

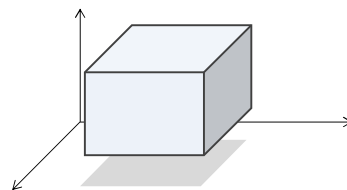
Course Plan

- lec. 1: **Introduction** ●
- lec. 2: **Mathematics** for 3D Games ●●●●●●●●
- lec. 3: **Scene Graph** ▶▶
- lec. 4: **Game 3D Physics** ▶●●●●● + ●📍
- lec. 5: **Game Particle Systems** ▶
- lec. 6: **Game 3D Models** ●●
- lec. 7: **Game Textures** ▶●●
- lec. 8: **Game Materials** ●
- lec. 9: **Game 3D Animations** ▶●●●
- lec. 10: **3D Audio** for 3D Games ●
- lec. 11: **Networking** for 3D Games ●
- lec. 12: **Interactive Agents** for 3D Games ●
- lec. 13: **Rendering Techniques** for 3D Games ●

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Geometry proxies: «AABB»

As the name implies,
typically used as **BOUNDING**
volume, not a collider

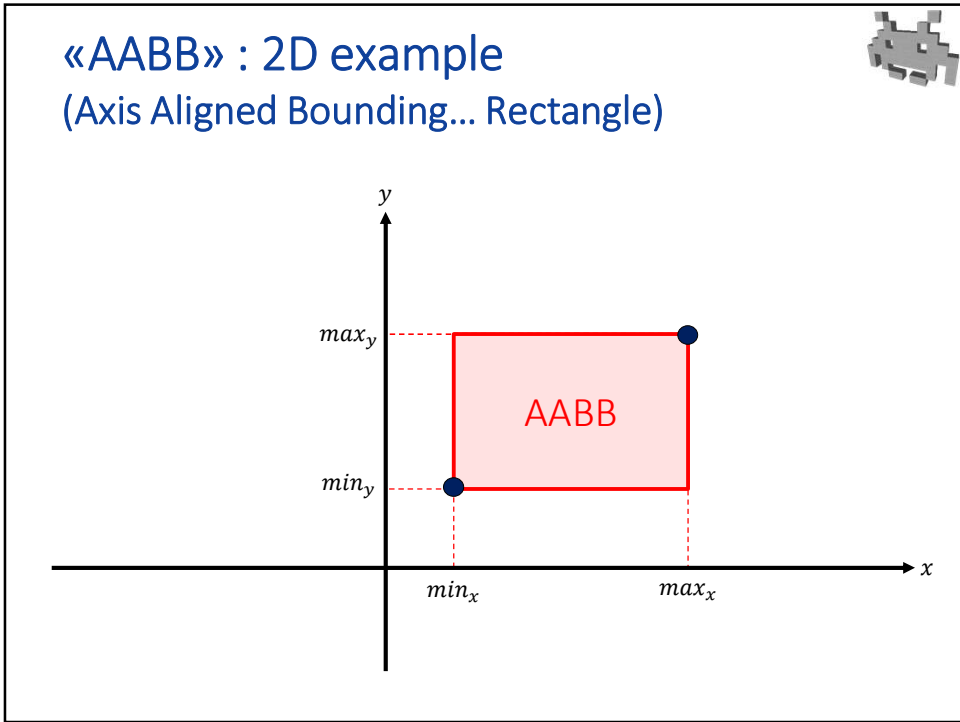


Axis Aligned Bounding Box

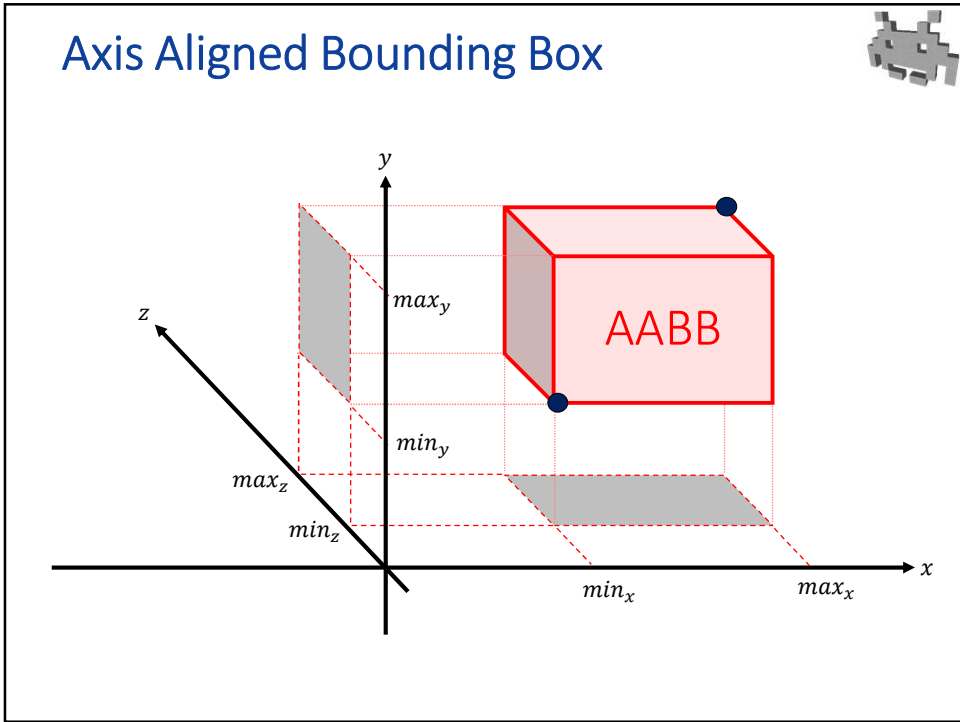
- Consists of three interval
 $[min_x, max_x] \times [min_y, max_y] \times [min_z, max_z]$
- Concise to store
 - Two 3D points: (min_x, min_y, min_z) & (max_x, max_y, max_z)
- Easy to find the minimal AABB encapsulating a given set of points
- Easy to test for collision VS a point, or another AABB
 - Exercise: how?
- Under transforms:
 - ☹️☹️☹️ if rotated, an AABB expands
 - (but can be easily scaled / translated)



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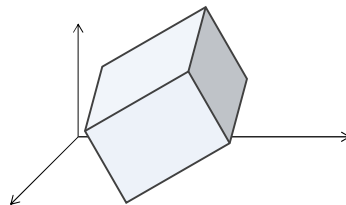


