

#### Animation in games

#### but, a note on terminology: in some contexts, procedural means "produced by a *simple* procedure" as opposed to "physically simulated"

#### Non procedural

- Assets!
- Fully controlled by artist/designer (dramatic effects!)
- Realism: depends on artist's skill
- Does not adapt to context
- Repetition artefacts

#### **Procedural**

- Physics engine
- Less control
- Physics-driven realism
- Auto adaptation to context
- Naturally repretition free

4

## Physics simulation in videogames



- 3D, or 2D
- "soft" real-time
- efficiency
  - 1 frame = 33 msec (at 30 FpS)
  - physics = 5% 30% max of computation time
- plausibility
  - but not necessarily accuracy
- robustness
  - should almost never "explode"
  - it's tolerable to have inconsistency in a few frames, as long as it recovers in subsequent ones

# Physics in games: cosmetics or gameplay?

- Just a graphic accessory? (for realism!)
  - e.g.:
    - particle effects (w/o feedback)
    - secondary animations
    - Ragdolling
- Or a gameplay component?
  - e.g. physics based puzzles
  - Popular approach in 2D (since always!)



7

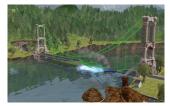
# Physics in games: cosmetics or gameplay? Just a graphic accessory? (for realism!) e.g.: particle effects (w/o feedback) secondary animations Ragdolling Or a gameplay component? e.g. physics based puzzles Popular approach in 2D (since always!)

# Physics in games: cosmetics or gameplay?

- Just a graphic accessory? (for realism!)
  - e.g.
    - particle effects (w/o feedback)
    - secondary animations
    - Ragdolling
- Or a gameplay component?
  - e.g. physics based puzzles
  - Rising trend in 3D







9

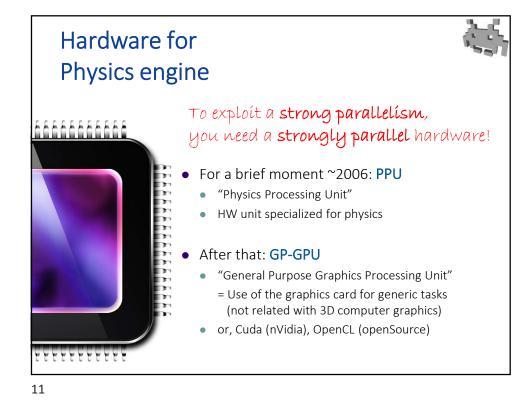
## Physics engine: intro



- Game engine module
  - executed in real time at game run-time
- A high-demanding computation
  - on a very limited time budget!
- ...but highly parallelizable
  - potentially, highly parallel

==> good fit for hardware support

(just like the Rendering Engine)



Main Software (libraries, SDK)

mostly CPU
(Microsoft)

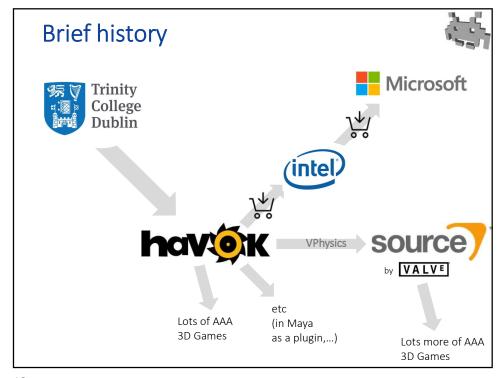
CPU+GPU
(CUDA) NVidia

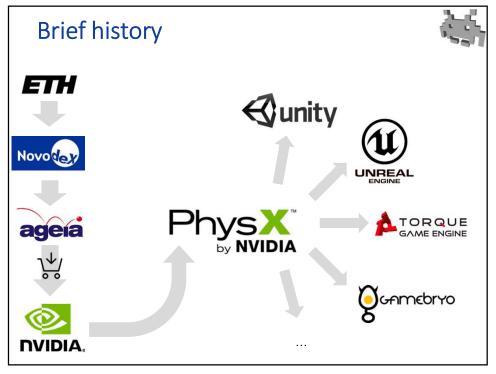
open source, free,
HW accelerated (OpenCL) + CPU

open DYNAMICS ENGINE

Open source, free

2D, open source, free





## The 2 tasks of the Physics engine



#### 1. Dynamics (Newtonian)

for objects such as:

- Particles
- Rigid bodies
- Articulated bodies
  - E.g. "ragdolling"
- Soft bodies
  - Ropes (specific solutions)
  - Cloth (specific solutions)
  - Hair (specific solutions)
  - Free-form deformation bodies (general)
- Fluids
  - Expensive!

