



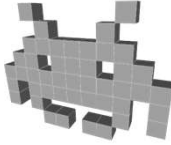
Course Plan



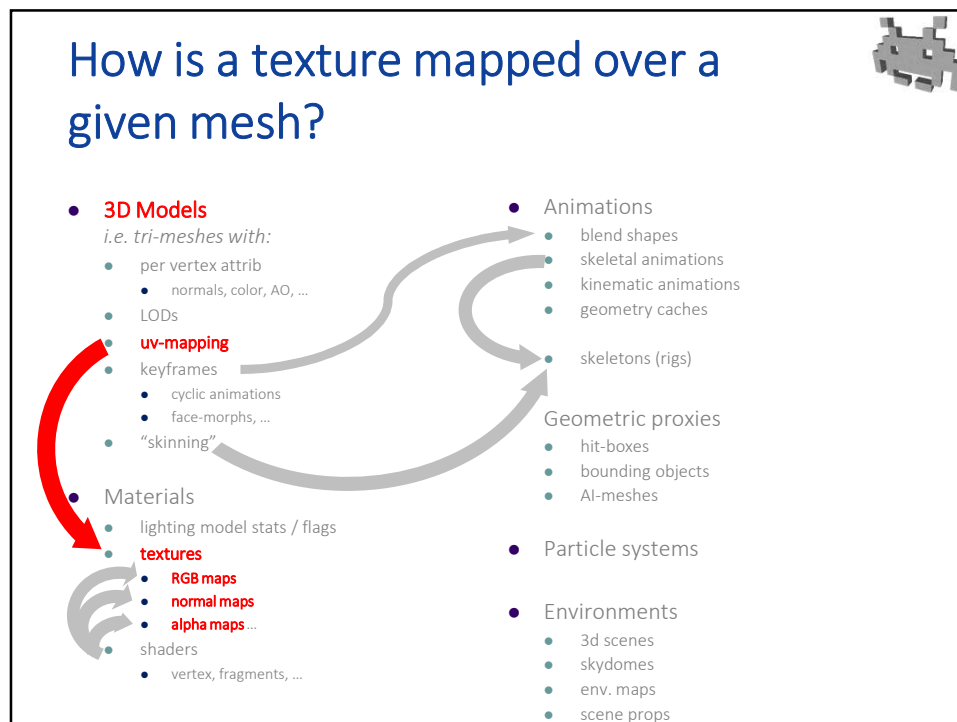
- lec. 1: **Introduction** ●
- lec. 2: **Mathematics** for 3D Games ●●●●●
- lec. 3: **Scene Graph** ●
- lec. 4: **Game 3D Physics** ●●● + ●●●
- lec. 5: **Game Particle Systems** ▸
- lec. 6: **Game 3D Models** ●●
- lec. 7: **Game Textures** ▸ ● 
- lec. 8: **Game 3D Animations** ●●●
- lec. 9: **Game 3D Audio** ●
- lec. 10: **Networking** for 3D Games ●
- lec. 11: **Artificial Intelligence** for 3D Games ●
- lec. 12: **Game 3D Rendering Techniques** ●●

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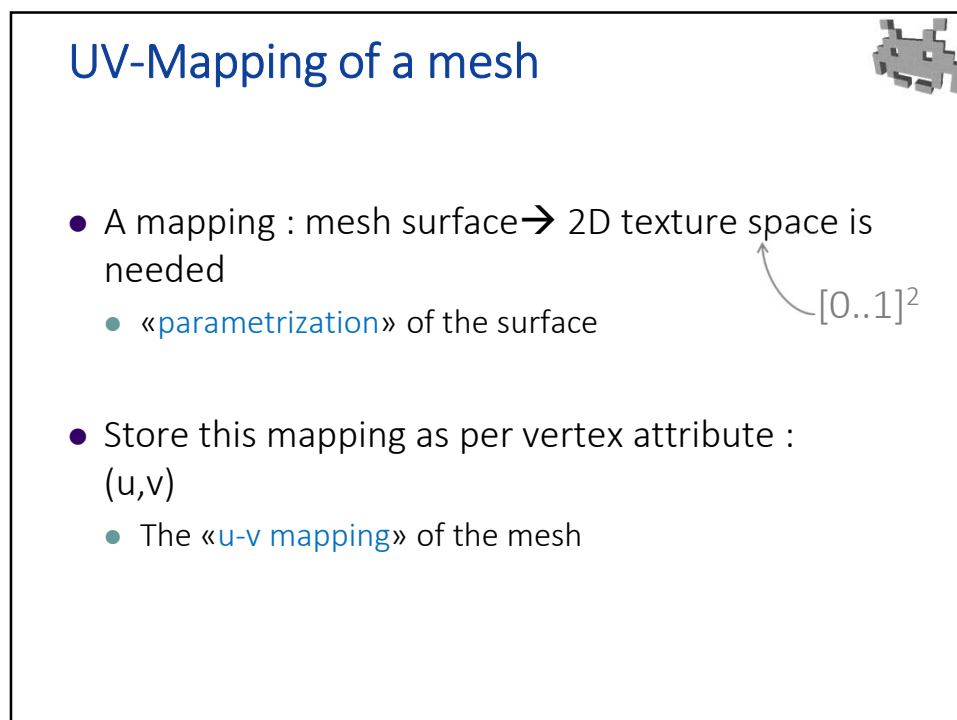
How is a texture mapped over a given mesh?



