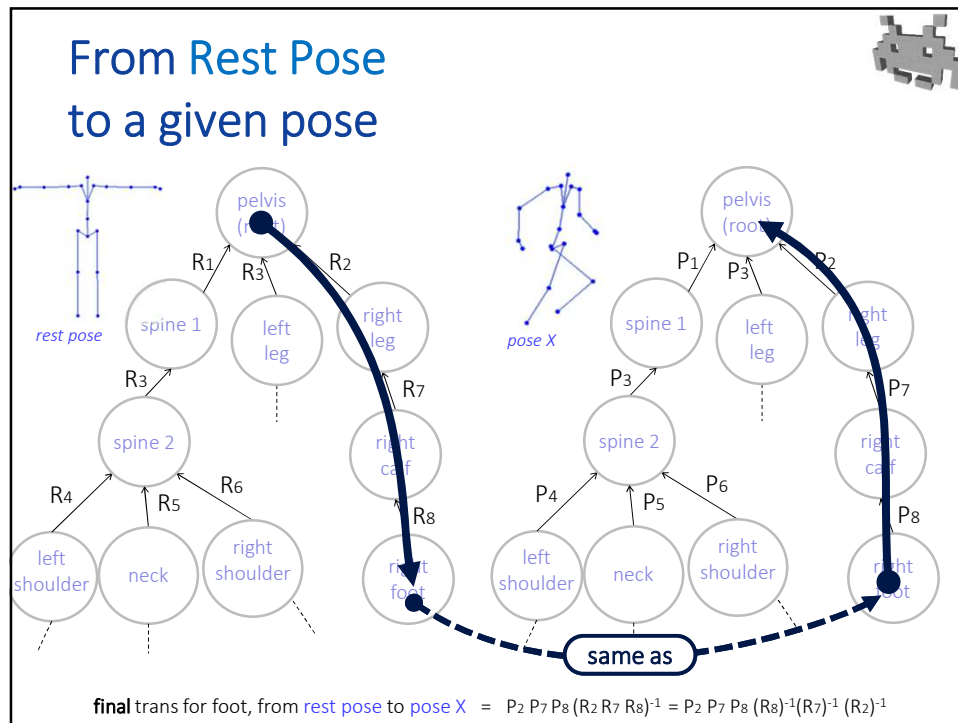


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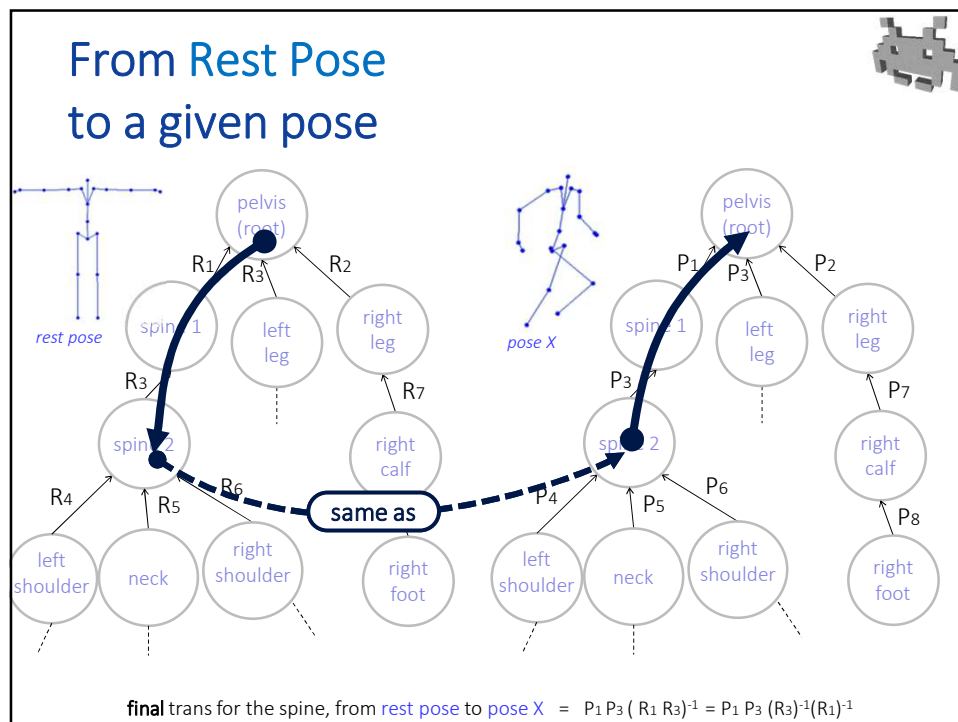
## From Rest Pose to a given pose



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## Bone transforms in a pose.

E.g. for «right foot» bone:

- **Local Transform:**  $P_8$ 
  - from «right foot» to «right lower leg»
- **Global Transform:**  $P_2 P_7 P_8$ 
  - from «right foot» space to «character» space
  - uses the **Hierarchy** of the **Skeleton**
    - once computed, skeleton **hierarchy** no longer needed
- **Final Transform:**  $P_2 P_7 P_8 R_8^{-1} R_7^{-1} R_2^{-1}$ 
  - from «character» space in rest pose to «character» space in dest. pose
  - uses the **Rest Pose** of the **Skeleton** ( $R_1 \dots R_N$ )
    - once this is computed, **Rest Pose** is no longer needed


the local frame of the character, which is the frame of the **root bone**

mesh (vertices normals...) is defined in this space!