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Geometry proxies: Oriented Bounding Box (OBB)



- A “parallelepiped”
 - generalized version of AABB: it's not axis-aligned
 - storage:
 - a rotation (e.g. a quaternion) +
 - an AABB
 - Can be freely transformed
 - note: but only if scaling is uniform
 - Tests: still relatively easy (exercise: how to test points?)

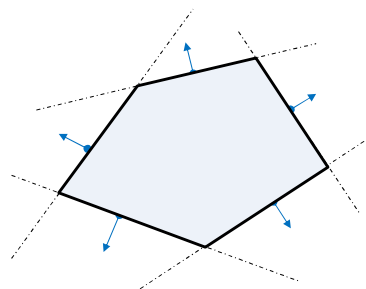


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Geometry proxies (in 2D): a Convex Polygon



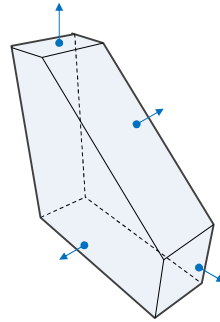
- Intersection of half-planes
 - each delimited by a line
- Stored as:
 - a collection of (oriented) lines
- Test:
 - a point is inside the proxy iff it is in each half-plane
- Flexible (good approximations)... and still moderate complexity



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Geometry proxies (in 3D): a Convex Polyhedron

- Intersection of half-spaces
- Same as previous, but in 3D
 - stored as a collection of oriented **planes**
 - each plane = a vec4 (normal, distance from origin)
 - tests: inside the proxy iff inside each half-space



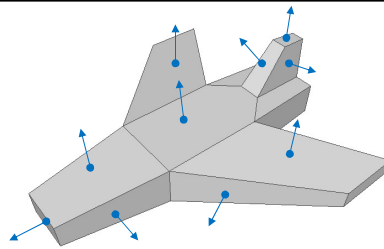
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Geometry proxies a (general) Polyhedron

↖ potentially **concave**

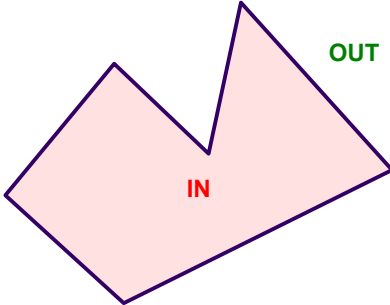
↖ not worth it for a **Bounding Volume** !