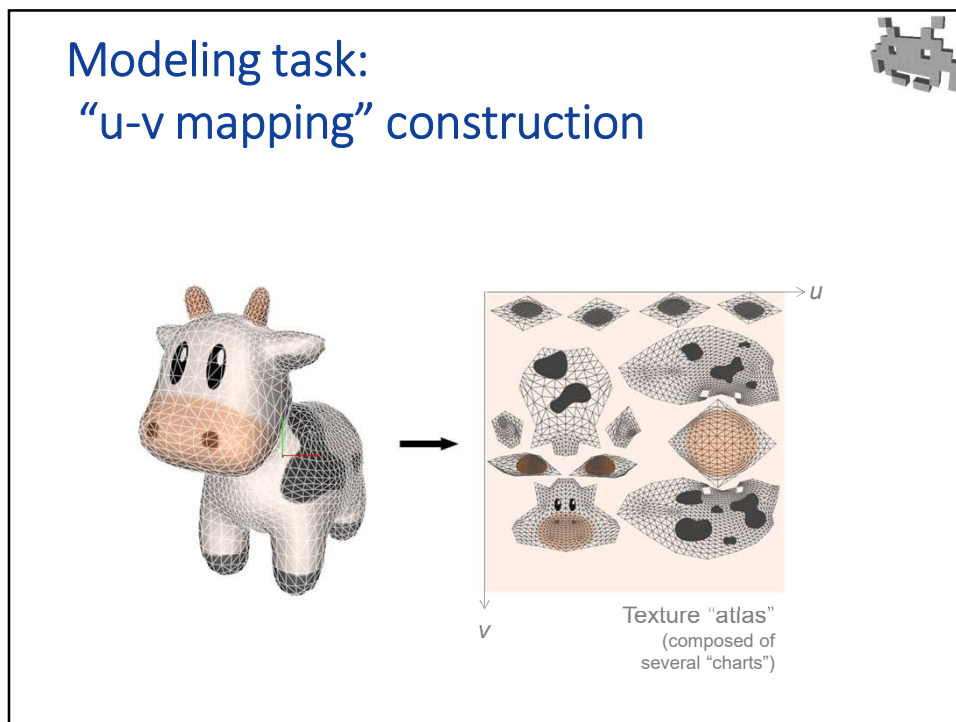
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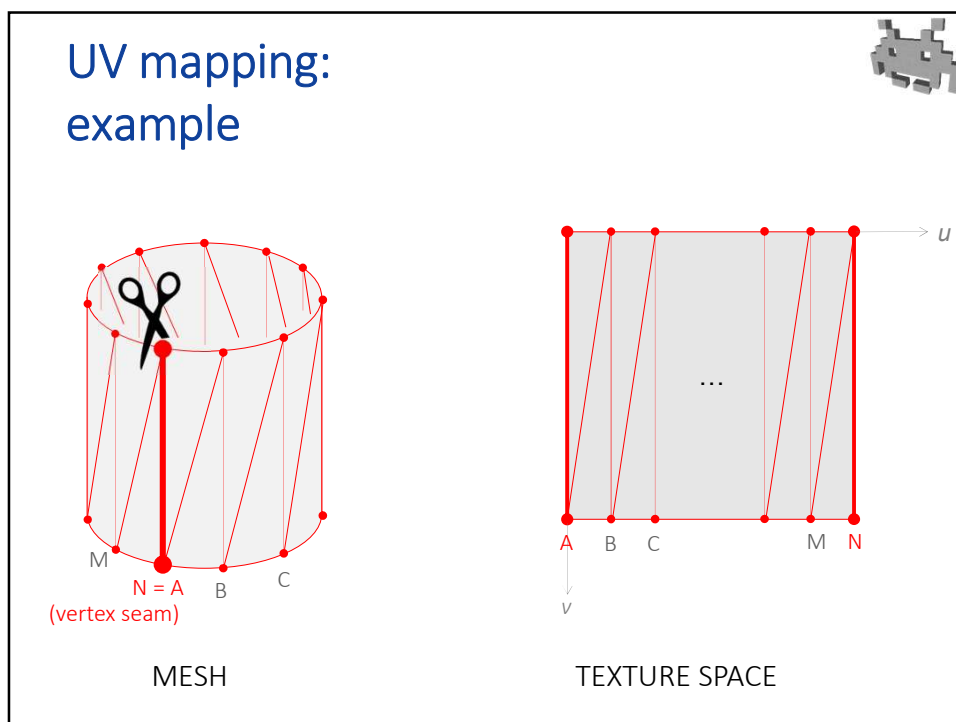
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Texture seams (or cut)

