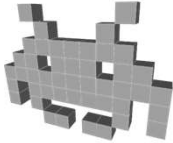


3D Videogames  
Università degli Studi di Milano



Rendering in 3D games  
(bridge lecture)



1

Course Plan



lec. 1: Introduction ●

lec. 2: Mathematics for 3D Games ●●●●●●

lec. 3: Scene Graph ●

lec. 4: Game 3D Physics ●●●●+●●

lec. 5: Game Particle Systems ●

lec. 6: Game 3D Models ●●

lec. 7: Game Materials ●

lec. 8: Game Textures ●●

lec. 9: Game 3D Animations ●●●

lec. 10: 3D Audio for 3D Games ●

lec. 11: Networking for 3D Games ●

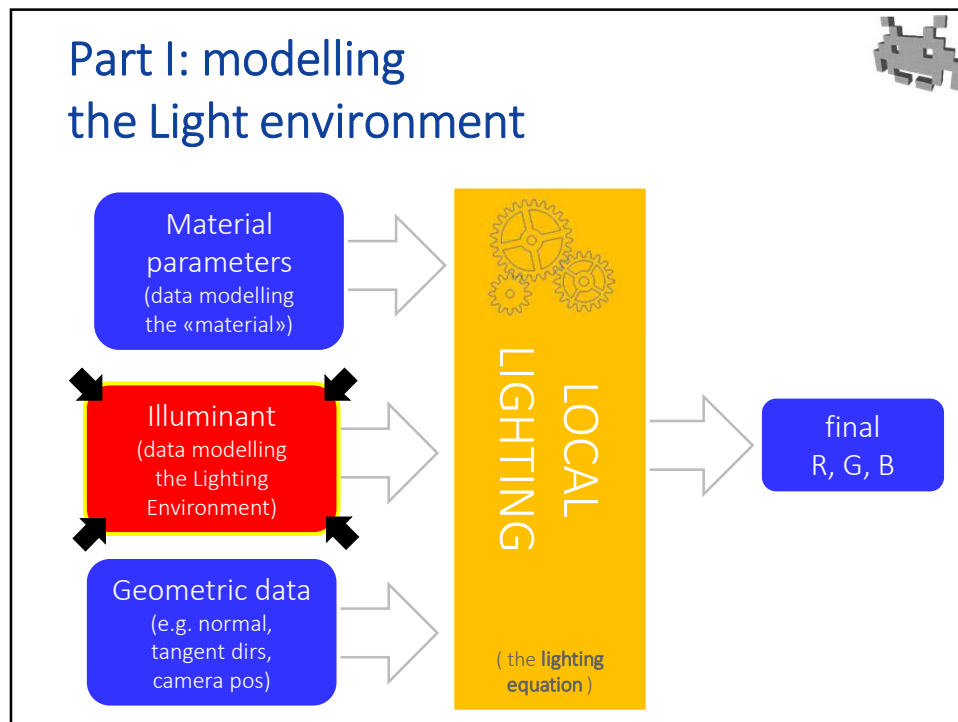
lec. 12: Artificial Intelligence for 3D Games ●

lec. 13: Rendering in 3D Games ●

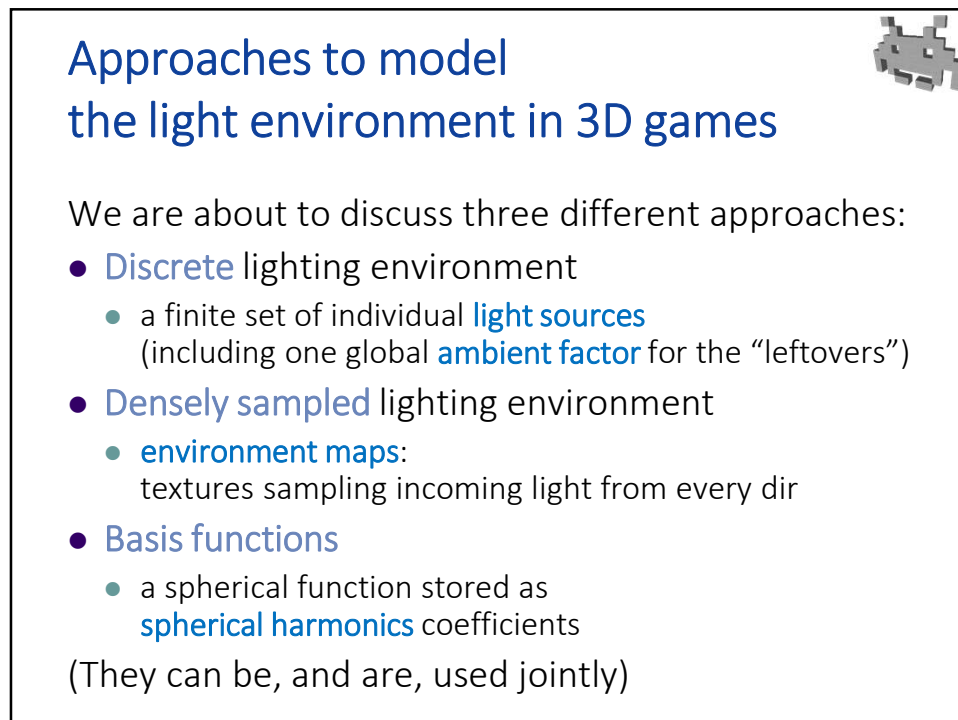
For a more general, deeper discussion of many of the subjects of this lecture, see the courses  
CG  
«Computer Graphics»  
and  
RTGP  
«Real-Time Graphics Programming»

  
bridge lectures

2



3



4

### A simple lighting equation (recap)

$$\begin{aligned}
 & \underbrace{(\hat{n} \cdot \hat{L}) \begin{pmatrix} d_R \\ d_G \\ d_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix}}_{\text{diffuse term}} + \underbrace{(\hat{n} \cdot \hat{H})^E \begin{pmatrix} s_R \\ s_G \\ s_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix}}_{\text{specular term}} + \underbrace{\begin{pmatrix} a_R \\ a_G \\ a_B \end{pmatrix} \otimes \begin{pmatrix} A_R \\ A_G \\ A_B \end{pmatrix}}_{\text{The "ambient" term (once)}} \\
 & \quad \quad \quad \text{nlerp}(\hat{V}, \hat{L}, 0.5) \\
 & \quad \quad \quad \text{the «half-way» vector}
 \end{aligned}$$

● material parameter  
● light parameter  
● 3D geometric data

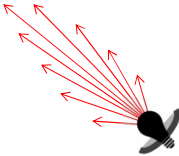
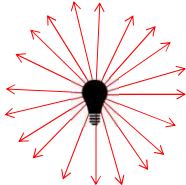
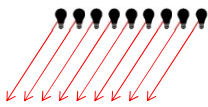
5

### Discrete illumination environments: a set of individual *light sources*

- a finite set of “light sources”...
  - not too many (e.g.  $\leq 16$ )
  - if more, can be assigned “priorities” to pick a subset for every object being rendered
- each light sits in a node of the scene-graph!
- each light can be of one type...

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Lights sources types & their attributes



directional lights

- intensity / color
- direction

point lights

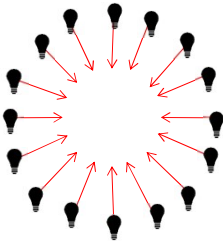
- intensity / color
- position
- falloff function (opt.)

spot-lights

- intensity / color
- position
- direction
- falloff function (opt.)
- angular falloff funct.
- “cookie” texture

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Lights sources types & their attributes



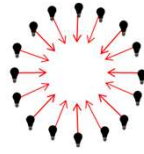
ambient light

- intensity / color
- (that’s it)

but can be shadowed  
AMBIENT OCCULSION  
term.  
E.g., stpred per-textel or  
per-vertex

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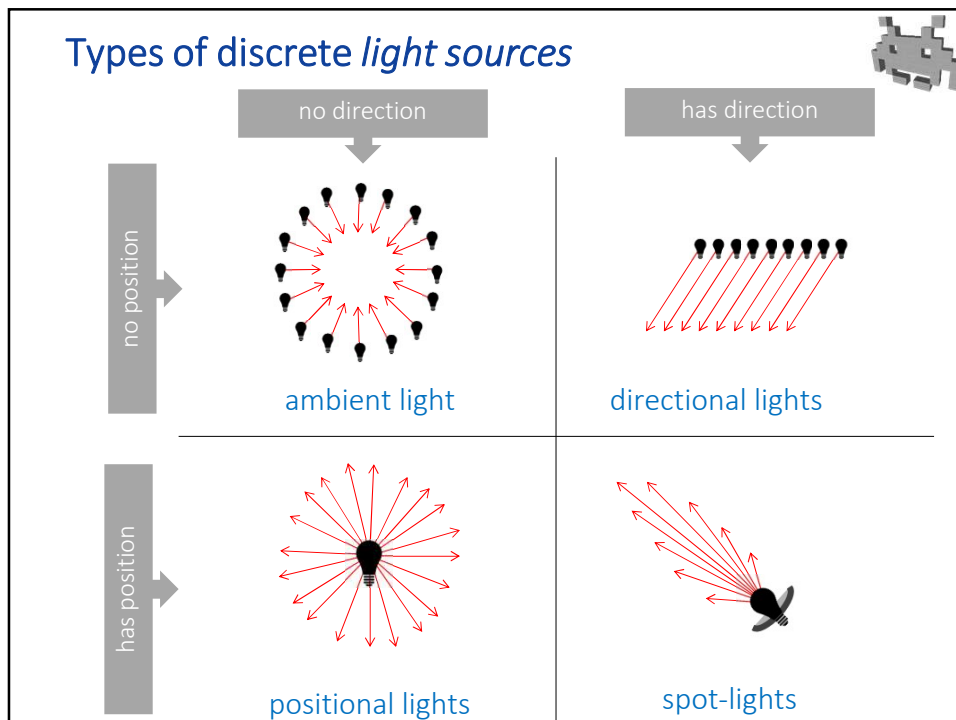
## Ambient light