#### 2. Collision handling

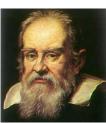
- Collision detection
- Collision response

15

#### **Fields** of study **Dynamics Statics Kinematics** The motion, Equilibrium states, The **motion** itself, no as a result of forces minimal energy states matter why it moves Example: Example: Example: "Subject to gravity, "In which state(s) can "If the angular speed of the this pendulum be still?" pendulum is currently X, how will this pendulum swing?" how fast is the ball moving?" (or vice versa)



# Newtonian Dynamics



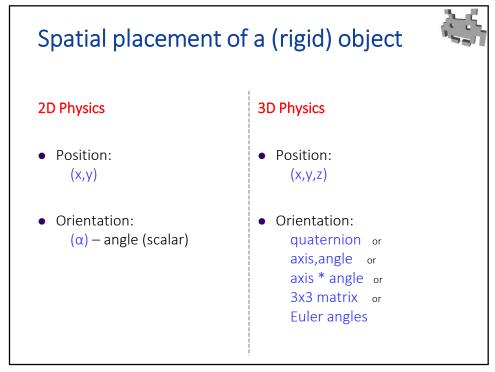


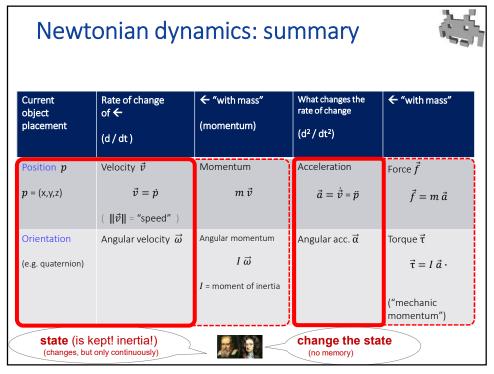
18

# Physics and spaces (observation)



- The scene hierarchy, or the entire distinction between local and global space, its's entirely "in our mind"
  - It's a useful abstraction to control or code scripted animations
  - E.g., kinematics animations, skeletal animations...
- But physics doesn't care about any of it
  - Physics happens entirely in global (world) space
  - Persistent spatial relationships (e.g., between a car and its wheels)
     either exists due to physical constraints, or they are irrelevant
  - Even if they physically exists, they are still enforced in global space, like all the rest of the physics simulation
  - Physics simulation computes changes to objects states (position, orientation...) in global space
  - But, as we know, these updates can be converted/stored in local space



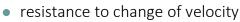


# Per-object constant: mass & its distribution (for non point-shaped ones)



A few quantities associated to each rigid object

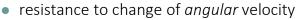
- constants: they don't (normally) change
- input of the physics dynamic simulation, not output
- Mass:





• 16

• Moment of Inertia:





- Barycenter:
  - the center of mass



30

distribution of mas

#### Mass: notes



- resistance to change of velocity
  - also called inertial mass
- also, incidentally: ability to attract every other object
  - also called gravitational mass
  - happens to be the same
- it's what you measure with a scale
- Unity of measure: kg, g, etc...



#### Barycenter: notes



- Aka the center of mass
  - it's a fixed position (for a rigid body)
- It's simply the weighted average of the positions of the subparts composing an object
  - literally "weighted": with their masses
- Does not necessarily coincide with the origin of the local frame of that object
  - but it can
  - otherwhise, it's a fixed point (in local frame)
- In a physical simulation, the position of a rigid body is better described as the position of its barycenter
- In absence of forces, the object rotates (orbits, spin) around this position.