- A vertex seam necessary to encode the UV-map

	X	Y	Z	U	V	...
V0	p_x0	p_y0	p_z0	$u0$	$v0$...
V1	p_x1	p_y1	p_z1	$u1$	$v1$...
V2	p_x2	p_y2	p_z2	$u2$	$v2$...
V3	p_x2	p_y2	p_z2	$u3$	$v3$...
V4	p_x3	p_y3	p_z3	$u4$	$v4$...
V5	p_x3	p_y3	p_z3	$u5$	$v5$...
V6	p_x4	p_y4	p_z4	$u6$	$v6$...

GEOMETRY + ATTRIBUTES

Tri:	Wedge 1:	Wedge 2:	Wedge 3:
T0	0	1	4
T1	4	2	0
T2	5	3	6

CONNECTIVITY

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Texture space notation

Texture Space (or "parametric space" or "u-v space")

Texture Space = $[0,1] \times [0,1]$

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Note: Texture space independent from texture resolution (or aspect ratio)



1024x512

128x64

Convenient!
We can reduce texture sheets res (balancing quality / memory) without affecting the mesh 'UV mapping.

Eg: load in GPU RAM only a few smaller MIP-map levels

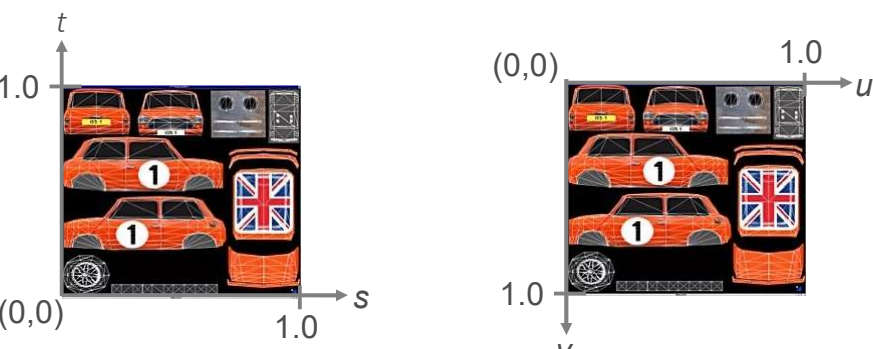
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Two notations

Most used (in game industry)

s-t
(es OpenGL)

u-v
(es DirectX)



(0,0)

1.0

1.0

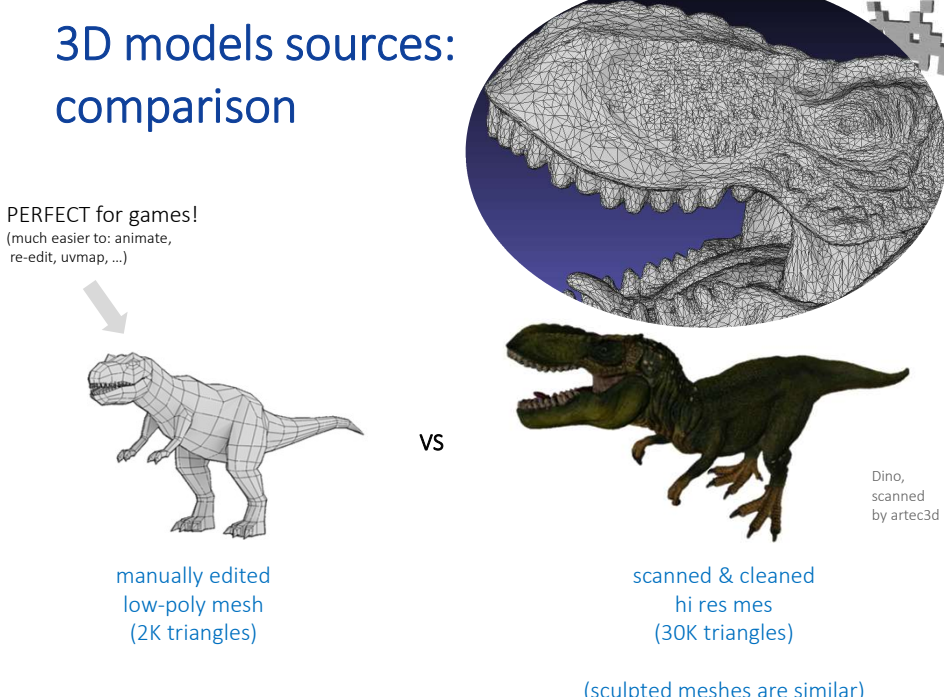
(0,0)

1.0

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3D models sources: comparison