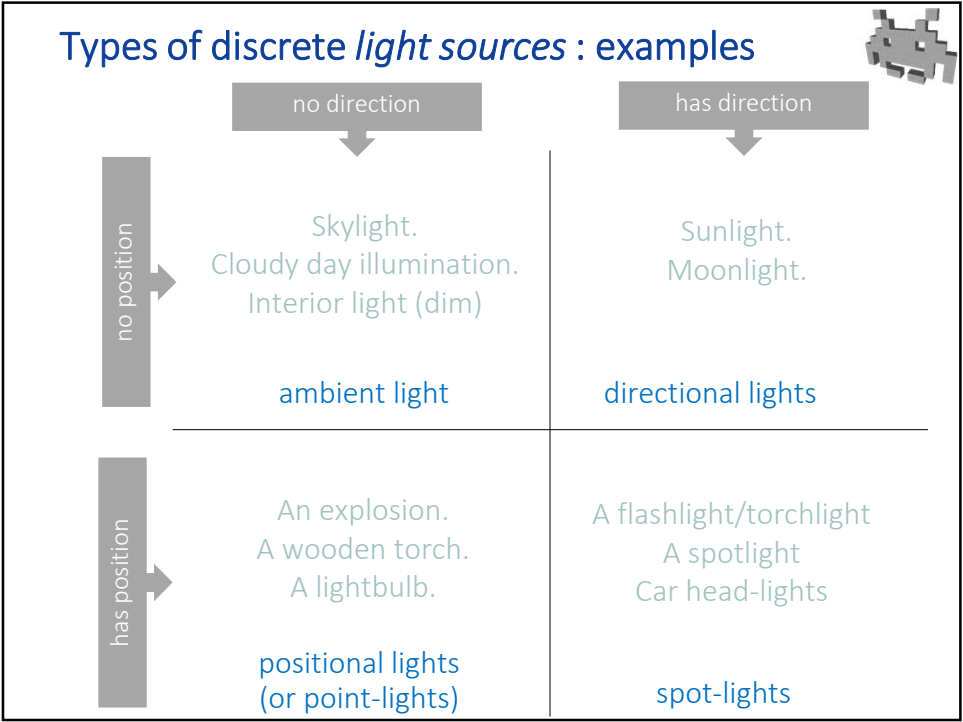
- models other all minor light sources + bounces
  - light incoming “from every direction at every position”
- examples:
  - in an overcast outdoor scene: it’s *high*
    - dim shadows, flat looking lighting:  
every photographs’ favorite for portraits!
  - in realistic outer space: it’s *zero*
  - in any other scenes : *something in between*
    - e.g., sunny day, or a torch-lit cave
- the lighting env. includes only one (or zero) lights of this type
- All other light sources are spatialized
  - Thus, they reside in the scene graph!

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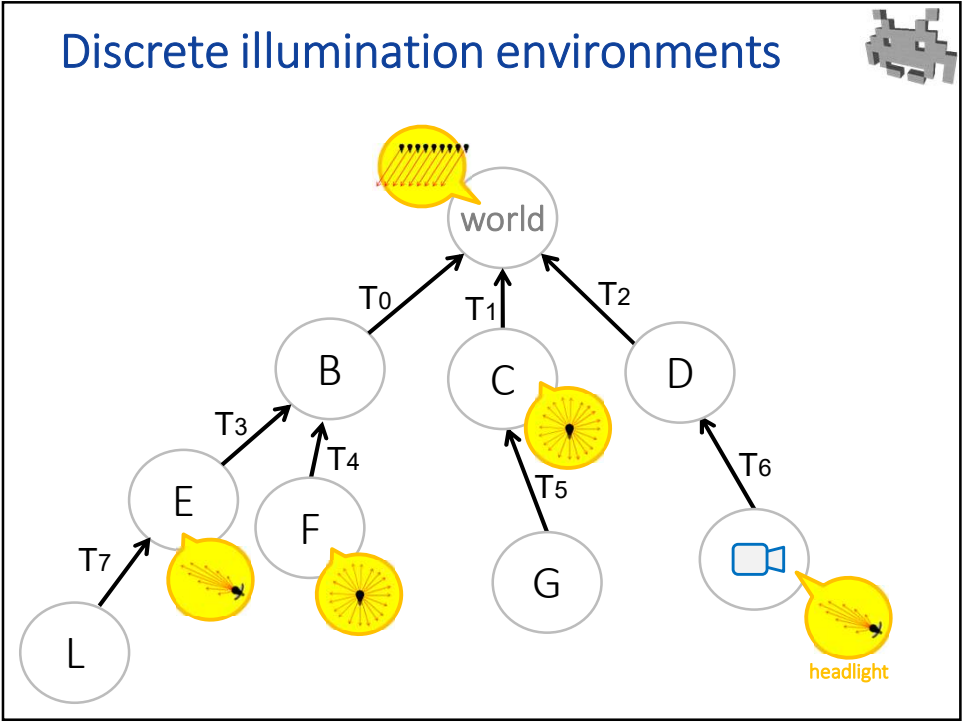
## Types of discrete light sources



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## Distance fall-off functions for positional lights & spotlights

- The **light intensity** of **positional lights** and **spotlights** can be dimmed down with distance from light-pos  $P_L$  to the pos of the fragment being lit  $P_P$ , scaling it by some positional «fall-off» function

$$f_P(\|P_L - P_P\|)$$

- In the real physical world,  $f_P(d) = 1/d^2$
- Other functions can be used, for example  $f_P(d) = 1/d$



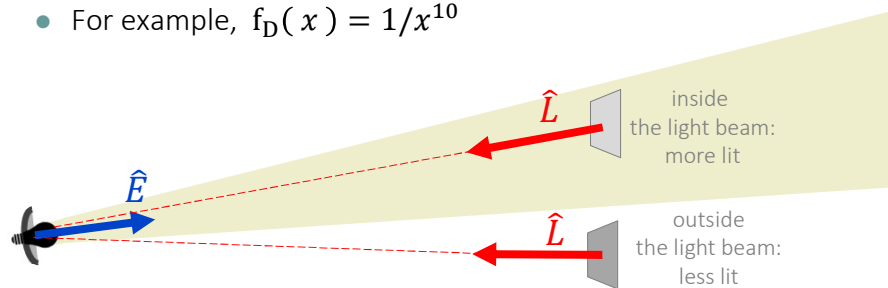
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## Angular fall-off functions for spotlights

- For **spotlights**, the **intensity** is also dimmed down by an «angular fall-off» function, when the direction of the light emission  $\hat{E}$  mismatches the light direction  $\hat{L}$ , scaling it by some function

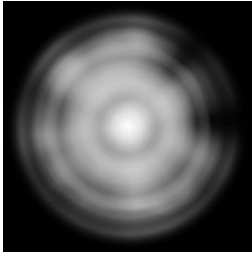
$$f_D(-\hat{E} \cdot \hat{L})$$

- For example,  $f_D(x) = 1/x^{10}$



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Spot-lights:  
they can use a “cookie texture”



as an alternative to angular fall-off functions

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In the lighting equation...

repeat and sum for each discrete light source

the one “ambient” light

diffuse term

specular term

$$(\hat{n} \cdot \hat{L}) \begin{pmatrix} d_R \\ d_G \\ d_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix} + (\hat{n} \cdot \hat{H})^E \begin{pmatrix} s_R \\ s_G \\ s_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix} + \begin{pmatrix} a_R \\ a_G \\ a_B \end{pmatrix} \otimes \begin{pmatrix} A_R \\ A_G \\ A_B \end{pmatrix}$$

Light incoming direction

For directional lights:  
just a constant.

For a point- or spot-light:  $\hat{L} = \frac{\text{pos of light} - \text{pos of lit point}}{\|\text{pos of light} - \text{pos of lit point}\|}$

Light RGB intensity

For a dir. light: a consts.