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## Pose (for a given rig) : data structure

- **pose** = array of (local) transforms
  - it's defined for one given rig
  - RAM cost:  $n\_bones \times bytes\_for\_a\_transform$



| Bone $i$           | Trasform[ $i$ ] |
|--------------------|-----------------|
| #0 (pelvis) [root] | L[0]            |
| #1 (spine)         | L[1]            |
| #2 (chest)         | L[2]            |
| #3 (shoulder sx)   | L[3]            |
| ...                | ...             |
| #10 (calf)         | L[10]           |
| ...                | ...             |

### Local Transform

It includes:


- a **Rotation**: always!
- a **Translation**: maybe  
If not, use the one defined in the **rest pose** of the rig.  
==> a pose cannot redefine bone *lengths*.
- a **Scaling**: usually not  
A joint cannot enlarge a part of the character

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## Pose (for a given rig) : data structure in GPU

- **pose** = array of **final** transforms
  - it's defined for one given rig
  - RAM cost:  $n\_bones \times bytes\_for\_a\_transform$



| Bone $i$           | Transform[ $i$ ] |
|--------------------|------------------|
| #0 (pelvis) [root] | F[0]             |
| #1 (spine)         | F[1]             |
| #2 (chest)         | F[2]             |
| #3 (shoulder sx)   | F[3]             |
| ...                | ...              |
| #10 (calf)         | F[10]            |
| ...                | ...              |

computed in preprocessing e.g. as:

$$L[2] \ L[7] \ (R[7])^{-1} \ (R[2])^{-1}$$

local transforms  
of *this* pose

local transforms  
of *rest* pose

final transforms

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## Skeletal Animation : data structure (CPU or GPU)

- 1D Array of **poses** (1 pose = 1 keyframe)
  - RAM cost:  
 $(num\ keyframes) \times (num\ bones) \times (transform\ size)$
  - Each pose assigned to time  $dt$ 
    - delta from start of animation  $t_0$
  - Sometime, looped
    - interpolation 1st keyframe with last

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### Step by step...



### From a bunch of pieces...

- one separate mesh in each “bone”
  - “calf” mesh, “head” mesh, “right-forearm” mesh...



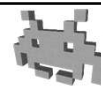
### ... to *a* single articulated model...

- 1 “skinned” mesh for the entire character
- in each vertex, an index of a bone
  - a vertex-bone link

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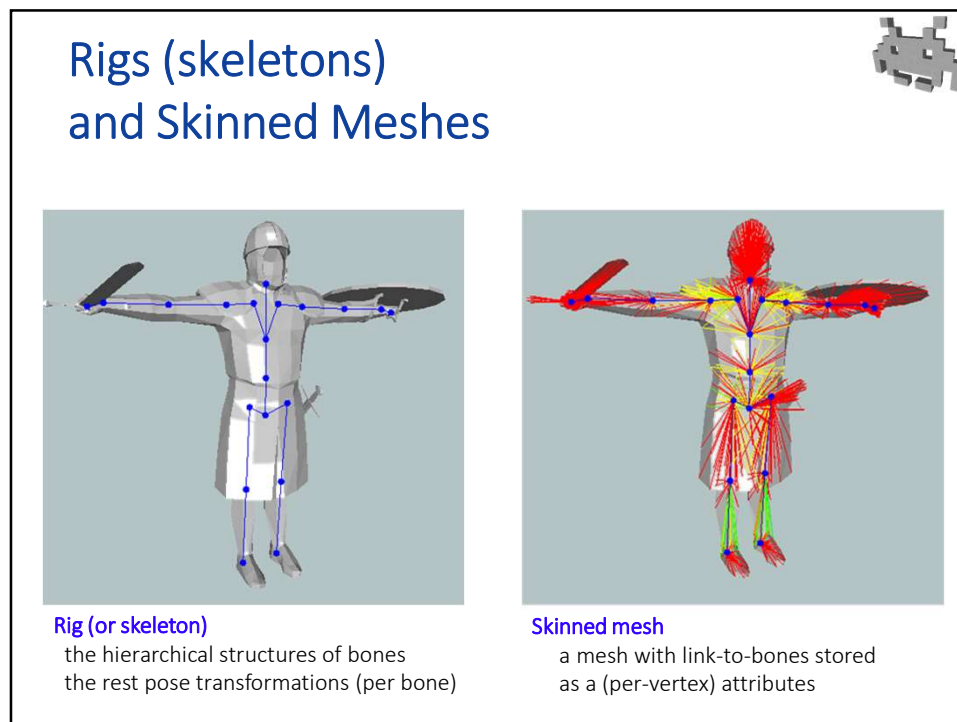
### ... to articulated *deformable* models.