PERFECT for games!
(much easier to: animate,
re-edit, uvmap, ...)



manually edited
low-poly mesh
(2K triangles)

vs

scanned & cleaned
hi res mes
(30K triangles)

Dino,
scanned
by artec3d

(sculpted meshes are similar)

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Construction of a UV-map for a mesh (or, UV-mapping of a mesh)

- Typical task of the modeler (digital artists)
 - (semi-)automatic algorithms very studied
- We need to find a spot in the (2D) texture space for each (3D) mesh triangle
- Similar to to:
 - Peel an apple (cutting part)
 - Lay each produced peel in 2D (unfolding part)
 - Pack the peels inside a rectangular space (packing part)
- Cuts (or “texture seams”) are (almost) always required!
 - they are discontinuity of u,v attributes
 - stored in the mesh as vertex-seams (vertex duplications)

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Modeling task: “u-v mapping”



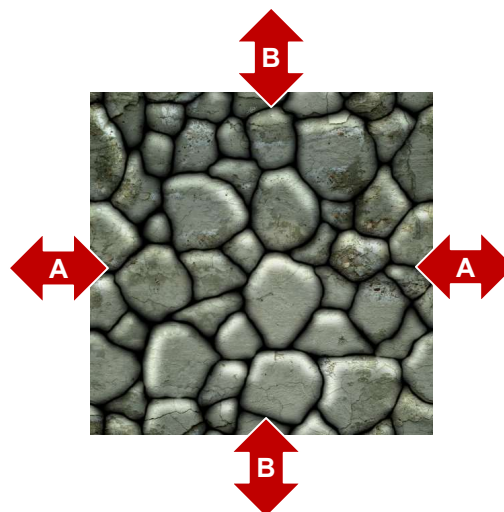
- Strategies:

- 1. select of the cutting edge
...or...
1. assign faces to texture “charts”
 - either way, decide where “texture seams” are
- 2. unfolding
 - minimizing “distortion” (by automatic algorithms)
- 3. charts packing (again, often automatized)
 - Minimize the empty space in textures
 - Assign areas according to necessities
(important parts → bigger texture space)
(sampling of the texels becomes [adaptive!](#))

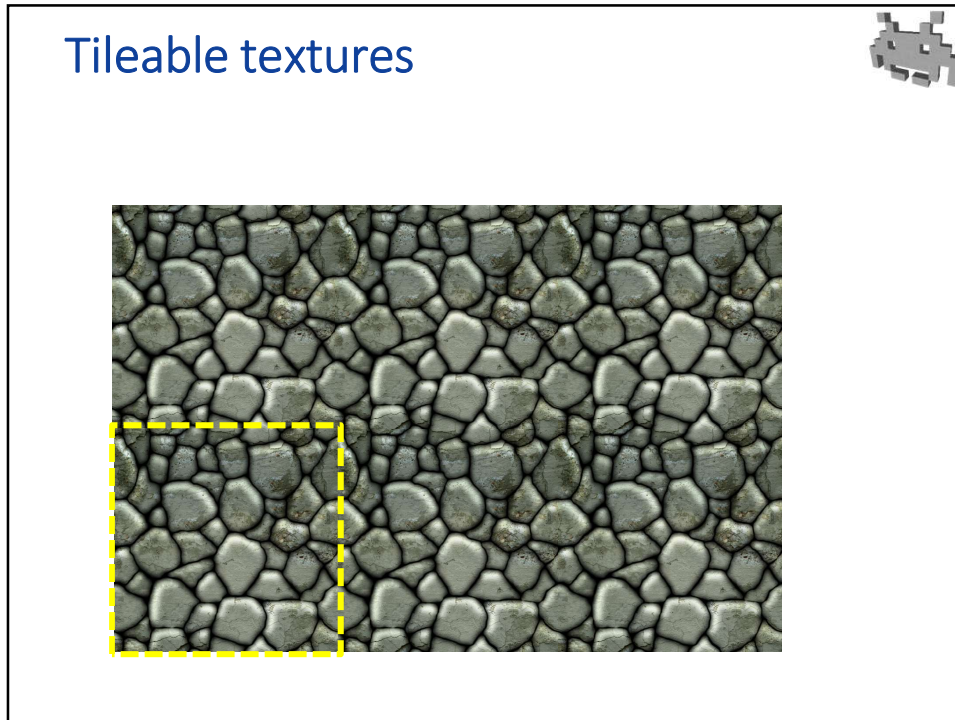
DEMO!