For point or spot-lights:  
attenuated by falloff functions (of angle, dist)

parameter = of the light

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### Types of discrete lights (a summary)



|                   | Ambient light                                                                                         | Directional light                                                               | Positional light          | Spotlight                                                        |
|-------------------|-------------------------------------------------------------------------------------------------------|---------------------------------------------------------------------------------|---------------------------|------------------------------------------------------------------|
| geometry          | (nothing)<br><i>(assumed at infinite)</i>                                                             | Direction ( <b>versor</b> )<br><i>(assumed at infinite)</i>                     | Position ( <b>point</b> ) | Position ( <b>point</b> ) &<br>Direction ( <b>versor</b> )       |
| can be dimmed by  | -                                                                                                     | -                                                                               | Falloff function          | Falloff function<br>Angular falloff function<br>"Cookie" texture |
| can be blocked by | Ambient Occlusion<br>either baked (per-vertex or per-textel) or dynamically computed (see SSAO later) | Cast shadows<br>(usually) dynamically computed (see shadow-map technique later) |                           |                                                                  |
| how many          | 0-1                                                                                                   | 0-N                                                                             | 0-N                       | 0-N                                                              |
| parameters        | Color/Intensity ( <b>RGB value</b> )<br>Priority?                                                     |                                                                                 |                           |                                                                  |

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### In which space to compute the lighting?

repeat for each light source

diffuse term

$$\hat{n} \cdot \hat{L} \begin{pmatrix} d_R \\ d_G \\ d_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix}$$

$$\hat{L} = \frac{P_L - P_P}{\|P_L - P_P\|}$$

specular term

$$\hat{n} \cdot \hat{H}^E \begin{pmatrix} s_R \\ s_G \\ s_B \end{pmatrix} \otimes \begin{pmatrix} L_R \\ L_G \\ L_B \end{pmatrix}$$

$$\text{nlerp}(\hat{V}, \hat{L}, 0.5)$$

the «half-way» vector

ambient term

$$\begin{pmatrix} a_R \\ a_G \\ a_B \end{pmatrix} \otimes \begin{pmatrix} A_R \\ A_G \\ A_B \end{pmatrix}$$

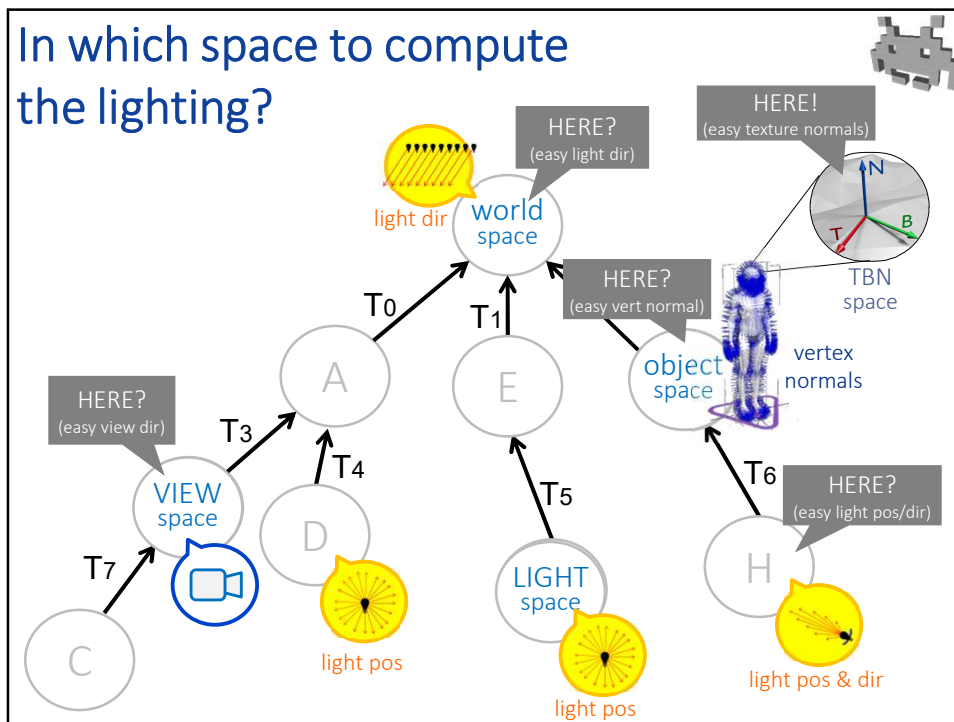
emission term

$$\begin{pmatrix} e_R \\ e_G \\ e_B \end{pmatrix}$$

3D Point / Vector / Versor

Q : in which space to express them (and the others like them)?  
A: whichever!  
As long as it's the same space

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### In which space to compute the lighting?

- All **versors** that used in the **lighting equation** must be expressed in the **same space**
  - view direction, light directions, half-way vector, normals, tangent dirs...
- Choice: which space to use?
  - View space? (the space of the camera)
  - World space?
  - Local object space? (the space of the object currently being rendered)
- With normal maps, usually the most efficient solution is:
  - Use the same space the normals are expressed
  - For normal stored as attribute: the Local Space (aka Object Space)
  - For Tangent Space normal maps: in the the TBN space. Then...
  - ...all other versors must be transformed into this space, *per vertex!*
  - ...the normals accessed from the texture can be used *right away, per pixel!*
  - This minimizes the amount of transformations needed

↑  
for anisotropic materials

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## Discrete illumination environments Summary



- Pros:
  - simple to re-position / reorient individual light sources
    - both at design phase, or dynamically (at game exec)
  - good model of illuminants as:
    - explosions (positional lights)
    - car lights (spot-lights lights)
    - sun direction (directional light)
  - relatively easy to compute (hard, soft) shadows for them
- Cons:
  - each light source requires extra processing ... for each pixel!
    - therefore: hard limit on their number. Prioritize them
    - therefore: are often given a (physically unjustified) radius of effect
  - they don't model well:
    - area light sources (e.g., from back-lit clouds)
    - reflections on metal objects

main illuminants  
of the scene!

see  
shadow  
map  
later

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## Continuous lighting environments



- In general terms, a lighting environment is a function:

$$f : \Omega \rightarrow \mathbb{R}$$

set of unit directions

or  $f : \Omega \rightarrow \mathbb{R}^3$  if we want colored lights

- $f(\hat{d}) \equiv$  **intensity/color** of light coming from dir  $\hat{d} \in \Omega$
- With **discrete** light environments:
  - we define  $f$  only over a few  $\hat{d}$ , with individual lights
  - $f$  is a constant for every other  $\hat{d}$ , with ambient light
  - note:  $f$  is potentially defined differently in every point in the scene (when **positional** light sources are used). Cool!
  - note:  $f$  is dynamic: it's easy to move & turn on/off & change lights from a frame to the next. Cool!
  - But its not super realistic lighting env.

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## Continuous lighting environments



- In general terms, a lighting environment is a function:

$$f : \overset{\text{set of unit directions}}{\Omega} \rightarrow \mathbb{R}$$

or  $f : \Omega \rightarrow \mathbb{R}^3$  if we want colored lights

- $f(\hat{d}) \equiv$  **intensity/color** of light coming from dir  $\hat{d} \in \Omega$
- Let's see two ways to encode a **continuous**  $f$  instead
  - Way 1: environment maps  
(just sample it, store it as a **texture**)
  - Way 2: with basis functions  
(good for very smooth lighting envs)
  - note: for now, we assume  $f$  is the same in everywhere in the scene
  - note: not easy to change  $f$  over time (there are ways – see later)
  - typically, a more realistic lighting env.

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## Densely sampled illumination environments



- A light intensity / color from each direction  $\hat{d}$
- Asset to store that:  
  **"environment map" texture**



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Densely sampled illumination environments

- Latitude/longitude format (of a unit vector  $\hat{d}$ )

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Densely sampled illumination environments

- Aka “sky-map” texture
  - because it doubles as a texture for the “sky boxes”

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## Densely sampled illumination environments

- **Environment map:** (asset)
  - a texture with a texel  $t$  for each direction  $\hat{d}$ 
    - $t$  stores the intensity/color of the light coming from direction  $\hat{d}$
- Q: how to determine  $u, v$  position of  $t$  for a given  $\hat{d}$ ?
  - i.e. how to parametrize (flatten) the unit sphere
- Different answers are possible...

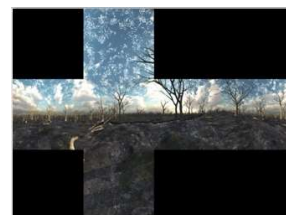
unit vector



latitude/longitude format



mirror sphere  
format



cube-map format  
(ad-hoc HW support!)

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## Environment map (asset)

- A texture with a texel  $t$  for each direction  $\hat{d}$ 
  - $t$  stores the light coming from direction  $\hat{d}$
  - useful to compute reflections on (curved) metallic objects
  - often HDR (see later)
- Pro: realistic, complex, detailed, hi-freq, light env
  - best for mirroring materials (such as metal, glass, water)
- Pro: can be captured from reality
  - see "mat-cap"
- Con: expensive to update for dynamic scenes
  - no prob, for static environments only
- Con: assume far away illuminants
  - Not accurate for close illuminant



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## Environment map (asset): uses

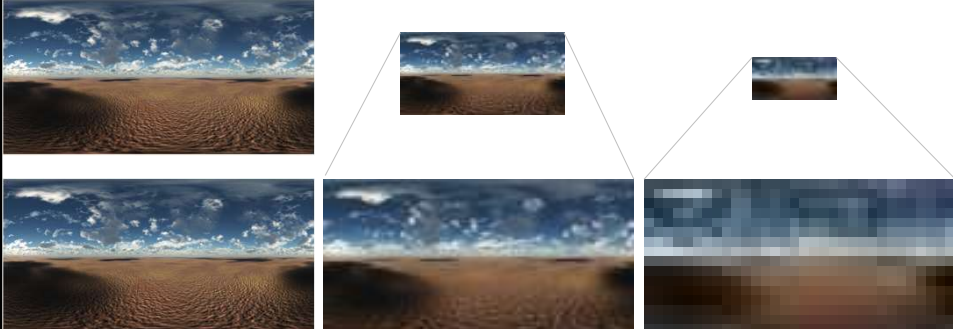
1. Reflection mapping
  - metallic objects
  - in short: material roughness → mipmap level!