- Idea: link each vertex to multiple bones
  - «blended» skinning
  - each linked bone with a strength (a weight)
- Transform of the vertex:
  - **interpolation** of the final **transformations** associated to the linked bones
  - **weights** of the interpolation: defined per-vertex
- Data structures: per-vertex attributes
  - store:
    - [ bone index , weight ]  $\times N_{\max}$
    - (typically,  $N_{\max} = 4$  or  $2$ , see later)

*the “Skinning”  
of the mesh  
blended version  
(the one which is  
actually used in  
games)*

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## Skinned Mesh: data structure

- A Mesh with a **skinning**
  - A **per vertex attribute**
  - Stored per vertex:
    - [ bone index , weight ] x  $N_{max}$
    - example:

bone links

Vertex 134 →

| Bone Index          | Weight |
|---------------------|--------|
| 9 (Spine B)         | 0.4    |
| 13 (Chest)          | 0.1    |
| 15 (Shoulder Right) | 0.4    |
| 16 (Forearm Right)  | 0.1    |

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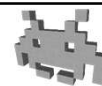
## $N_{\max}$ = How many bone links for each vertex



- It's a call of the Game engine!
- typical used value:
  - 1 (non-blended skinning) (bonus: no need to store weights)
  - 2 (cheap, e.g., for mobile games)
  - 4 (top quality – standard)
  - more: never in games (currently)
- Can one lower  $N_{\max}$  ?
  - yes, in preprocessing
  - e.g., task for a game tool
  - e.g.: Unity does this during skinned mesh import (if asked to)

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## (but why put a hard-wired bound on bone links?)

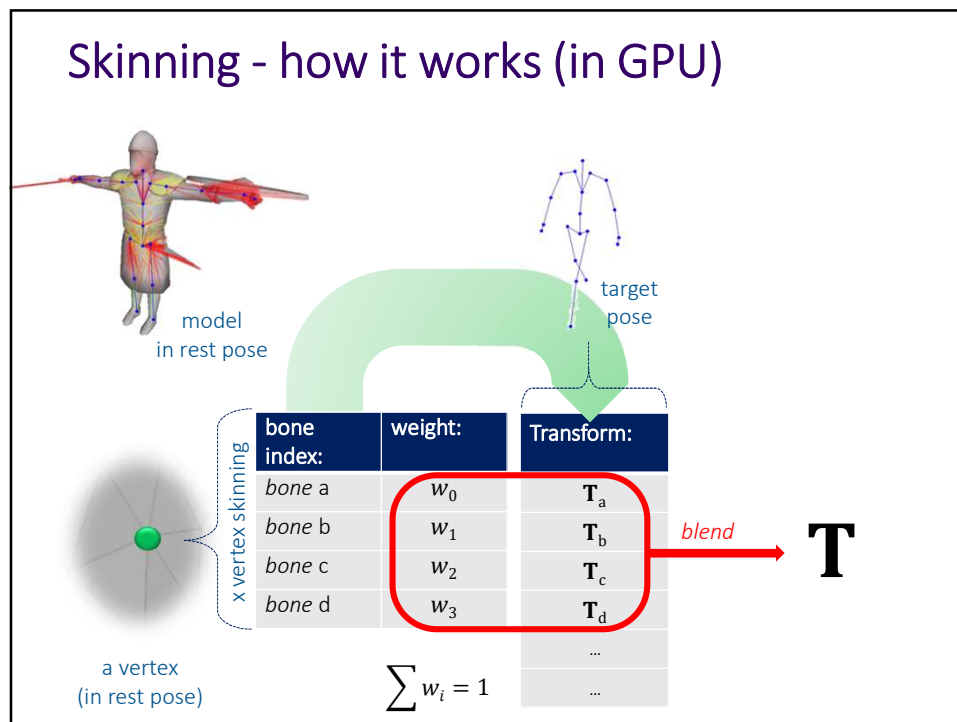


- Reduces performance cost
  - $N_{\max}$  transforms need be interpolated in GPU
    - in vertex shader
  - GPU = no good at control:
    - always uses exactly  $N_{\max}$  trasform
    - unused bones: weight = 0
- Reduces GPU RAM cost
  - reduces storage
  - fixed length arrays: good for GPU
    - $N_{\max}$  (index,weight) pairs
    - even where fewer are locally needed (e.g., if 1 bone, weight is automatically 1)

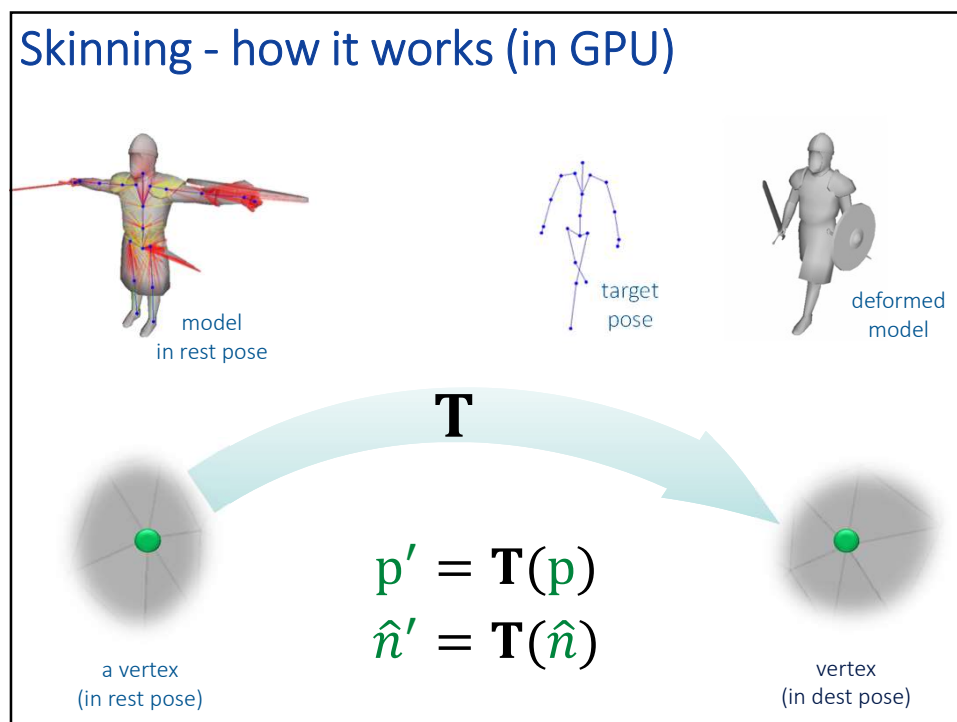
example:

| Bone Index | Weight |
|------------|--------|
| 9 (Head)   | 1.0    |
| --         | 0.0    |
| --         | 0.0    |
| --         | 0.0    |