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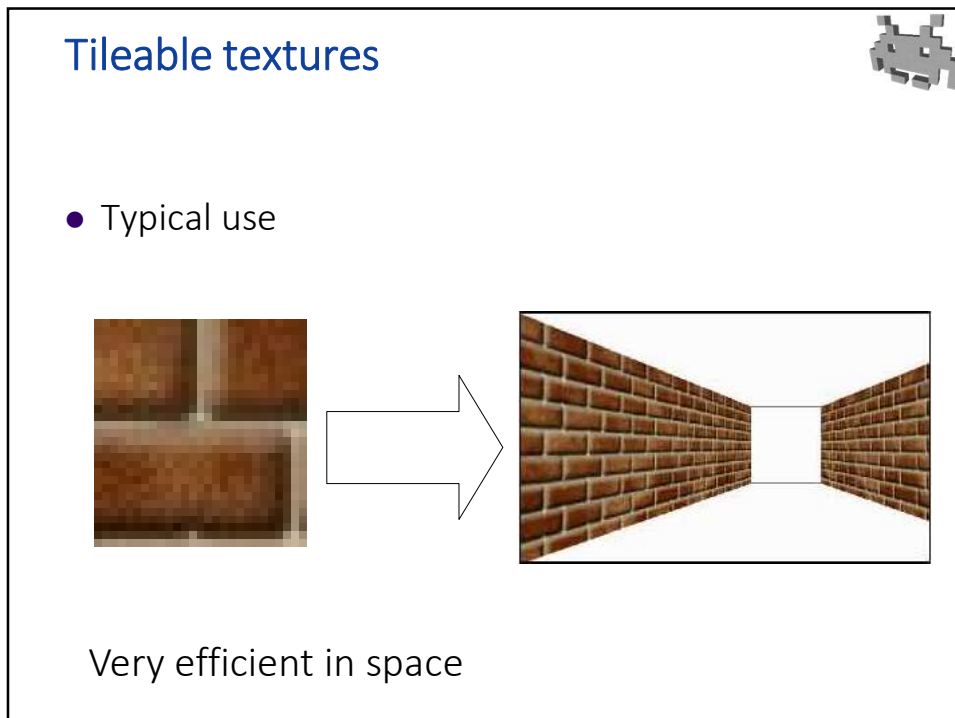
Tileable Textures



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Two types of UV-maps



- **NOT injective** UV mapping
 - Different zones of the mesh mapped to the same texture region
 - e.g.: with overlapping charts
 - ☺ Optimization of texture RAM
 - Can exploit of simmetries / repetitions
- **Injective** UV mapping
 - 1 (non empty) point on the texture = 1 point on the mesh
 - non-overlapping charts!
 - ☺ Generality / Flexibility
 - Used for several scopes (e.g. light baking)
- Different objectives
 - often, both are present: 2 distinct UV maps
 - 2 distinct UV attributes for each vertex


aka: **"UV-map"** (the standard)

aka: **"Unwrapping"**
 or: **"Unwrapped UVs"**
 or: **"1:1 UV-map"**
 or: **"Lightmap"** UV-map
 or: **"Non-overlapping"** UV-map


Which is the type of the UV-maps shown in prev slides?

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RGB maps: How are they obtained?




- Image *first, then* UV-mapping
 - e.g. images from photos
 - e.g. tileable images
- UV-mapping *first, then* paint 2D
 - paint with 2D app (e.g. photoshop)
- UV-mapping *first, then* paint 3D
 - paint within 3D modelling software,
 - or: 1. export 2D rendering,
 2. paint over with e.g. photoshop,
 3. reimport images
 4. goto 1




UV-mapper



2D painter



UV-mapper



3D painter

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RGB maps: How are they obtained?

...or:

- *first* paint 3D
 - on hi-res model,
 - “paint” on vertex attributes
 - e.g. with Z brush...
- *then* coarsen
 - build / autobuild final low-poly version
- *then* UV-map
 - the low-poly model
 - must be a 1:1 mapping!
- *then* auto-texture
 - auto build texture

*more
about
this later...*

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Cutout textures example Texels = transparency level (0 or 1)

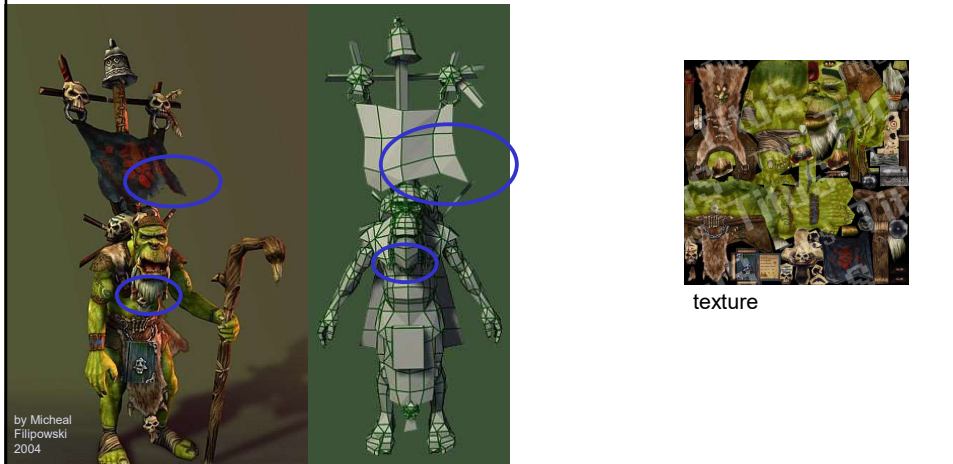


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Cutout textures

Texels = transparency level (0 or 1)

- e.g.: drapes, beard...