Roughness 0  
MIPMAP 0

Roughness 0.25  
MIPMAP 1

Roughness 0.5  
MIPMAP 2



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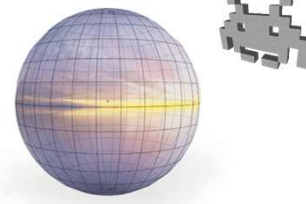
## Environment map (asset): uses

1. Reflection mapping
  - metallic objects
  - material roughness → mipmap level!
2. More generally,  
description of the lighting env
  - for lighting computation
3. Coverage of the background
  - e.g., as a texture covering the 3D “skybox” / “skydome” mesh



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## Skydome / skybox mesh



- A mesh encapsulating the entire scene
  - shows far away objects
  - note: for technical reason, the rendering doesn't show really far away objects – see "far plane clipping"
  - technically, it shows objects at  $\infty$  distance
- Shaped as a large cube/sphere surrounding the scene
- Centered in the same node as the camera
  - so, it "follows the camera": "players can never reach it"
- But rotated as the world frame
  - not as camera!
  - (similar to: the transform of the microphone node)
- The environment map doubles as a color texture over this mesh
  - The sphere is painted with the background objects (stars, sky, mountains on the horizon, etc)

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## Light environments: using Basis Functions



- Lighting environment:
  - a *continuous* function  $f : \Omega \rightarrow \mathbb{R}$
- $f(\hat{v})$  = amount of (rgb) light coming from direction  $\hat{v}$
- Store  $f$  through basis functions

set of all unit vectors  
(i.e., surface of the unit sphere)

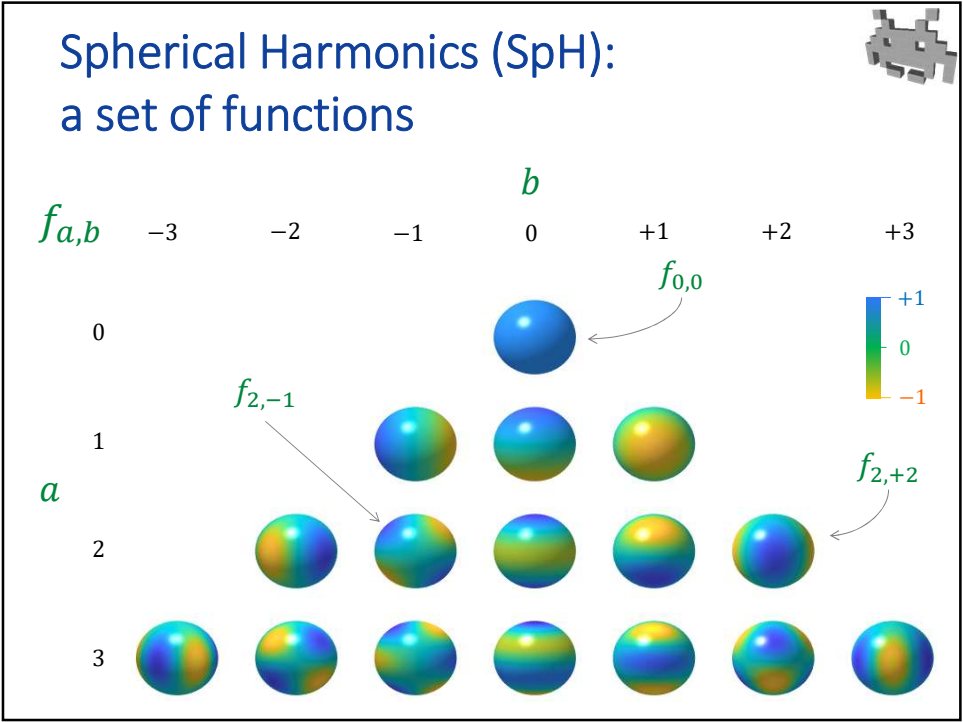
or  $\mathbb{R}^3$  if RGB  
colored light

$$f(\hat{v}) \cong a_{0,0} \cdot f_{0,0}(\hat{v}) + a_{1,-1} \cdot f_{1,-1}(\hat{v}) + a_{1,0} \cdot f_{1,0}(\hat{v}) + a_{1,+1} \cdot f_{1,+1}(\hat{v}) + \dots$$

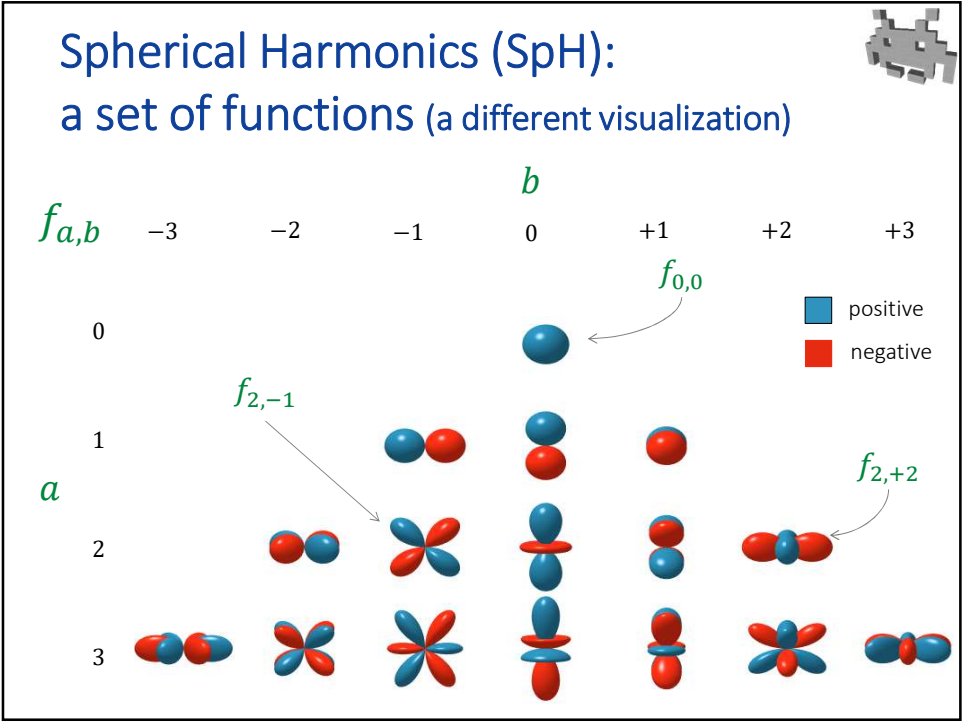
fixed spherical "basis" functions (always the same ones)

a few scalar values to be stored, in order to represent (an approx. of)  $f$

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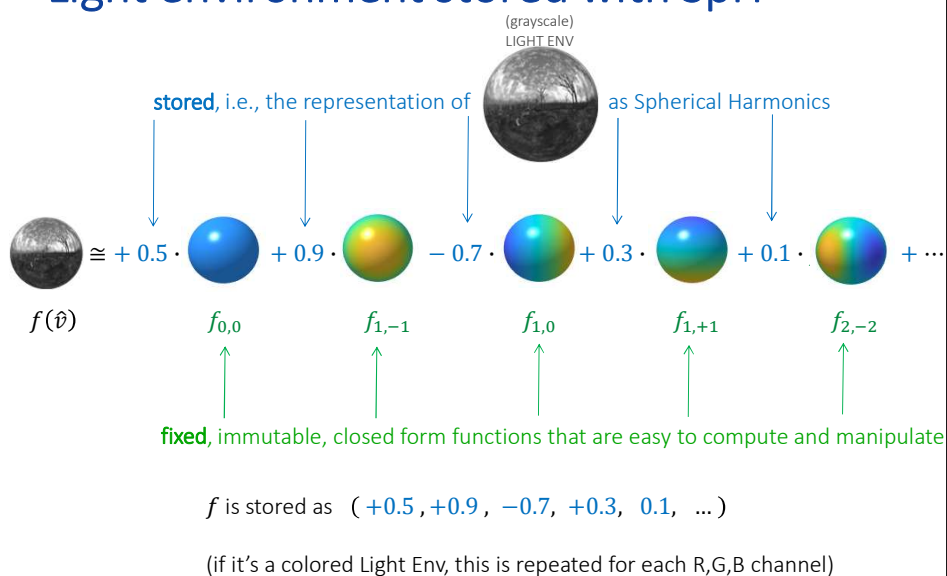
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## Spherical Harmonics (SpH): a good choice for the basis functions

- Spherical Harmonics is a good set of basis functions for spherical functions
- Each function in the set has two indices  $a, b$ 
  - the degree  $a$
  - the order  $b$
- $f_{a,b}(\hat{v})$  with  $a \geq 0, -a \leq b \leq +a$
- $f_{0,0}(\hat{v}) = 1$  a constant function  
(so, scalar  $a_{0,0}$  represent the *total amount* of light)
- all other basis function sum up to 0  
(i.e., their integral over  $\Omega$  is zero)
  - so, they control the distribution not the *quantity*, of light
- they are designed to have useful mathematical properties  
(e.g., orthogonality – the integral of the product of any two is 0)
- all SpH functions are easy to evaluate, integrate, etc

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## Light probes: Light environment stored with SpH



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## Light probes: Light environment stored with SpH



- Spherical Harmonics (SPH) in brief:
  - store Illumination Env as a small number (4,9,16...) of scalar **weights** of as many fixed **spherical basis functions**.
- Pros:
  - very compact representation
  - it models continuous functions well:  
good for smooth lighting environments
  - it allows for efficient computation of the Lighting equation
  - it's easy to interpolate between light envs!
- Cons:
  - continuous functions *ONLY*
    - not good for hi-freq details: for example, no hard lights
    - not sudden variations (unless very many coefficient used)
- Good for soft light env