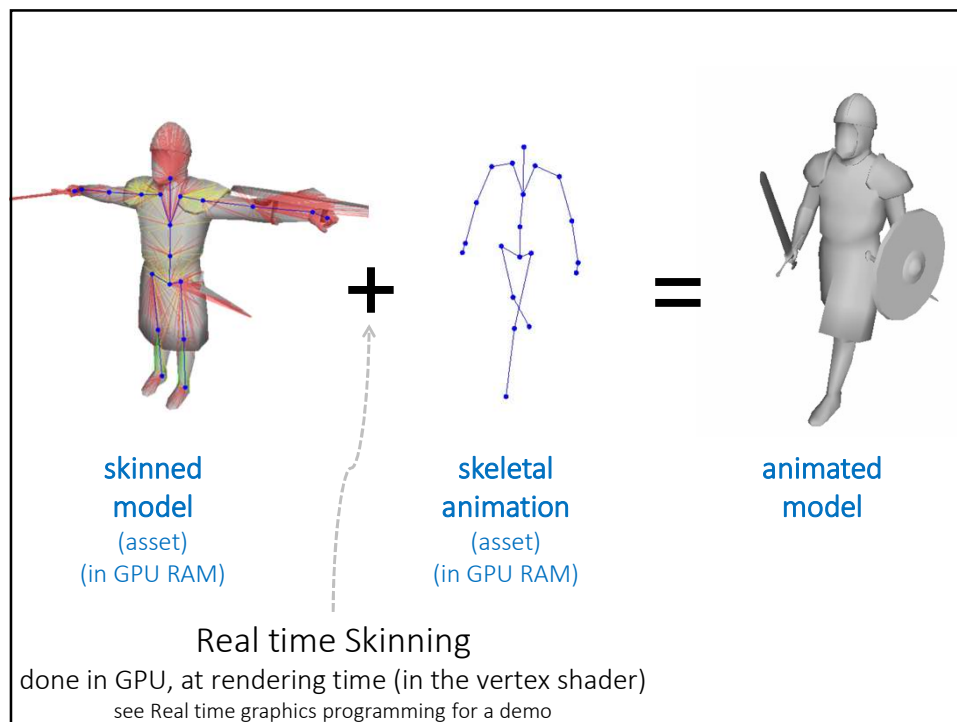
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### GPU real time Skinning – variants

(a choice of the rendering engine)

| Bone:  | Weight: | Transform: |
|--------|---------|------------|
| bone a | w0      | T0         |
| bone b | w1      | T1         |
| bone c | w2      | T2         |
| bone d | w3      | T3         |

blend → **T**

how are they stored?

*Answer 1:*  
«Linear Blend Skinning»

*Answer 2:*  
«Dual Quaternion Skinning»

how is this done?

as a 4x4 matrix transformiton

as a dual quaternion

|                               |                                    |
|-------------------------------|------------------------------------|
| as a 4x4 matrix transformiton | with linear matrix interpolation   |
| as a dual quaternion          | with dual quaternion interpolation |

*nothing else works!*

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### Linear Blend Skinning (LBS)

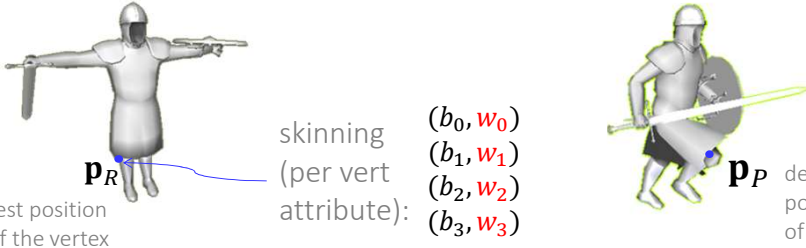
more in general,  $N_{max}-1$

$$\mathbf{p}_P = \left( \sum_{i=0}^3 \mathbf{w}_i \mathbf{T}[b_i] \right) (\mathbf{p}_R)$$

interpolation of the per-bone matrices

$$= \sum_{i=0}^3 \mathbf{w}_i (\mathbf{T}[b_i] (\mathbf{p}_R))$$

interpolation of per-bone transformed points



rest position of the vertex  $\mathbf{p}_R$

skinning (per vert attribute):