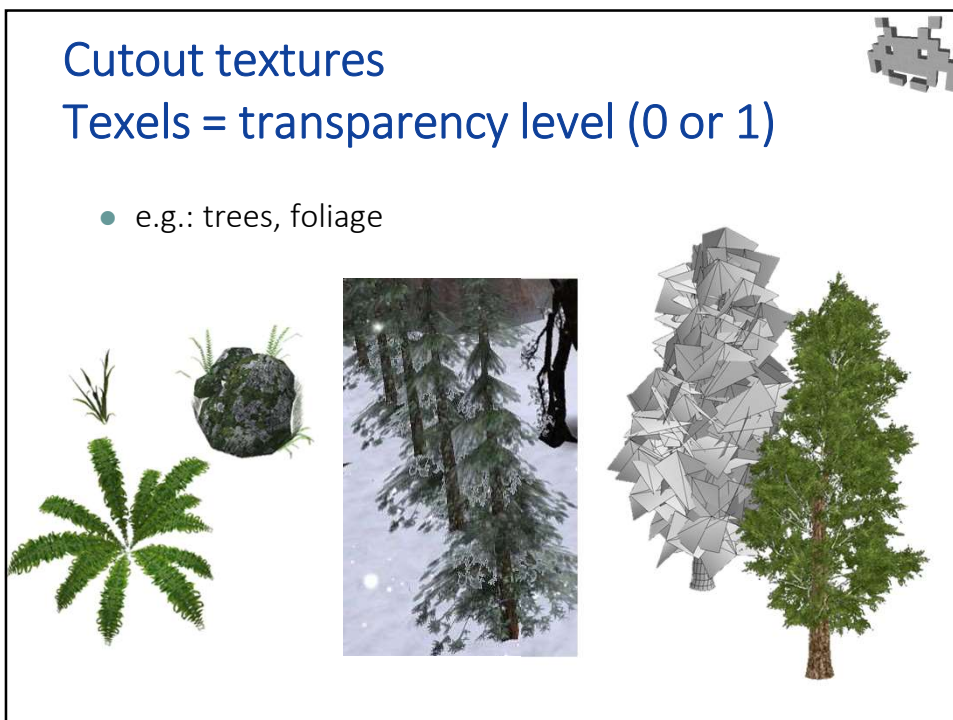


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Cutout textures

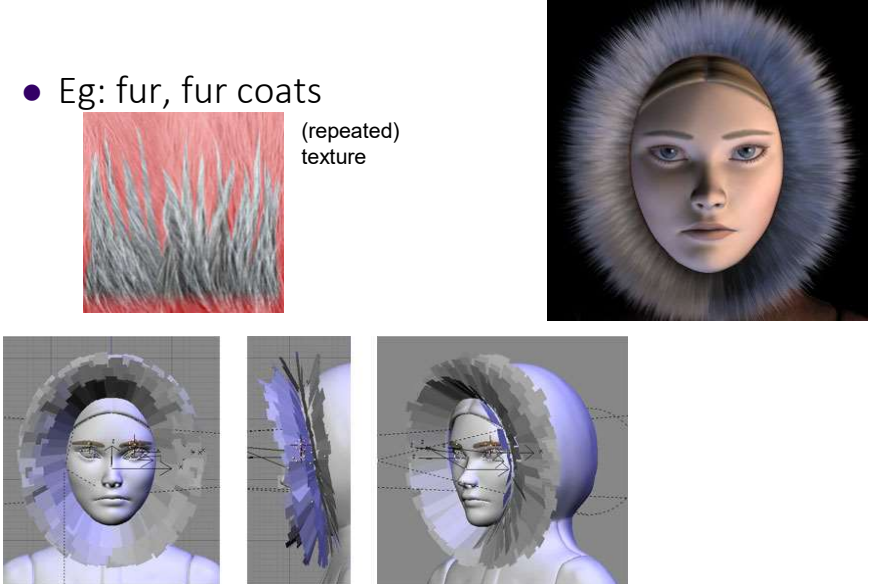
Texels = transparency level (0 or 1)