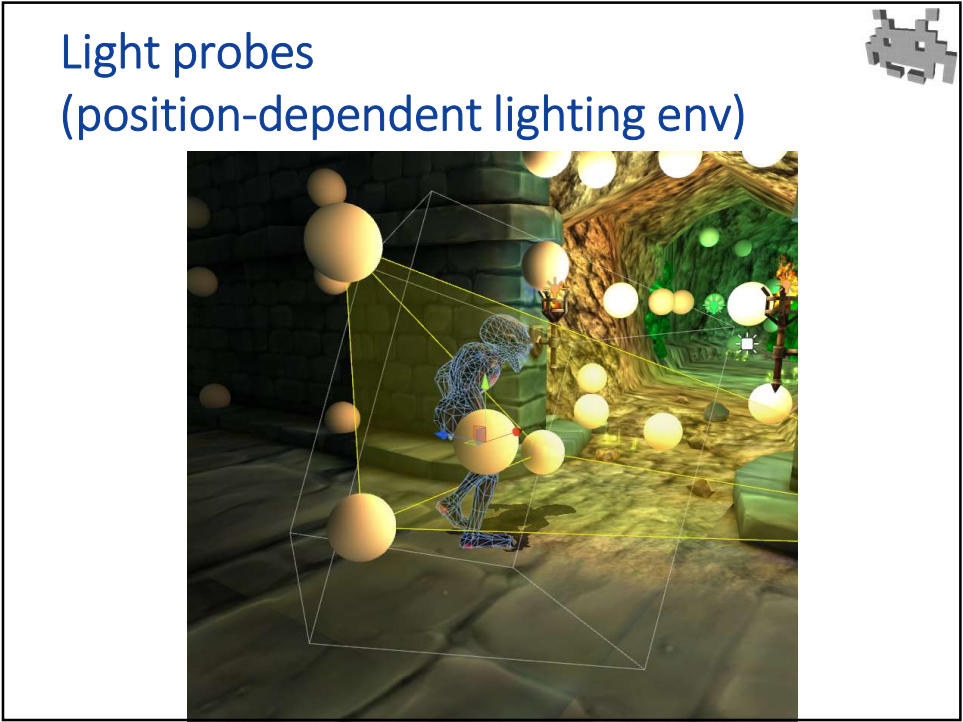
40

## Light probes (position-dependent lighting env)

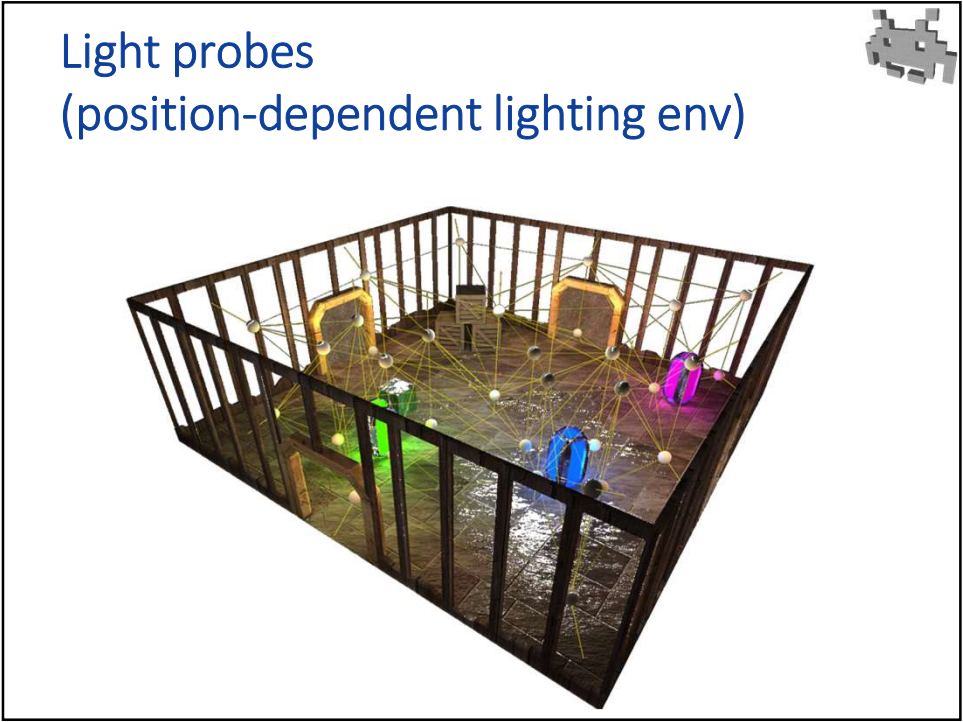


- A light probe == a (precomputed) lighting env.  
to be used around a given 3D position of the scene
- Light Probe lighting:
  - preprocessing: disseminate the scene with light probes
    - Store them as... low-res environment maps
    - ...or, with SPH (the standard solution)
  - at rendering time, for an object currently in pos (xyz),  
use an **interpolation** of near-by "light probes"
    - note: two (or more) SPH function can be interpolated!
    - easy: just interpolate the weights

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## Part II: basics of GPU-based rendering



- Summary:
  - a brief summary of rasterization-based rendering (currently, almost universally adopted in 3D games) (somehow threatened by novel “ray tracing” based approaches)
  - the graphic pipeline and its programmable parts
  - depth-maps
  - double buffering
  - deferred shading
  - multi-pass techniques in general (with examples)

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## Rendering task for in 3D games: overview



- Real time
  - (20 or) 30 or 60 FPS
- Hardware (GPU) based
  - pipelined, stream processing
- therefore: one class of algorithms (hardwired)
  - **rasterization** based algorithm
  - recent trend: switch to **ray-tracing** algorithms?
- Complexity:
  - Linear with # of primitives
  - Linear with # of pixels

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## High-level view of mesh rendering



To render a mesh:

- load in **GPU RAM**:

- ✓ Geometry + Attributes
- ✓ Connectivity
- ✓ Textures
- ✓ Vertex + Fragment Shaders
- ✓ Global Material Parameters
- ✓ Rendering Settings

THE MESH ASSET

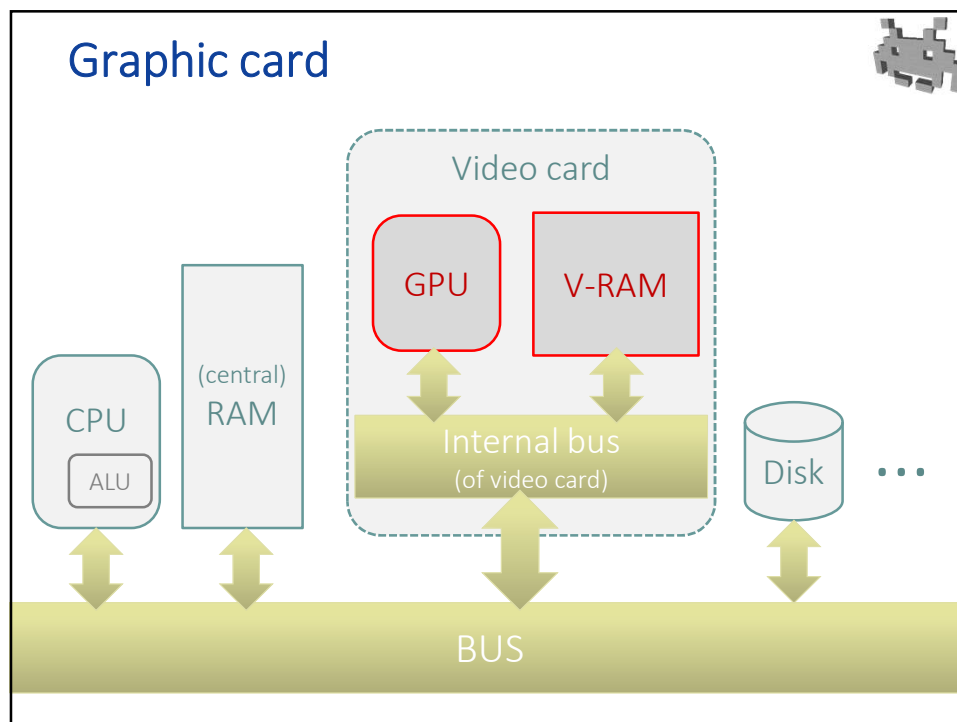
THE MATERIAL ASSET

- issue the **Draw-call**

For this lecture, we need go lower level (a bit)

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## Graphic card



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Rendering of a mesh =  
rasterization of all its triangles

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GPU pipeline –  
a simplified conceptual version

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## Rasterization based rendering: steps (remarks 1/2)



- **Vertex processor: (per vertex)**
  - Input: vertex data (position + initial attributes)
  - Output: a final screen position, and other (refined) attributes
- **Rasterizer: (per triangle)**
  - Input: a triplet of processed vertex (with attributes)
  - Output: many "fragment", one for each pixel covered by the triangle, each with interpolated attributes
- **Fragment shader: (per fragment)**
  - Input: a fragment (with attributes)
  - Output: a final rgb color (plus: an alpha value, plus: a depth value)
- **Output combiner: (per fragment)**
  - Writes the rgb color on the screen buffer
  - Overwrites, blends, or preserves the old value