- $(b_0, w_0)$
- $(b_1, w_1)$
- $(b_2, w_2)$
- $(b_3, w_3)$

deformed position of the vertex  $\mathbf{p}_P$

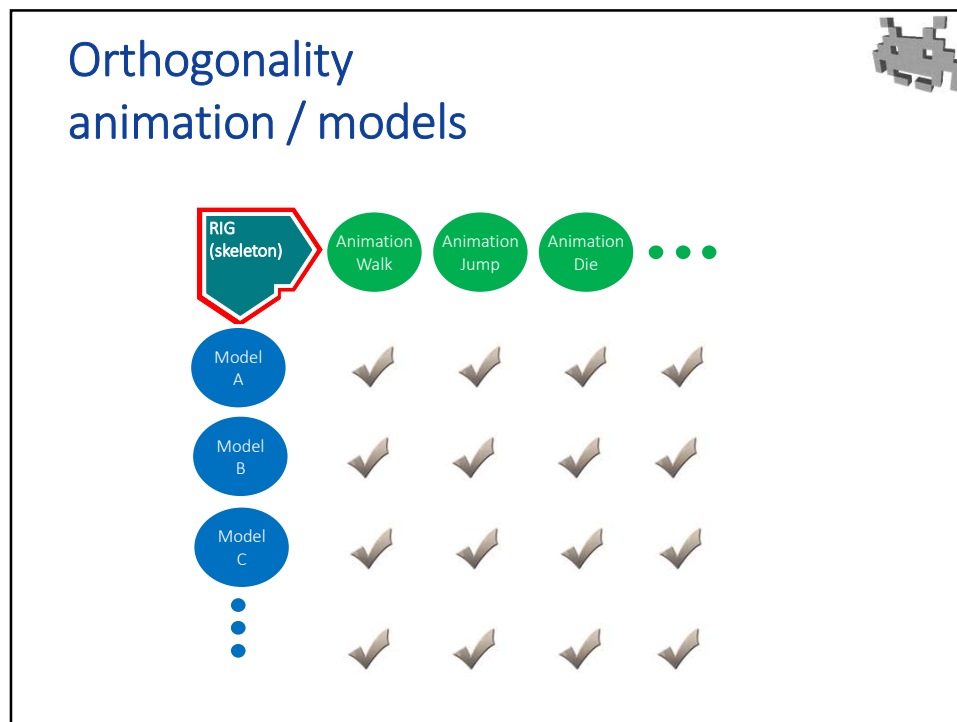
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### Dual Quaternion Skinning (DQS)

- Per-bone final transform stored as a **dual quaternion** See lecture on transform representation
  - better quality
  - better interpolation
  - > GPU cost
    - (necessary ops: around +50%)
- LBS or DQS?
  - a call of the game engine

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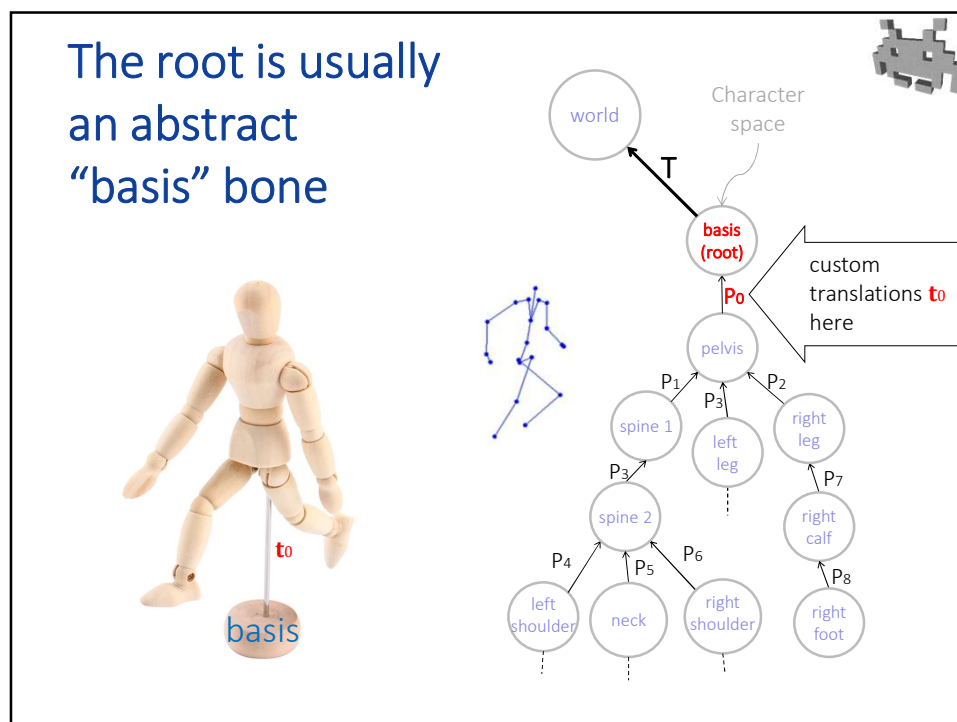
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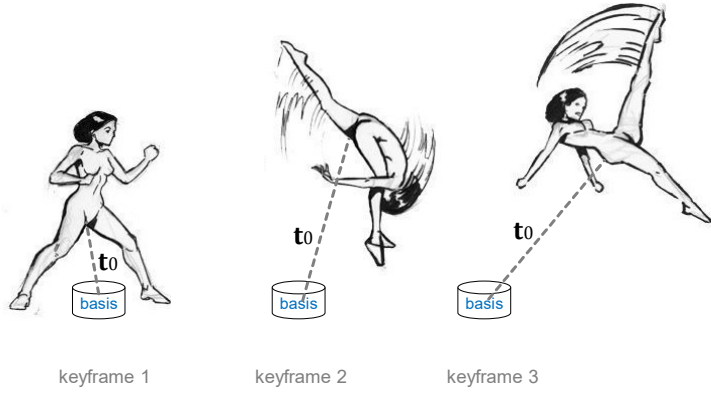


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## Basis bone



keyframe 1      keyframe 2      keyframe 3

so that each animation asset can include  
a global displacement **to** in each keyframe

the basis bone is (normally) the only one redefining the *translation* in the rest pose!