32

#### Moment of inertia: notes 1/3



• Resistance to change of angular velocity





• (an object rotates around its barycenter)

#### Moment of inertia: notes 2/3



- Scalar moment of inertia
  - Resistance to change of angular velocity
  - Depends on the total mass, and also on its distribution
    - the farthest one sub-mass from the axis, the > the resistance
- In 2D: it's a fixed value (for a given rigid object)
  - The object always spins around its barycenter

34

## Moment of inertia: notes 3/3

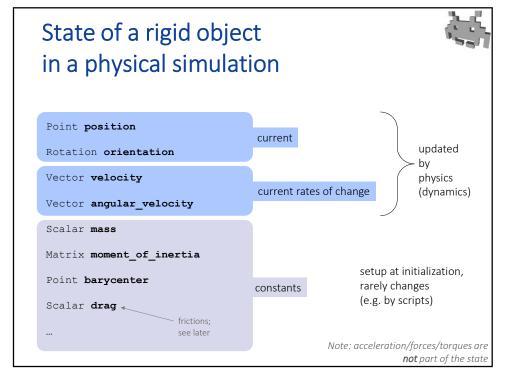


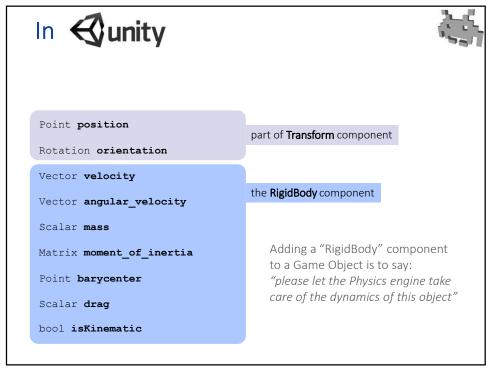
- In 3D: the rigid objects spins around an axis passing through the barycenter
  - for any possible axis of rotation, you have a different scalar moment of inertia
  - ullet for a given axis  $\hat{a}$  the scalar moment is given by

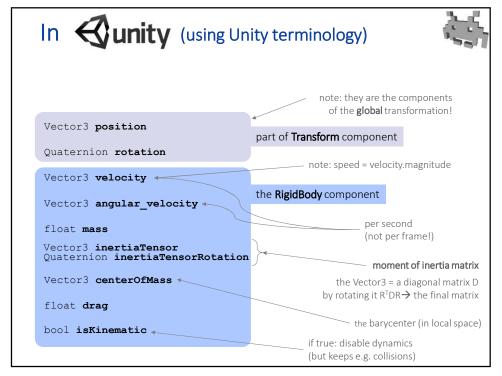
 $\hat{a}^{\mathrm{T}} \mathbf{M} \hat{a}$ 

where 3×3 matrix M is the «(moment of) inertia matrix» aka the «(moment of) inertia tensor»)

- M can be computed for a given rigid object
  - how: that's beyond this course
  - in practice: use given formulas for common shapes
  - or, sum the contributions for each sub-mass
- M describes the scalar moment of inertia for any possible axis or rotation