- A... luxury **Collider**
 - The most **accurate** approximations
 - But, the most **expensive** tests / storage
- Specific algorithms to test for collisions
 - requiring some preprocessing
 - and data structures (**BSP-trees**, see next)
- Creation (treat them as meshes):
 - sometimes, with automatic simplification
 - often, hand-designed by artists (low poly modelling)
- Wait, is this the same as a 3D mesh used for rendering?
 - Many differences (compare with mesh later, lecture 6)



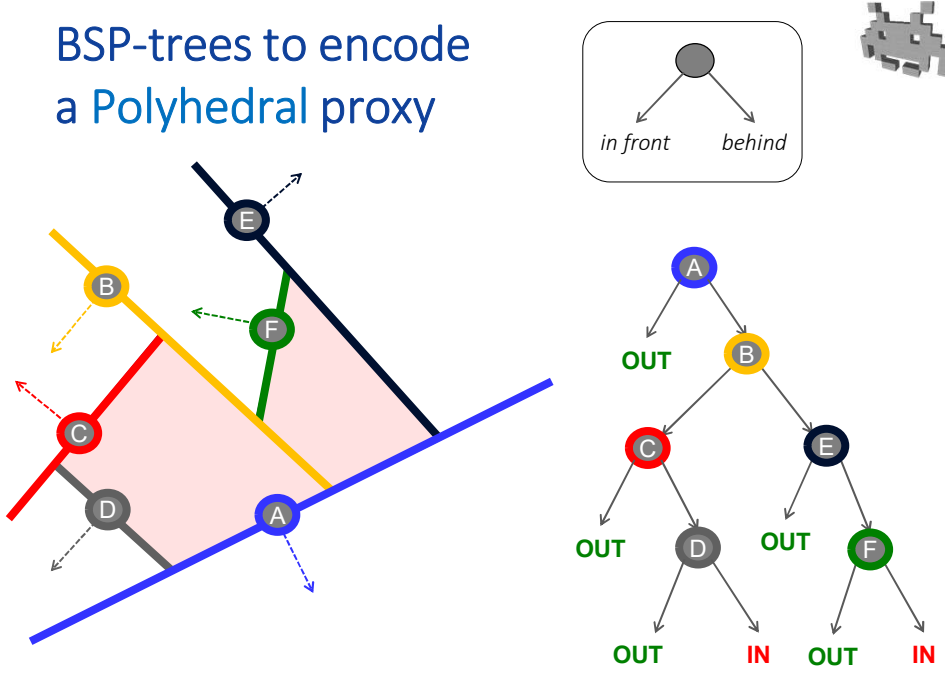
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BSP-trees to encode a Polyhedral proxy (Concave too)



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BSP-trees to encode a Polyhedral proxy



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BSP-tree (Binary Spatial Partitioning tree)



- A way to store a (convex, or concave) polyhedron
- A hierarchical structure
 - a binary tree
 - root = all space, child-nodes = partition of parent
 - each internal node is split by an *arbitrary* plane in 2D: a line
 - plane stored as (n_x, n_y, n_z, k)
 - each leaf stores one bit: "inside" or "outside" the proxy
 - tree is precomputed (and optimized) for a given polyhedron
 - to test a point = traverse the tree root-to-leaf

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3D meshes for geometry proxies vs 3D meshes for rendering (notes)



see lecture on 3D models later

- Proxy-meshes are
 - much *lower res* (e.g. $< 10^2$ faces)
 - no *attributes* of course (no uv-mapping, no color, etc)
 - made of *generic polygons*, not just *tris* (as long as they are *flat*)
 - always *closed*, *water-tight* (inside != outside)
 - very different internal representation:
 - a set of bounding planes (in a BSP tree probably)
 - in addition to collection of vertices (3D points)

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Collision detection on Polyhedral proxies: examples



- Point VS Polyhedron:
just follow the tree, end in an IN or OUT leaf
- Sphere VS Polyhedron: more complex (think about it)
- Segment / Ray VS Polyhedron: also complex (think about it)
- Polyhedron VS Polyhedron: much more complex.
A trace of an algorithm is:
 - Preprocessing: find and store all edges (segments) of all Polyhedra (each edge: two endpoints)
 - At testing time: test all edges of polyhedron A vs polyhedron B (segment VS polyhedron), and viceversa