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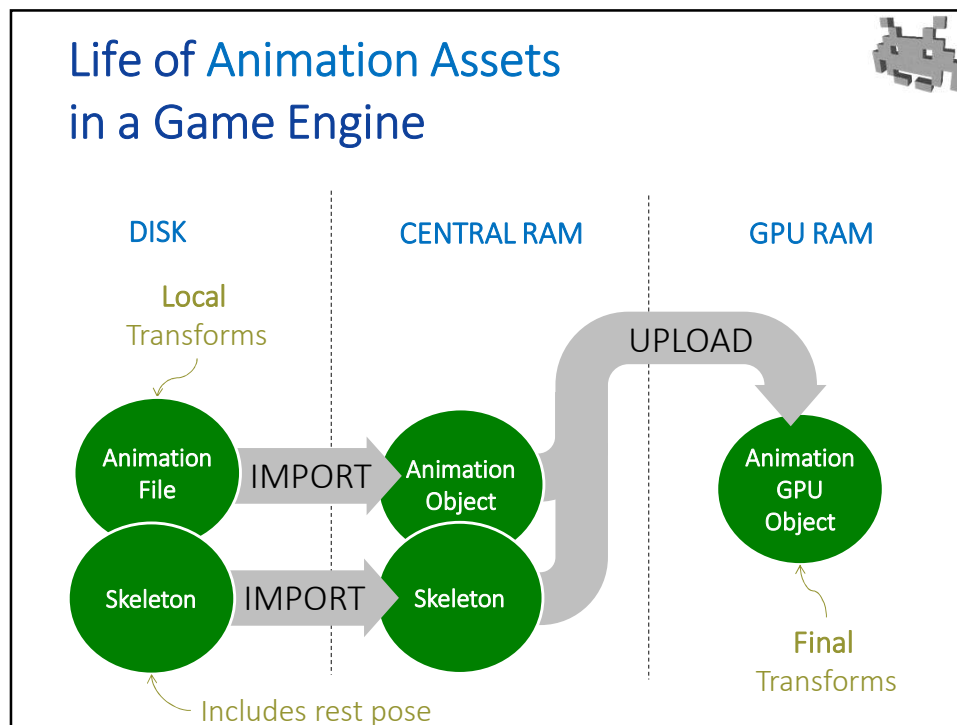
## (recap) Skeletal animations: 3 Assets (data structures)

- **Rig** (or “skeleton”)
  - Tree of **bones**
  - $\forall$  **bone**  $\Rightarrow$  reference frame (in rest pose)
    - reference frame root bone = object space
- **Skinned** 3D Models
  - Mesh with links: **vertices**  $\Rightarrow$  **bones**
  - $\forall$  vertex: attributes: [ **bone index** , **weights** ]  $\times N_{\max}$
- **Skeletal animations**
  - Sequence of keyframe **poses**
  - $\forall$  pose,  $\forall$  **bone** = a local transform

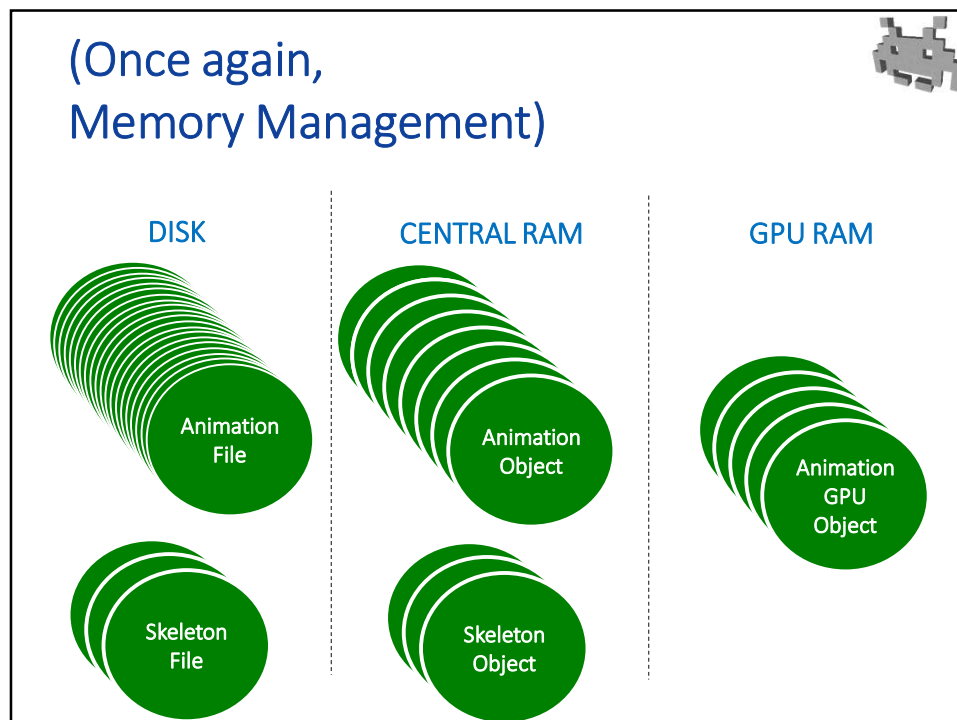
examples of interchange formats (for all three):