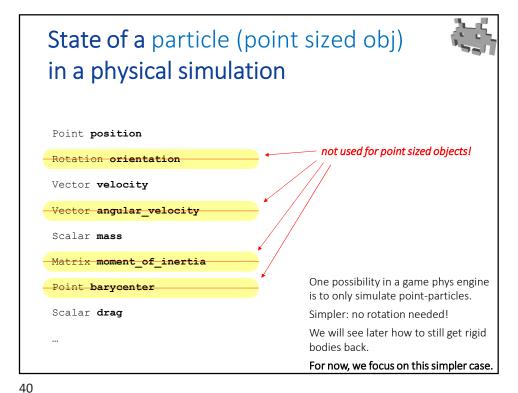




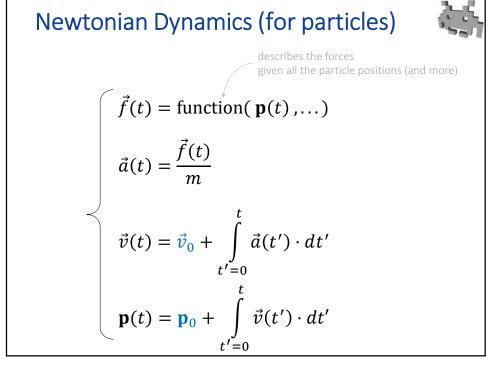
#### The case of particles

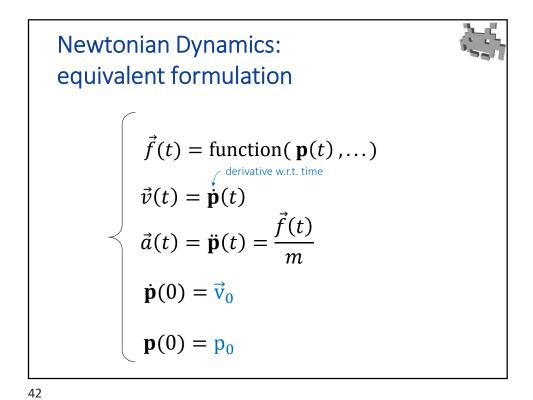


- For now, we will study a simpler case: the dynamics of particles (and its simulation)
- Particle = ideal object shaped like a point,
   with all the mass concentrated in that point
- Particles-only is easier because the orientation (rotation) is irrelevant, and so the following are also irrelevant
  - the center of mass (it's the position of the particle itself);
  - the distribution of mass, i.e. the moment of inertia (there's none);
  - the torques (instead, there's only forces);
  - the angular velocity (instead, there's only linear velocities)
- These things are only relevant again for non-point sized (rigid) objects
- The basic algorithms, however, are the same.



-0





Dynamics (Newtonian)

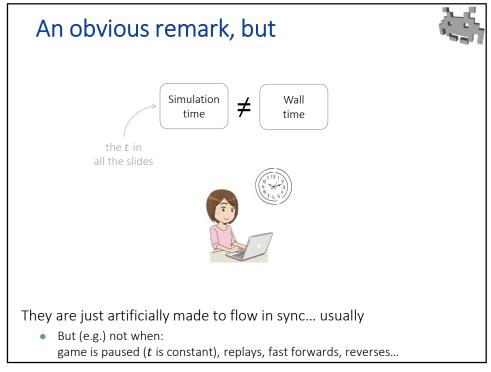
forces

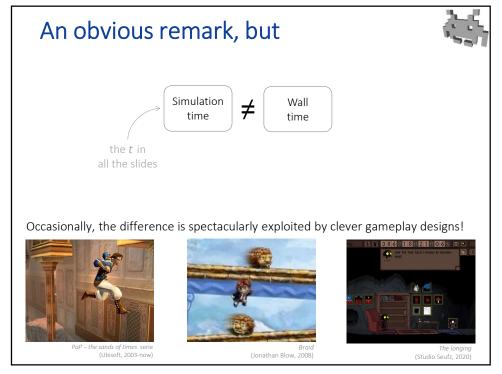
positions

velocity

43

Marco Tarini Università degli studi di Milano





## Computing physics evolution



• Analytical solutions:

Given force functions (and acc), find the functions (pos, vel,...) in the specified relations:

$$\begin{cases} \vec{f}(t_C) = funz(p(t_C),...) \\ \vec{a}(t_C) = \vec{f}(t_C)/m \\ \vec{v}(t_C) = \vec{v}_0 + \int_0^{t_C} \vec{a}(t) \cdot dt \\ p(t_C) = p_0 + \int_0^{t_C} \vec{v}(t) \cdot dt \end{cases}$$

• Numerical solutions:

3. goto 2

46

## **Analytical solutions**

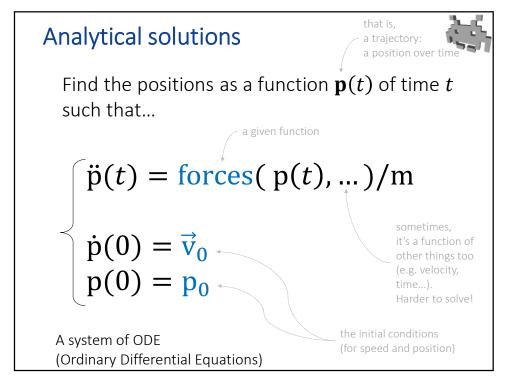


$$\mathbf{p}(t) = \text{some function of } t$$

$$\vec{v}(t) = \dot{\mathbf{p}}(t)$$

$$\vec{a}(t) = \dot{\mathbf{p}}(t) = forces(\mathbf{p}(t), \dot{\mathbf{p}}(t), t, ...)/m$$

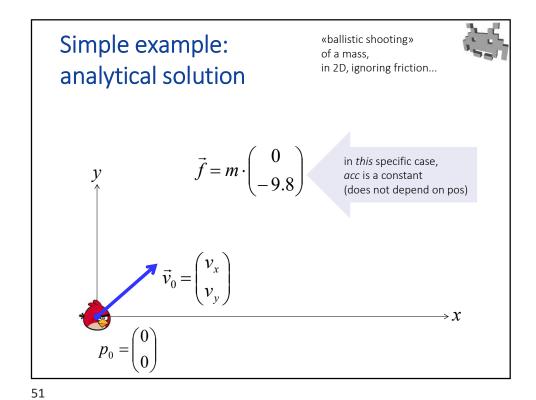
$$\dot{\mathbf{p}}(0) = \vec{\mathbf{v}}_0 \\
\mathbf{p}(0) = \mathbf{p}_0$$

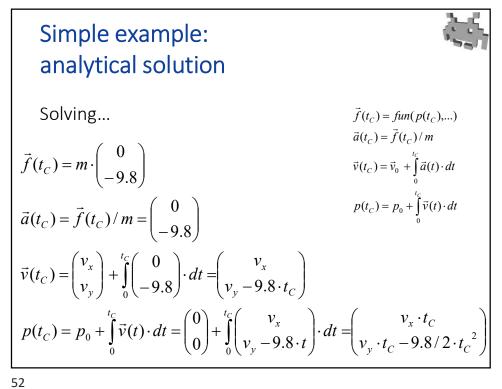


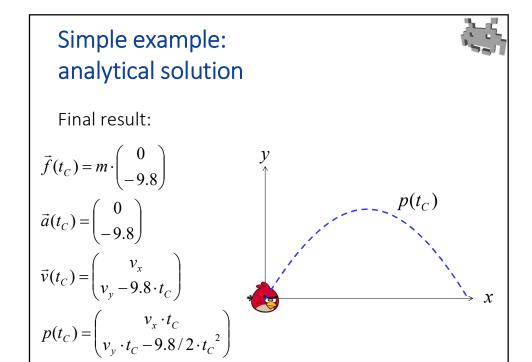
### **Analytical solution**



- Difficult to find
  - a function such that...
- Often, it doesn't even «exist»
  - in a form that we can write using common functions such as polinomials, algebraic functions, exponential trigonometry, etc
- When it exists, they are very convenient
  - we can find the position / the velocity for any given t
  - we can predict the status of the simulation for any given time
- Examples of systems that admit an analytical solution:
  - systems with a force function is constant w.r.t. positions & velocities (solution: just find its integral, twice)
  - two bodies (no more than two!), subject to reciprocal gravity force
  - a single pendulum, if one accepts an approximation (only good for small oscillations)
- Most other systems don't!