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3D meshes for geometry proxies vs 3D meshes for rendering (notes)



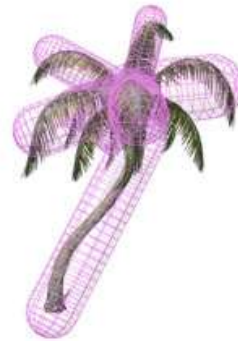
see lecture on 3D models later

- Proxy meshes are
 - much **lower res** (e.g. $< 10^2$ faces)
 - no **attributes** (no uv-mapping, no color, etc)
 - based **generic polygons**, not just **tris** (as long as they are *flat*)
 - **closed**, **water-tight** (inside != outside)
 - different internal representation:
 - if **convex** : a set of bounding planes
 - if **convex** : a BSP tree

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Geometry Proxies: Composite

- A proxy can be a union of sub-proxies
 - inside the proxy *iff* inside of *any* sub proxy
- Very expressive
 - better approximation for many objects, even with few proxies
 - note: union of **convex** proxies can be **concave** !
- Efficient to test / store
 - Compared to alternatives
- Difficult to construct automatically

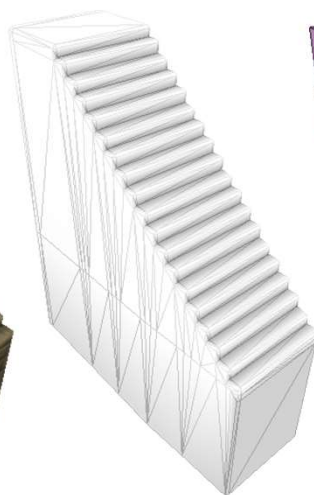


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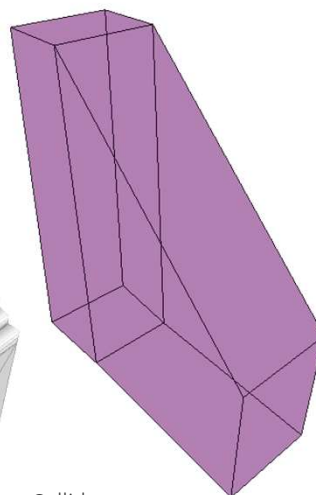
Collision Proxy examples



mesh for rendering
(~600 tri faces)

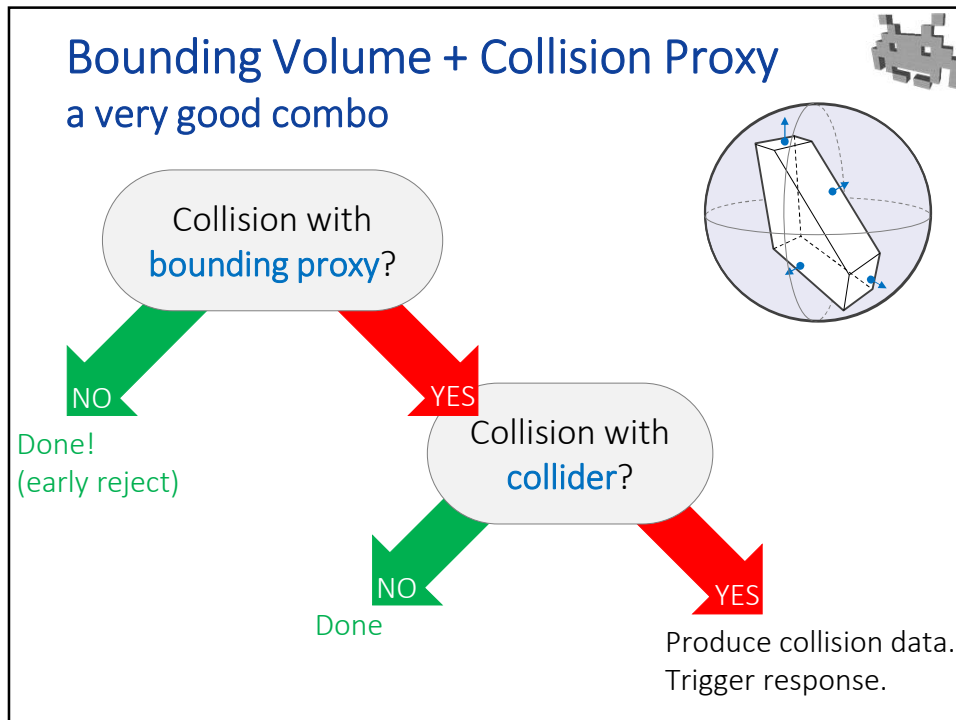


(in wireframe)