- **.SMD** (Valve), **.FBX** (Autodesk), **.BVH** (“behaviour” Biovision)

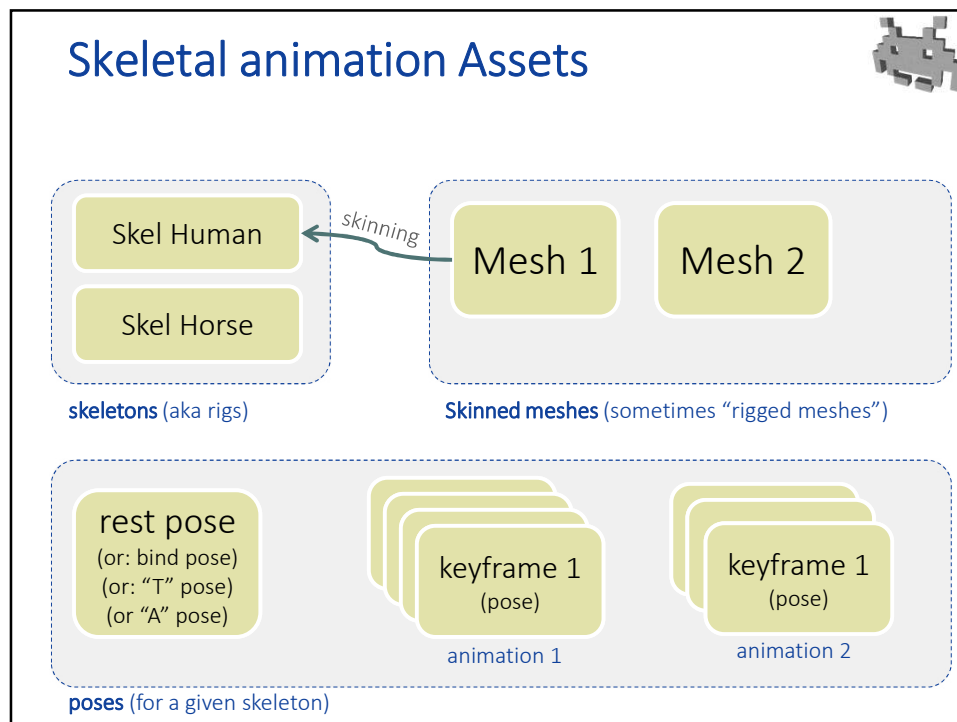
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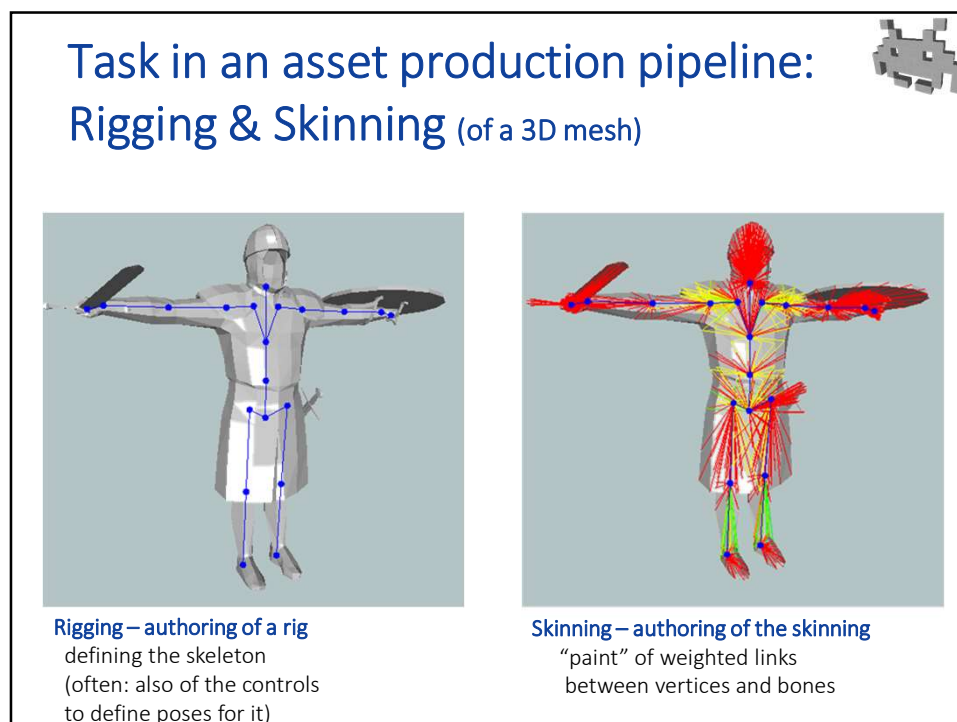
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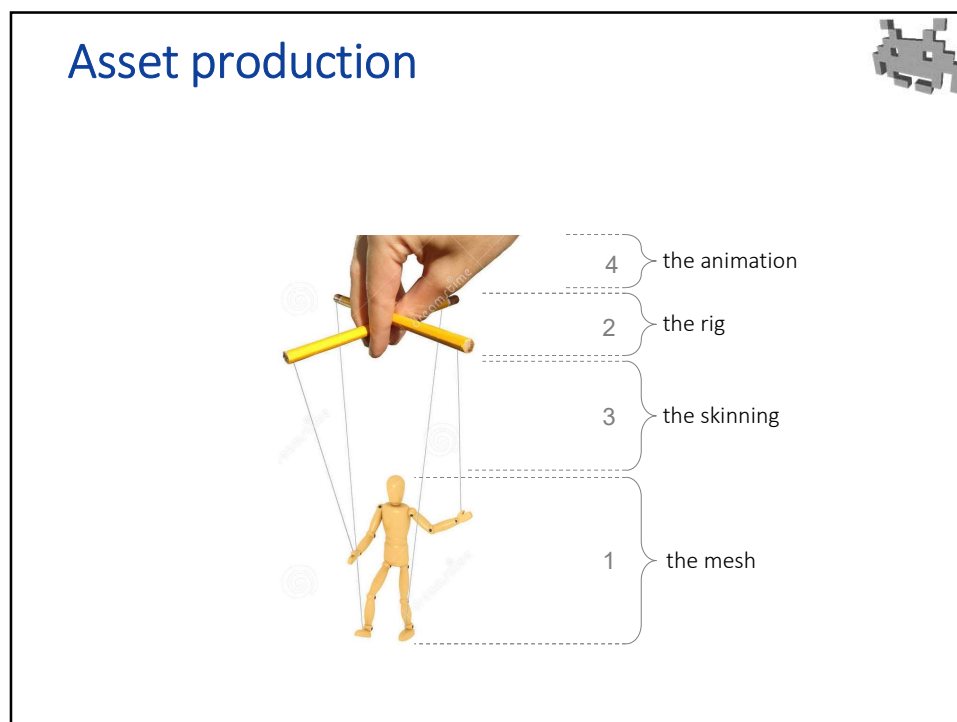
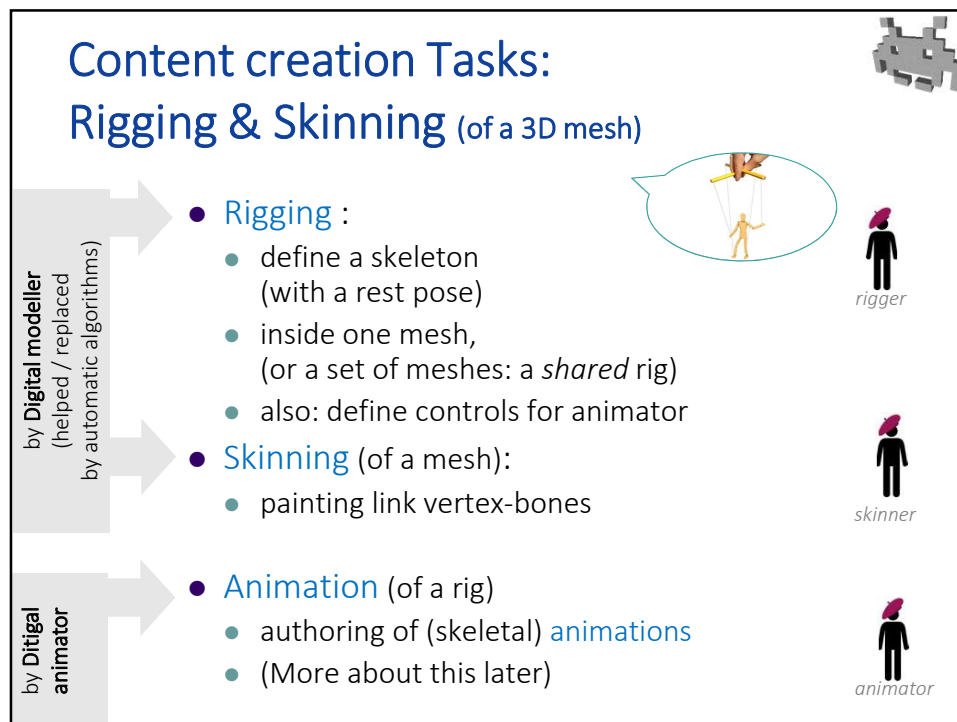
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## Skeletal animations: authoring / obtaining them



- Manual editing
  - digital animators
  - help from:
    - IK (in animation interfaces),
    - physical simulations (for “secondary” animations)
- From physics simulation
  - just use the right set of constraints!  
(easy, in Verlet)
  - in preprocessing (bake them) or  
on the fly: “Ragdolling”
- Or...

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## Skeletal animations: authoring / obtaining them



- Motion capture  
 (“mocap”)



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## Motion capture



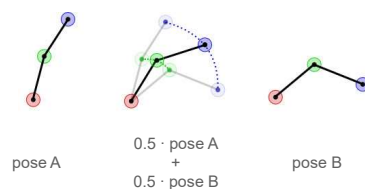
- Requires heavy setup (maybe not in the future?)
  - Markers / suits
  - Controlled cameras
  - Studio
  - Action must take place in a working space
- Requires skilled actors / performers / athletes
- Can be used to capture
  - single animations (a football stunt, walking)
  - joint performances (cutscenes)
- Requires much postprocessing
  - (cleanup, extraction of keyframes)

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## Interpolation poses



- any two poses can be interpolated!



- just interpolate the per bone *local* transform
- attention: this requires re-computation of *final* transforms after interpolation

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