## Numerical integration



$$\vec{f}(t_C) = \text{function}(p(t_C), \dots)$$

$$\vec{a}(t_C) = \vec{f}(t_C)/m$$

$$\vec{v}(t_C) = \vec{v}_0 + \int_0^{t_C} \vec{a}(t) \cdot dt$$

$$p(t_C) = p_0 + \int_0^{t_C} \vec{v}(t) \cdot dt$$

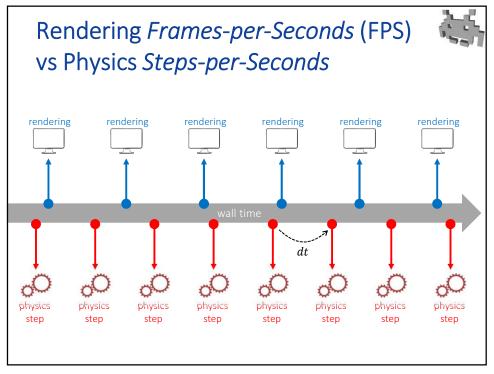
It's our way to solve the ODE

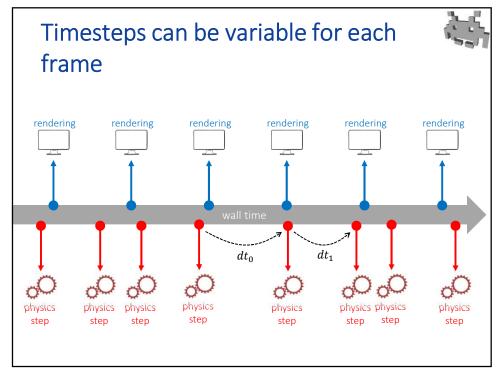
#### Numerical integration



- A numerical integrator computes the integral as summed area of small rectangles
  - For a physics engine, this means just updating velocity and positions at each physics step
- A crucial parameter is the width of the rectangles i.e.
   dt = the duration of the physics step (in virtual time)
  - If physics system perform N steps per second:
     dt = 1.0 sec / N
  - N is not necessarily same rendering frame rate
     e.g.: rendering 30 FPS but physics: 60 steps per seconds
  - dt is not necessarily constant during the simulation (but in most system, it is)

55

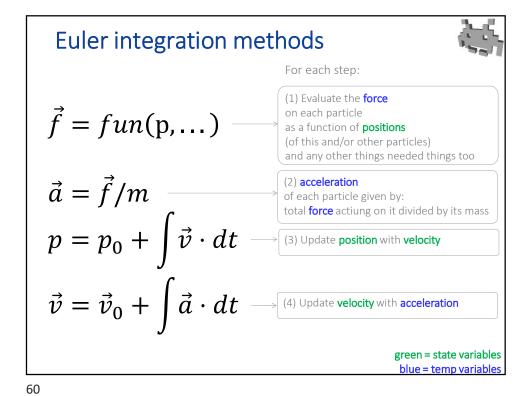


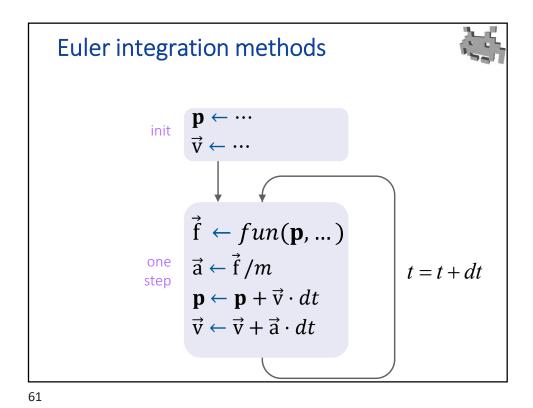


#### Numerical methods: features



- How efficient / expensive
  - must be at least soft real-time
    - (if from time to time computation delayed to next frame, ok)
- How accurate
  - must be at least plausible
    - (if stays plausible, differences from reality are acceptable)
- How robust
  - rare completely wrong results
    - (and <u>never</u> crash)
- How generic
  - Which phenomena / constraints / object types is it able to recreate?
  - requirements depend on the context (ex: gameplay)





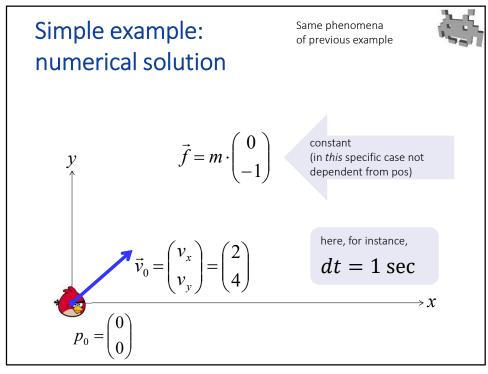
Marco Tarini Università degli studi di Milano