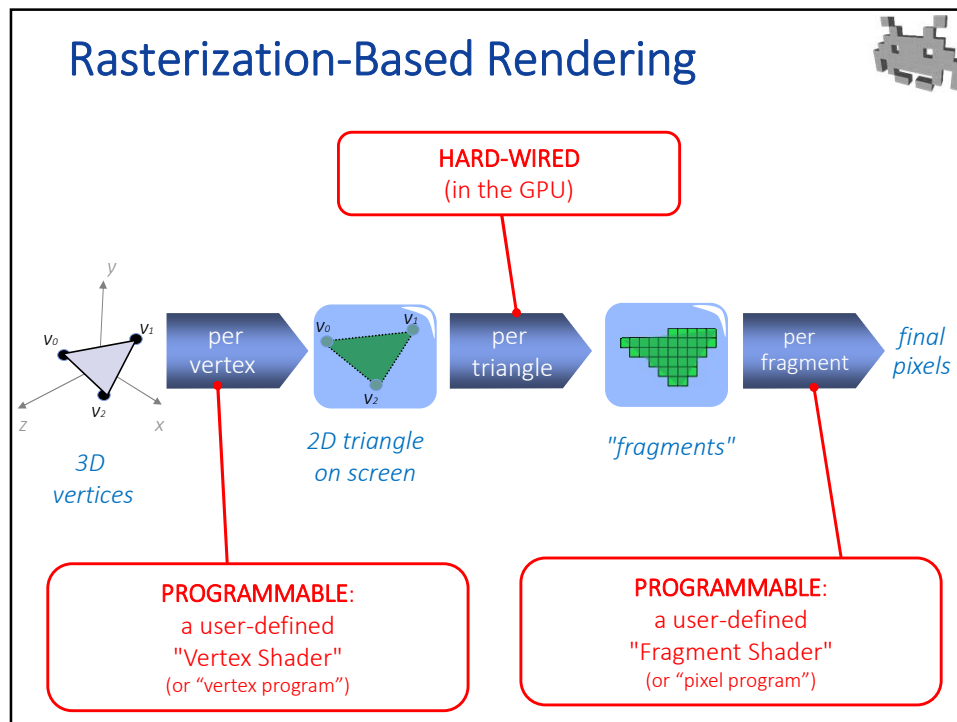
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## Rasterization based rendering: steps (remarks 2/2)

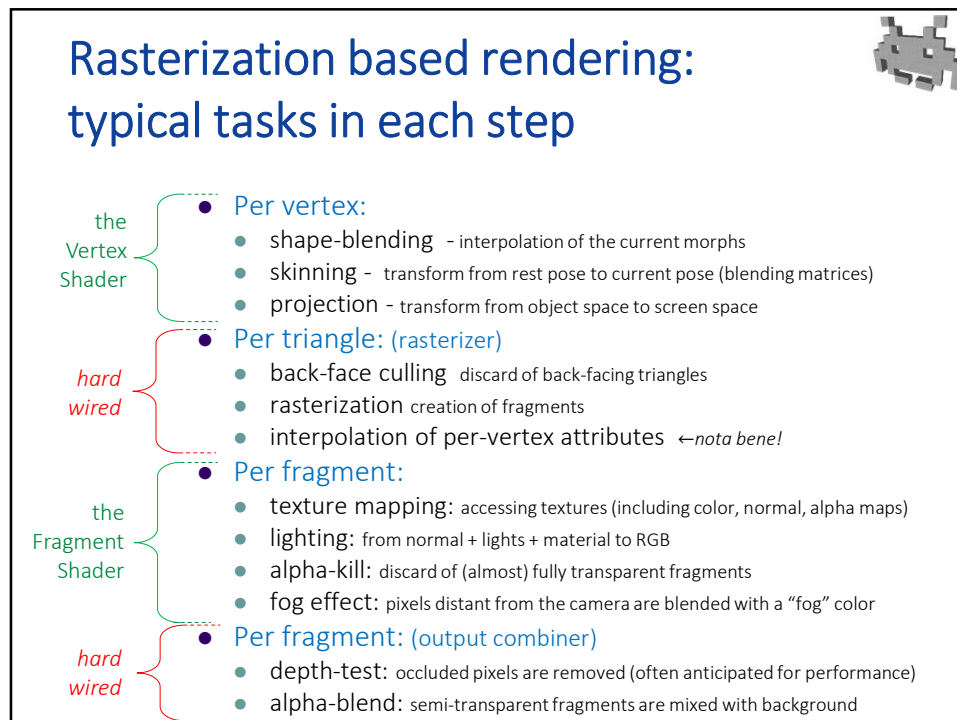


- It's a **pipelined architecture**:  
every step works in parallel with all others
  - E.g., while fragment are processed, the next triangle is being rasterized, and the next vertices are processed
- It's a **SIMD architecture**:  
Every step does the same processing on several inputs, producing several output, all in parallel,
  - E.g., several fragments are processed at the same time (each one independently from the others)
  - E.g., same for vertices

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## GPU pipeline – bottlenecks (remarks and terminology)



- Like in any pipeline, the process goes *as slow as its slowest stage*
  - i.e., the «bottleneck» of the pipeline determines the total speed
  - Any other stage is idle for part of the time (which is always a waste)
    - stages before the bottleneck are «choked» (they wait for the next stage to be ready for their output)
    - stages after the bottleneck are «starved» (they wait for the input from previous stage)
- Terminology about bottlenecks: (in CG)
  - “per vertex” stage is the bottleneck: the app is **geometry-limited** («it cannot process geometry fast enough»)
  - “per fragment” stage is the bottleneck: the app is **fill-limited** («it cannot fill the screen buffer with pixels fast enough»)
- Performances (rendering FPS) of a game only improves if computational load is lifted from the bottleneck phase  
Examples:
  - using all meshes at LOD 2 instead of LOD 0 does not help a fill-limited app
  - reducing the resolution of the screen does not help a geometry-limited app
  - using a simpler lighting model does not help a geometry-limited app

← MORE COMMON CASE, FOR GAMES

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## In many game engines, shaders are part of the “material asset”



To render a mesh:

- load (in GPU RAM):
  - ✓ Geometry + Attributes
  - ✓ Connectivity
  - ✓ Textures
  - ✓ **Vertex + Fragment Shaders**
  - ✓ Global Material Parameters
  - ✓ Rendering Settings
- issue the Draw-call



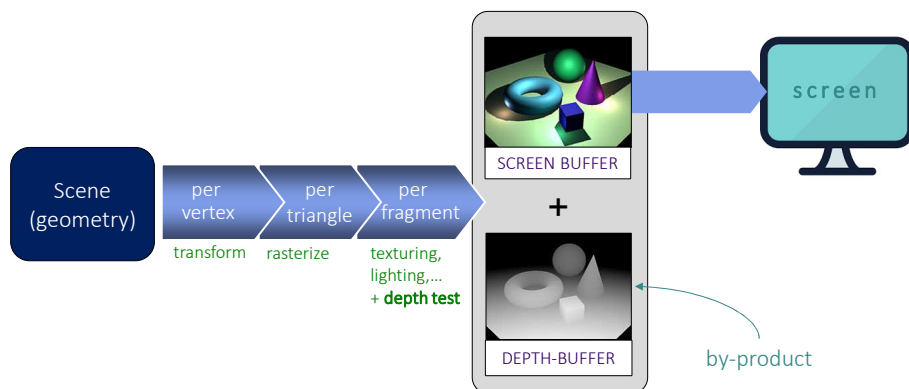
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## Programming languages for writing shaders

- High level:
  - **HLSL** (High Level Shader Language, Direct3D, Microsoft)
  - **GLSL** (OpenGL Shading Language)
  - **CG** (C for Graphics, Nvidia)
  - **PSSL** (PlayStation, Sony)
  - **MSL** (Metal, Apple)
- Low level:
  - **ARB** Shader Program  
(the “assembler” of GPU – now deprecated)

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## basics: Depth buffer



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## Depth buffer (or Z-buffer) (or depth-map)



- Any rendering producing a **screen-buffer** ...
  - which is sent to the screen
- ...also produces a **depth-buffer**
  - as a by-product!
  - not sent to the screen: it's an "offline" buffer
  - it's used during the rendering to determine occlusions and remove "hidden surfaces" (i.e., make what is behind something else is not seen, because it's occluded by that something)
  - see the Computer Graphics course for more details
- many rendering algorithms exploit the depth-buffer
  - for different uses
  - for each pixel on the screen, we have not only its RGB value, but its depth value (a scalar from 0 – close to the camera, to 1 – far from the camera)

a 2D array  
of **RGB values**  
of some  
resolution

a 2D array  
of **depth values**  
(scalars in 0 to 1)  
of the  
same resolution