Collider:
10 (polygonal) faces

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Bounding Volume + Collision Proxy a very good combo


```
if (!intersect( boundingVol, X ) )  
{  
    // nothing to do: early reject!  
}  
else {  
    CollisionData d;  
    if (collide( hitBox, X , &d ))  
    {  
        collision_rensponse( d );  
    }  
}
```

note: **intersect** and **collide** aren't the same function here

a simpler **Bounding Volume** with, inside, a more complex **Collision Object** approximating the object

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How to construct a geometry proxy to be used as a collider?



“Given an object representation M , build a good **collision proxy** for it”

- M = 3D model of e.g. a dragon, a castle, a character...



difficult task to automatize (by algorithms)

- especially if we want to pick simpler (more efficient) proxies (such as compound of a few spheres, capsules, boxes)
- especially if we need good approximations



often done manually (by digital artists)

Geometry proxies for colliders are assets !

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How to construct a geometry proxy to be used as a bounding volume?



“Given an object representation M , build a tight **bounding volume** for it”

- a M = 3D model of e.g. a dragon, a castle, a character...



This task can be (and is) automatized

- note: finding the optimal (smallest possible) bounding volume: computationally difficult (**can be NP complete**)
- find a “good enough” bounding volume: a lot easier (**heuristics**)
- can be done on the fly during game execution
- For example, think about algorithms to find a bounding volumes of type...
 - AABB (trivial!)
 - Sphere – i.e. a “bounding sphere” (less trivial)
 - Capsule, OBB (more difficult!)

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Digression: collision detection in traditional 2D sprite-based games



- An easier problem
- We can leverage **collision detection for 2D sprites**
 - *it's accurate*: «**pixel perfect**»
 - *it's efficient*: **HW supported**
(hard-wired support, as part of sprite rendering)
 - little need for **proxy** approximations for colliders
(same structure – the sprite – both for collision and for rendering)
 - easy bounding “volume”: axis-aligned bounding-rectangle of the sprite

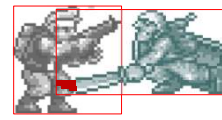
in screen space



NO COLLISION



NO COLLISION



COLLISION

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Collision detection



- Efficiency issues:
 - a) test between object pairs:
 - Must be efficient
 - b) avoid quadratic explosions of needed tests
 - n objects $\rightarrow n^2$ tests ?

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Collision detection: the broad phase

- So far, we have seen how to detect a collision between one given pair of objects
- Problem: we don't want to test every pair of objects!
 - Even excluding static-static pairs: still way too many (quadratic)
- Idea: in a «**broad phase**», we quickly identify pairs of objects that need testing
 - Objects that are safely far from each other are never even tested
 - Only objects that are... “suspiciously close” must be tested
- Note: the broad phase must be *strictly conservative*
 - **not ok** to discard object pairs that actually collided,
 - **ok** to test objects that *didn't* actually collide
- Let's see strategies to do so

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The «broad-phase» of coll. detection (avoiding quadratic explosion of # of tests)