- e.g.: trees, foliage



Texture mapping and Alpha Test

- Eg: fur, fur coats



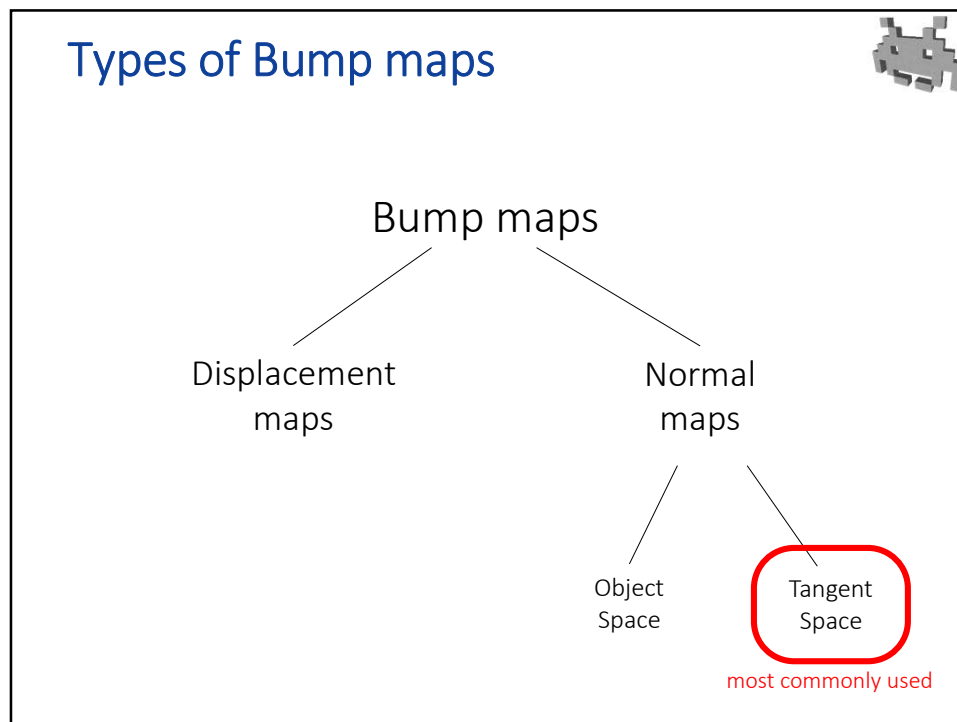
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Bump-Map (*)

- a **texture** modelling (or, providing an illusion of **shape details** (i.e., high-frequency geometric features))
 - details not modeled by the “real” geometry (the mesh)
 - remember: meshes tend to be low-poly
 - not much detail in them
 - approach also known as “**Texture-for-Geometry**”
 - rationale: texels are cheaper to render/store than vertices!
 - geometric details may extrude **out** or be engraved **in** the “real” (mesh) surface
 - in many cases: the detail affects lighting only
 - sufficient to trick the eye
 - especially true with dynamic lighting

(*) This terminology not universal: «Bump-map» can mean just «displacement map»

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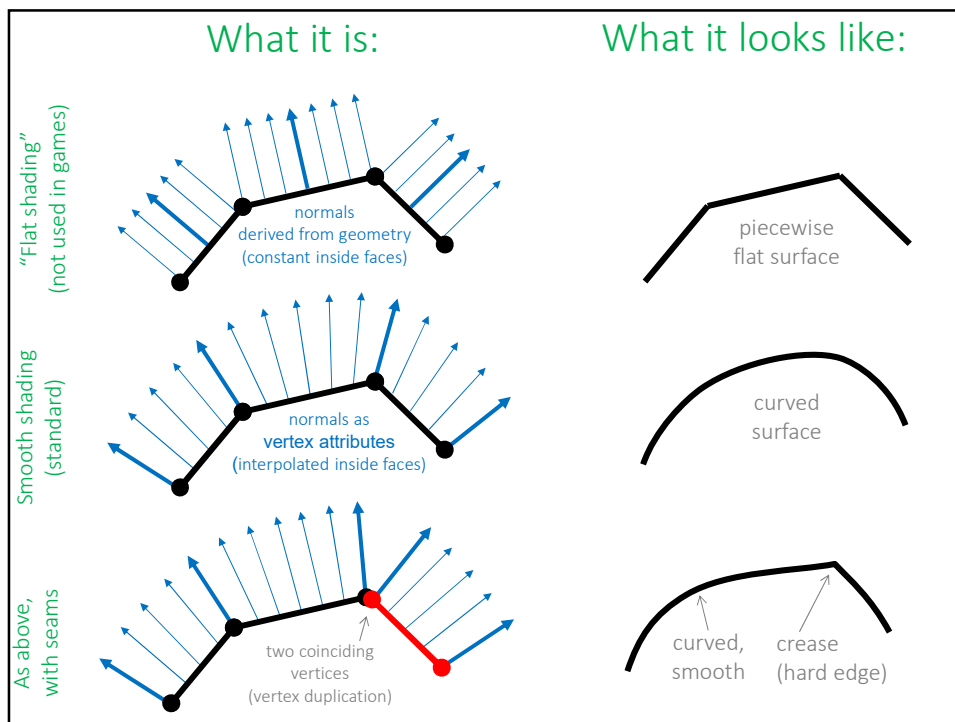