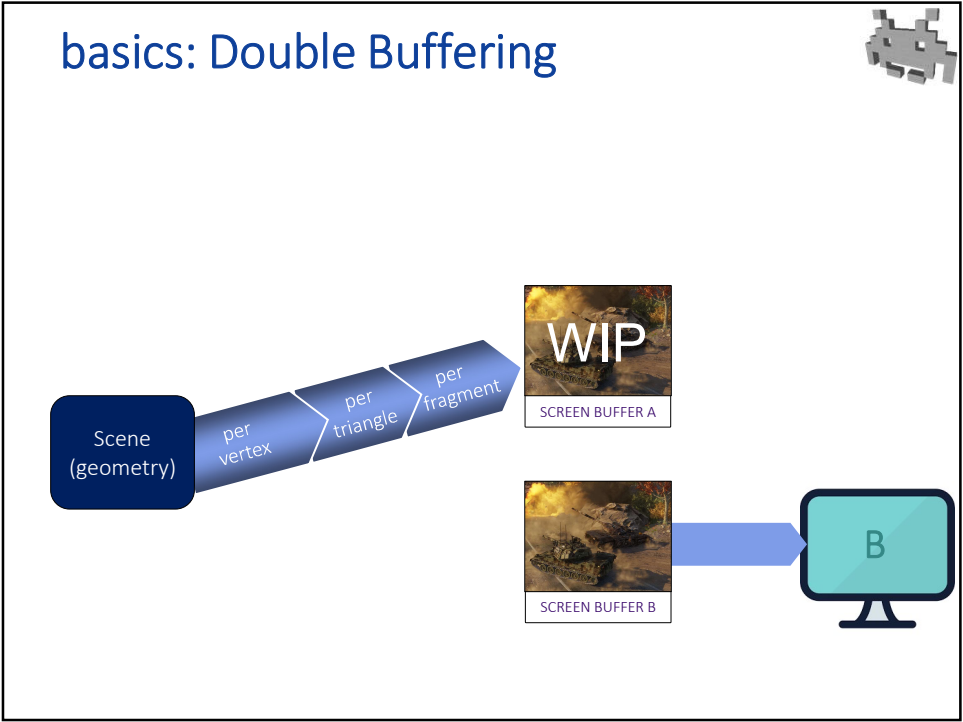
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## basics: Double Buffering

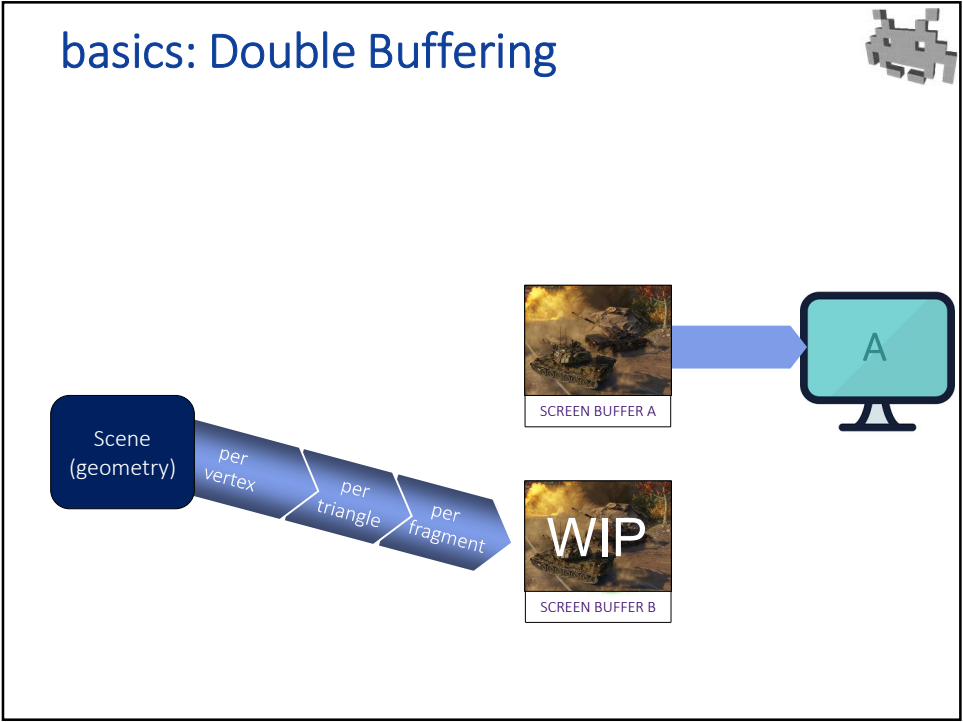


- To render a scene, all meshes are rendered succession
  - Filling the screen buffer
- Double-buffering is a basic technique to prevent any incomplete buffer to ever reach the screen
  - E.g., a rendering where some of the meshes is still not rendered
- How it works:
  - We have two RGB buffers: the front-buffer and the back-buffer
  - The **front buffer** shows the last complete rendering and is the one the screen shows
  - The **back buffer** is filled by the renderings, but it is not shown (it's yet another example of "off-screen buffer")
  - Screen Swap: When the back buffer is ready, the two buffer are swapped (instantaneously)
  - Info about variants: look up what "V-sync" means in 3D games settings
  - Observation: no need to double the depth-buffer

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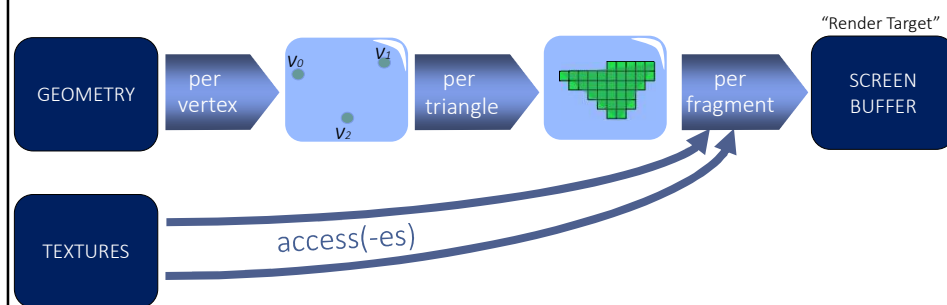
## Off-screen buffers



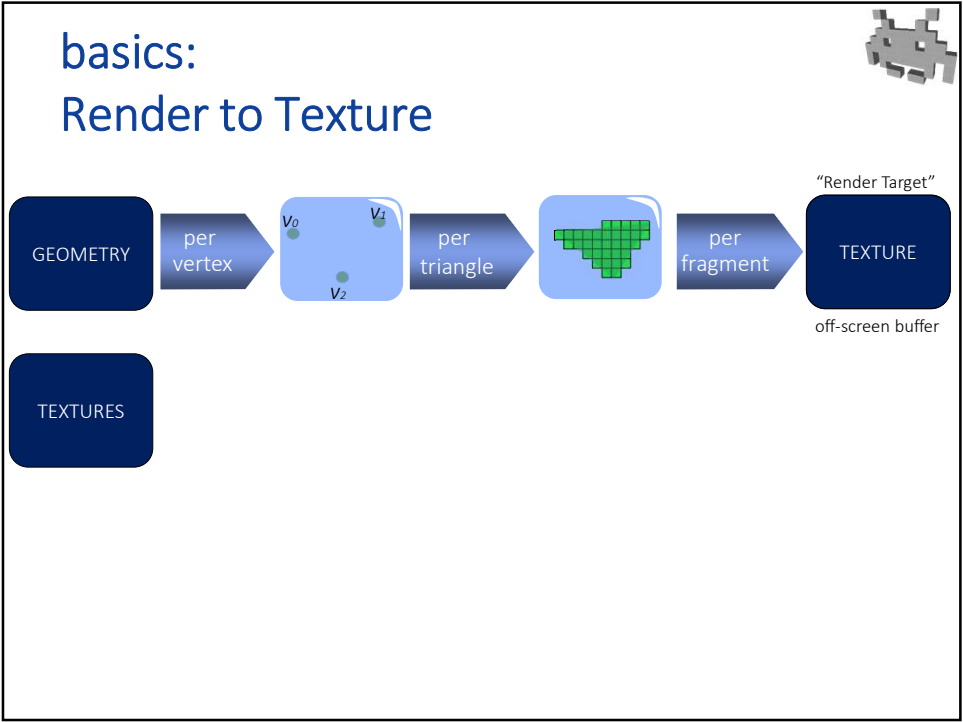
- The rendering produces a **screen buffer** (2D array of RGB pixel) that is sent to the screen and is made visible to the player
- Any buffers that is used internally but and not sent to the screen is called an **off-screen buffer**
  - Example: the **depth buffer** (2D array of depth values)
  - Example: the **back-screen buffer** (double buffering techniques)
- Many rendering techniques are based on producing an off-screen buffer *then* using it in another pass
  - For example, to re-using it a texture in another rendering pass

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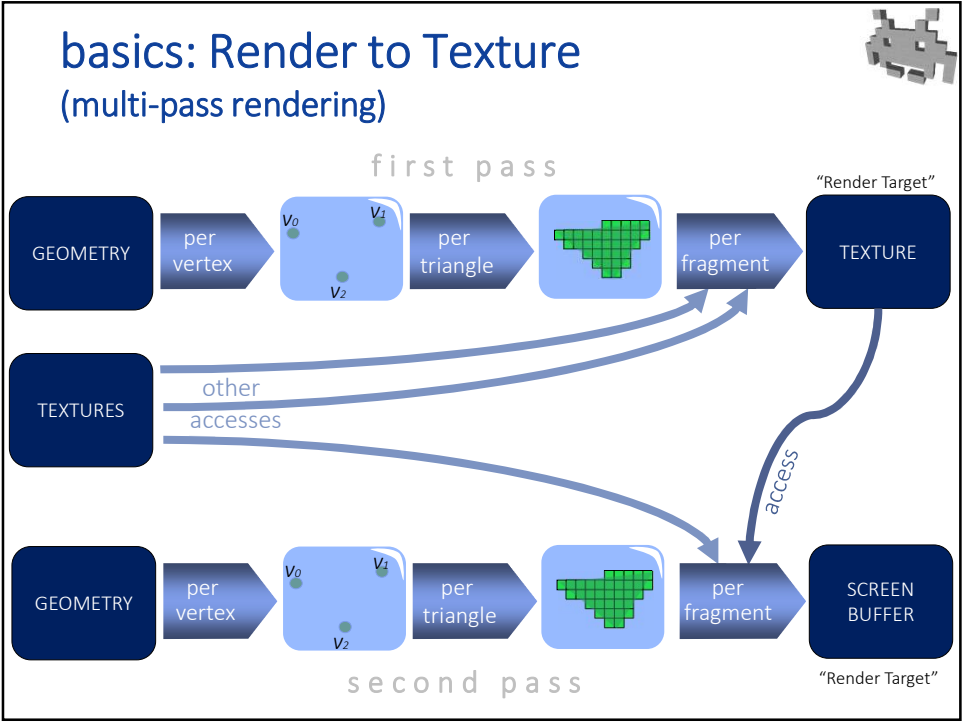
## Texture access: it's in the per fragment process