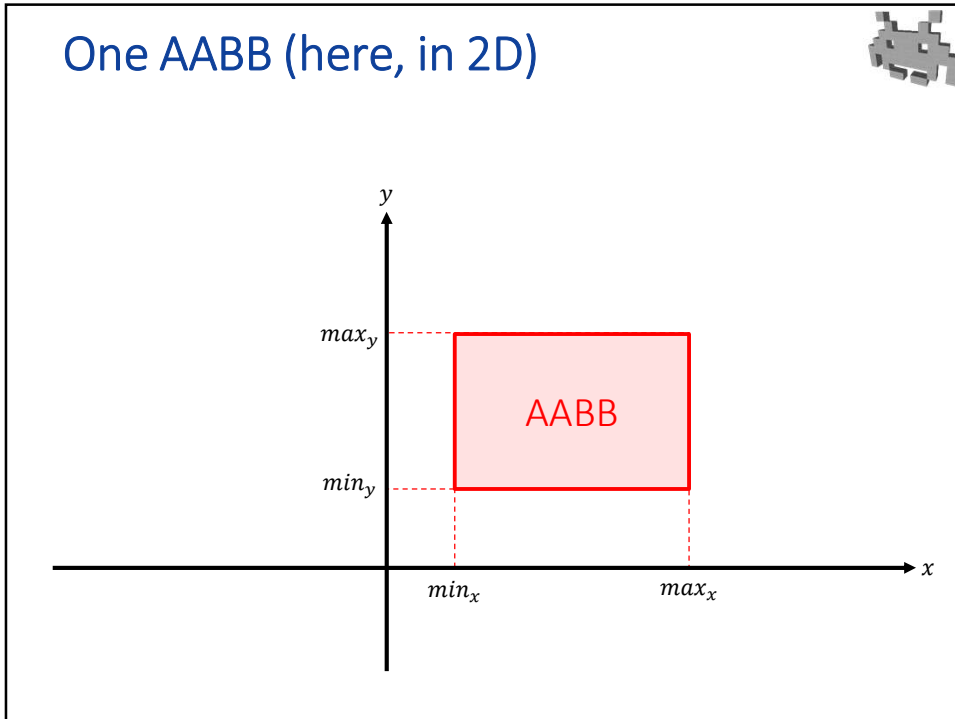
- Classes of solutions:

1) Sorting-based algorithms

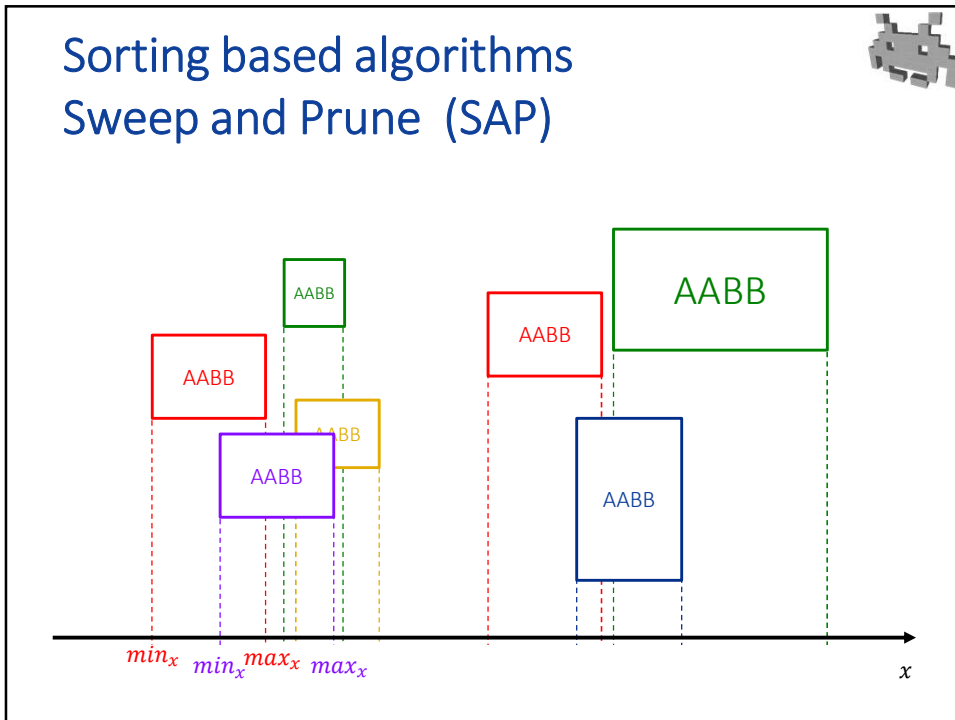
2) **spatial indexing** structures

3) BVH – Bounding Volume Hierarchies

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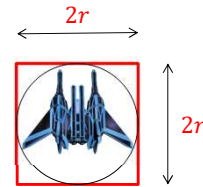


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Sweep And Prune (SAP) strategy (aka "Sort and Sweep")

1. Bound:

- Quickly find the AABB for each collider (in its current rotation + translation)
- E.g.: use the AABB encapsulating the transformed Bounding Sphere



2. Sort min_x and max_x of all AABB together

- just adjust the sorting used in the previous frame
- it will be already *almost sorted*! To exploit this...
- use an *incremental* sorting algorithm, like bubblesort

only
 $O(n \log n)$

3. Sweep the sorted intersections, from smaller to larger

- Quickly detect intersecting intervals in x (how?)