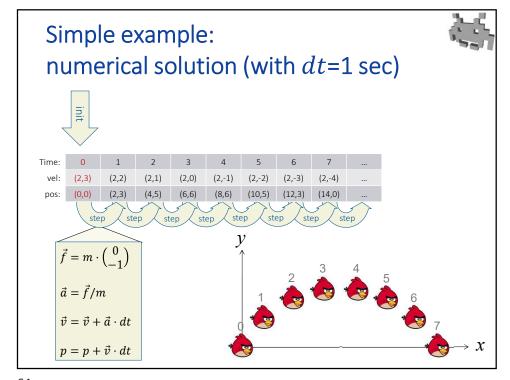
#### Forward Euler pseudo code

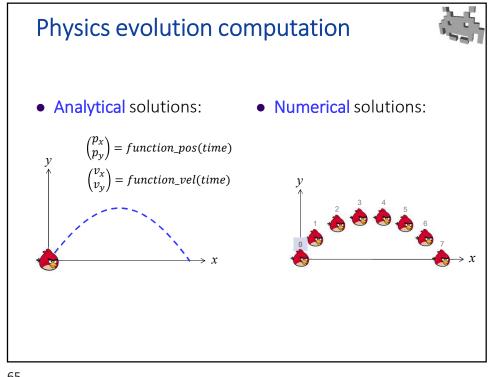


```
Equivalent to...
Vec3 position = ...
                                           \vec{f_i} = function(p_i, \dots)
Vec3 velocity = ...
                                           \vec{a}_i = \vec{f}/m
\vec{v}_{i+1} = \vec{v}_i + \vec{a}_i \cdot dt
void initState(){
   position = ...
   velocity = ...
                                           p_{i+1} = p_i + \vec{v}_i \cdot dt
void physicStep( float dt )
   Vec3 acceleration = compute_force( position ) / mass;
   position += velocity * dt;
   velocity += acceleration * dt;
void main(){
  initState();
  while (1) do physicStep( 1.0 / FPS );
```

62







#### Physics evolution computation



- Analytical solutions:
  - Super efficient!
    - Close form solution
  - Accurate
  - Only simple systems
  - Formulas found case by case (often they don't even exist)
  - NOT USED
     (but, for instance, useful to to make predictions for, e.g. A.l.)

- Numerical solutions:
  - Expensive (iterative)
    - but interactive
  - Integration errors
  - Flexible
  - Generic
  - USED FOR DYNAMICS

66

### Integration errors



- A numerical integrator only approximates the actual value of the integrals
- The discrepancy (simulation errors) accumulates with virtual time during all the simulation
- How much error is accumulated?
- It depends on dt
  - smaller  $dt \Rightarrow \text{smaller error}$  (simulation is more accurate) but, clearly
  - smaller dt ⇒ more steps are needed (for simulate the same virtual time)
     ⇒ simulation is more computationally expensive, but smaller errors,

#### Order of convergence



- How much does the total error decrease as dt decreases?
  - That's called the Order of the simulation
  - 1<sup>st</sup> order: the total error can be as large as O(  $dt^1$  )
    - "if the number of physics steps doubles (physical computation effort doubles) dt becomes halves and errors can be expected to halve"
    - The error introduced by each single step is O( $dt^2$ ),
  - The Euler seen is 1st order
    - This is not too good, we want better
    - Note: The error is usually not that bad as linear with *dt*, but they *can* be

68

# The integration step dt of any numerical methods (summary)



number of physics

steps per sec, or «physics FPS»

dt : delta of virtual time from last step

- the "temporal resolution" of the simulation!
- if large: more efficiency
- fewer steps to simulate same amount of virtual time
- if small: more accuracy
  - especially with strong forces and/or high velocities
- Common values: 1 sec / 60 ... 1 sec / 30
  - i.e. a step simulates around 16 ... 32 msec. of virtual time
  - note: it's not necessarily the same refresh rate of rendering (FPS of rendering ≠ FPS of physics. Rendering can be less!)
  - note: dt is not necessarily the same in all physics steps (need more accuracy now? Decrease dt