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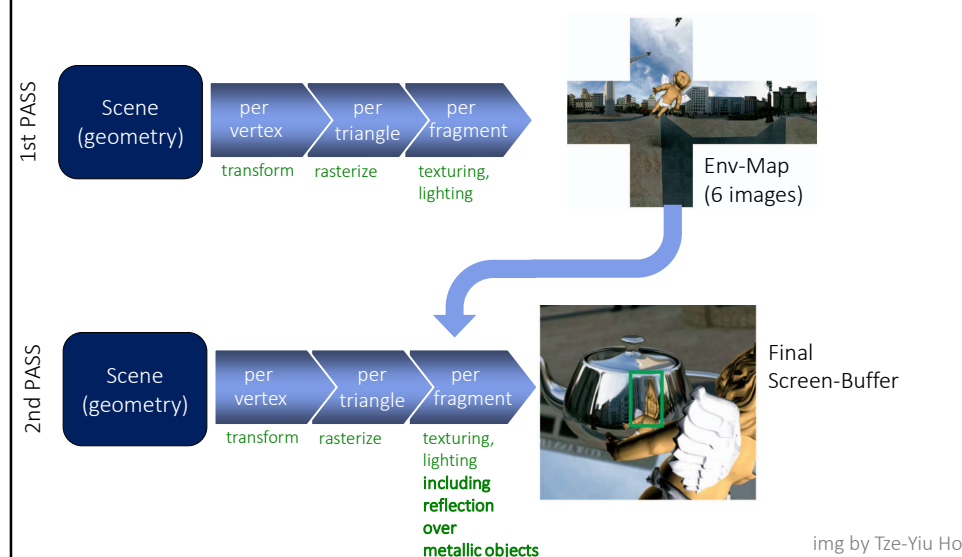
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## Multipass rendering techniques (a wide class of rendering techniques)

- 1<sup>st</sup> pass: fill an **internal 2D buffer**
  - an “**off-screen**” buffer
  - the output of this rendering, i.e. its “**render target**”
  - normally, the render target is the “**screen buffer**” (the buffer shown to the screen), but not in this case
- 2<sup>nd</sup> pass: fill the final **screen buffer**
  - using the just-computed off-screen buffer as a 2D texture
  - the 1<sup>st</sup> pass was... “**rendering to texture**”
- Note: good for GPU because...
  - the off-screen buffer is either only write-only (1<sup>st</sup> pass) or read-only (2<sup>nd</sup> pass). Never both!
  - the off-screen buffer is constructed and used in GPU RAM. No expensive swap of memory between CPU and GPU!

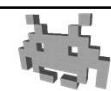
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## Example: metallic reflections of *dynamic* scenes



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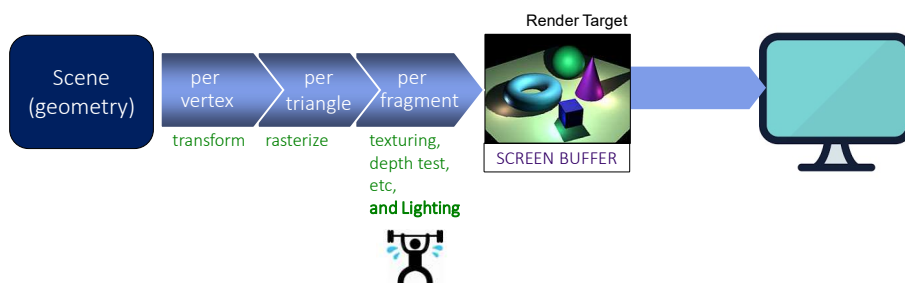
## Main rendering algorithms: two classes of approaches

- Forward rendering
- Deferred shading  
  - aka Deferred lighting (actually, a variation)
  - aka Deferred rendering (inappropriate?)
- Which approach to use?
  - Both are employed by games
  - Basilar choice! Implementation of all other rendering algorithms changes accordingly.

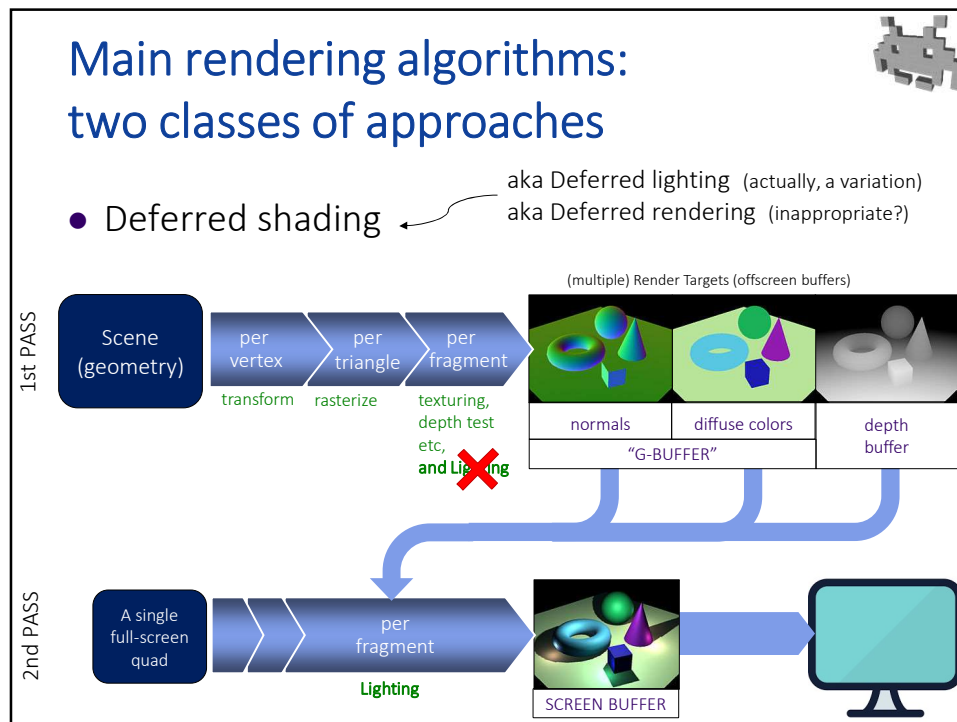
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## Main rendering algorithms: two classes of approaches

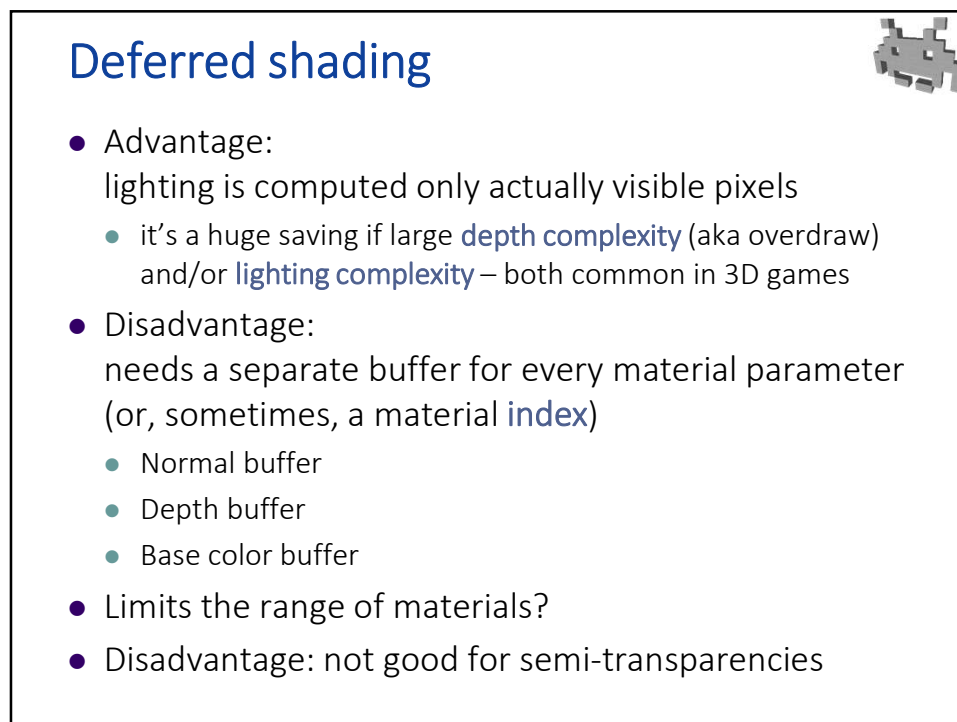
- Forward rendering



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