Even
faster
on
almost
sorted
lists!
 $O(n)$

4. Prune: among AABB intervals, ignore the ones that don't *also* intersect in both y and z

- Test the pairs that do

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The «broad-phase» of coll. detection (avoiding quadratic explosion of # of tests)

Classes of solutions:

1) Sorting-based algorithms

2) spatial indexing structures

Not covered
here

3) BVH – Bounding Volume Hierarchies

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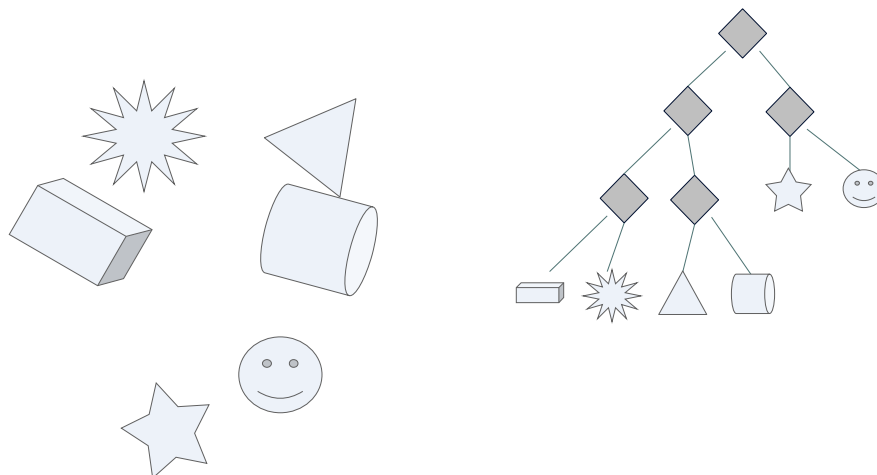
The «broad-phase» of coll. detection (avoiding quadratic explosion of # of tests)



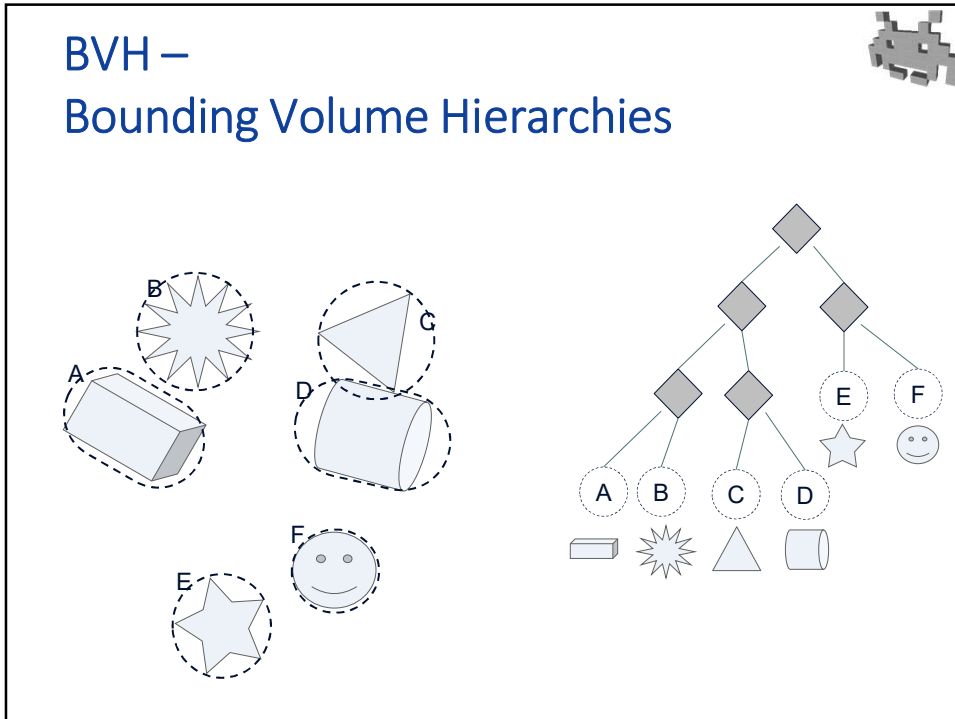
- Classes of solutions:
 - 1) Sorting-based algorithms
 - 2) *spatial indexing* structures
 - 3) BVH – Bounding Volume Hierarchies

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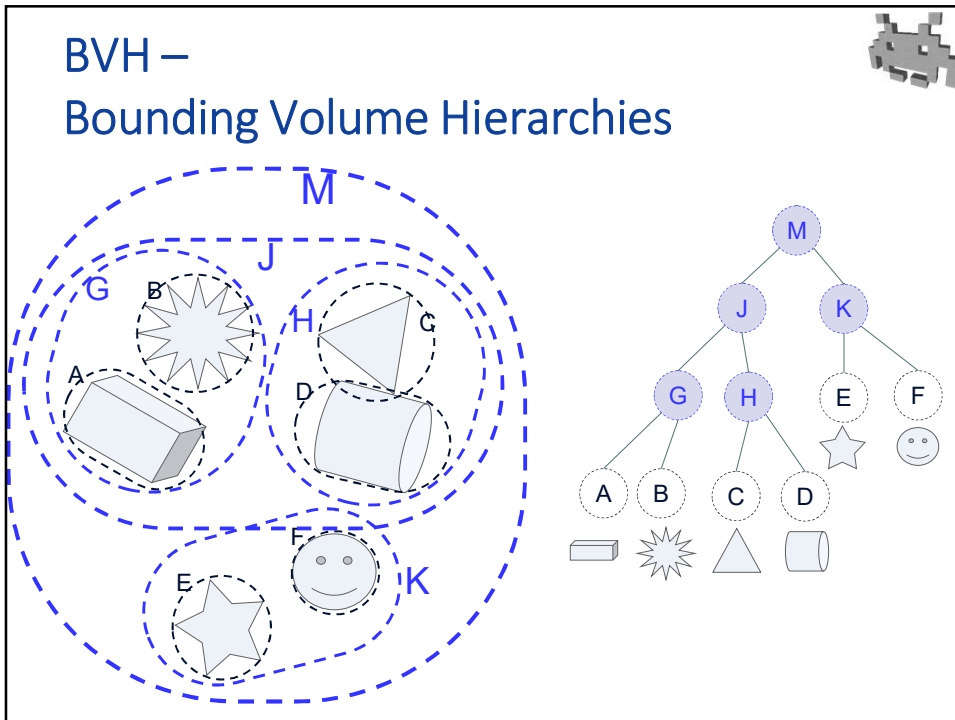
BVH Bounding Volume Hierarchy



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BVH

Bounding Volume Hierarchy

- We can use the hierarchy already defined by the scene graph
 - instead of a spatially derived one
- associate a Bounding Volumes to each node
 - rule: a BV of a node bounds all objects in the subtree
- construction / update: quick! 😊
 - bottom-up
- using it:
 - top-down: visit (how?)
 - *note*: it's **not** a single root to leaf path
 - may need to follow *multiple* children of a node (in a BSP-tree: only one)

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Collision Detection: to learn more...



Christer Ericson (ACTIVISION):
Real-Time Collision Detection
The Morgan Kaufmann Series in
Interactive 3-D Technology
HAR/CDR Edition
Elsevier

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Physics Engine: implementation issues for GPU



- Task: **Dynamics**
 - (forces, speed and position updates...)
 - simple structures, fixed workflow
 - highly parallelizable: **GPU** implementation easy
 - but: GPU can be non-fully deterministic (different cards, different vendors: different results)
- Task: **Constraints Enforcement**
 - still moderately simple structures, fixed workflow
 - problem: collision constraints not known a-priori: **GPU** more difficult
- Task: **Collisions Detection**
 - non-trivial data structures, hierarchies, recursive algorithms, sorting...
 - hugely variable workflow
 - e.g.: quick on no-collision, more work to do when the rare collisions occur
 - difficult to parallelize: **CPU**
 - but the outcome affects the other two tasks (e.g., creates constraints)
 - ==> **CPU-GPU** communication, and ==> **GPU** structures updates (problematic on many architectures)

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End of Game Physics. To gather more info...



- Erwin Coumans
SIGGRAPH 2015 course
<http://bulletphysics.org/wordpress/?p=432>
- Müller-Fischer et al.
Real-time physics
(Siggraph course notes, 2008)
<http://www.matthiasmueller.info/realtimephysics/>
- David H. Eberly:
Game Physics (2nd Edition)
MK Press
- Ian Millington:
Game Physics Engine Development (2nd Edition)
MK Press

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