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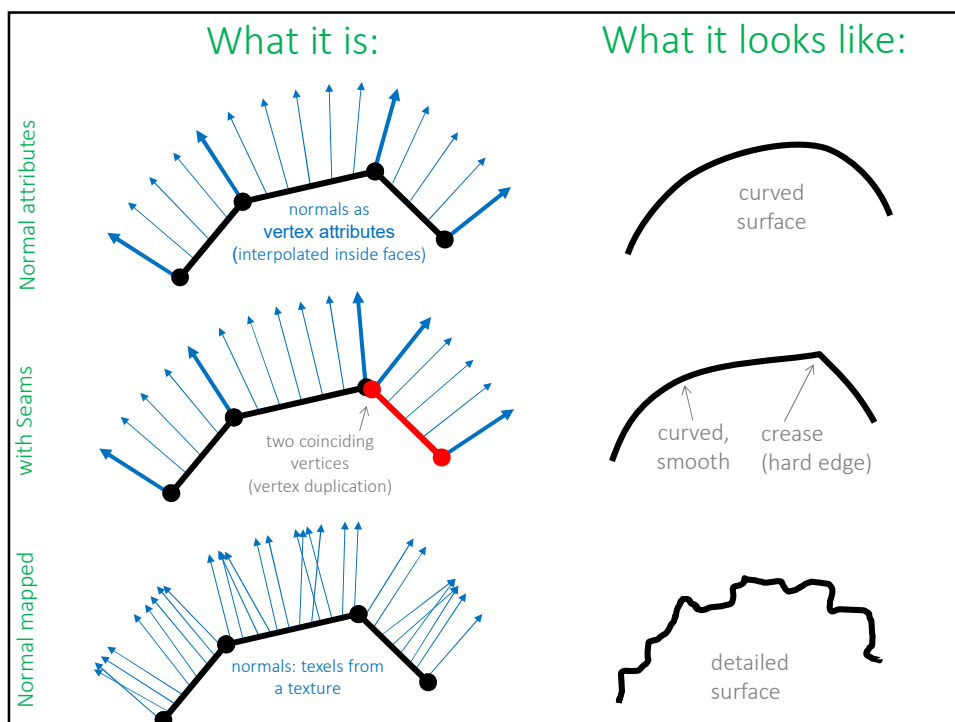
Types of Bump maps

- **Bump map:**
 - A texture encoding hi-frequency details
- **Displacement Map:**
 - Details are encoded by storing differences between mesh geometry and detailed surface:
 - as **scalars** (distance along the normal), or as **vectors**
 - used for: on-the-fly re-tessellation, and *parallax mapping* technique
- **Normal Map:**
 - Details are encoded by storing the normals of the detailed surface
 - used for: affecting the lighting
 - In which frame?
 - In **Object Space**: (Only for 1:1 UV-mapping)
 - In **Tangent Space**: (TBN space)
 - Usable on more surfaces independently from the orientation
 - Requires Tangent-Bitangent direction and normals on surface

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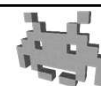
Bump-Map: from the modeler perspective



- **macro-structure** of the object → **low-poly mesh**
 - e.g.: the general shape of the horse
 - e.g.: the general shape of the face
 - e.g.: the general shape of the dragon
- **meso-structure** of the object → **bump-map**
 - e.g.: the musculature of the horse
 - e.g.: the wrinkles of the face
 - e.g.: the flakes of the dragon
- **micro-structure** of the object → **material parameters**
 - e.g.: the velvet-like fur of the horse
 - e.g.: the structure of the dermis / sebum
 - e.g.: the micro roughness / smoothnes of the flakes

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Displacement map : concept

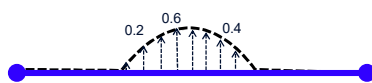


Stores the **distance** of the detailed surfaces
 from the plain geometry

- example: a bump-map for a screw-head



Detailed surfaces
 (which I would like to repress)



low-poly mesh
 (my approximation) (here: flat ☹)

0 0 0 0 0 0 0 0 1.5 6.6 7.5 4.2 0 0 0 0 0 0

displacement map
 (scalars)

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Displacement map: notes

- Each texel stores: a **distance** of the detailed surface
 - Along the **normal** direction (of low-poly mesh)
 - 1 **scalar** per texel → 1 channel texture
- Which way:
 - outwards (*extrusions*)
 - inwards (*excavations*)
 - or both (signed displacements)
- Storage:
 - **gray-scale** image (1 scalar per pixel)
 - remap values within the interval [0..1]
 - global scale factor (on the fly)
- Possible uses:
 - Direct lighting of implied normals: “embossing” effect (old effect: it’s a bad approximation, not common anymore)
 - Global illumination (ambient occlusion) See later
 - «Parallax mapping» technique See later
 - Intermediate data for the construction of a normal map See later



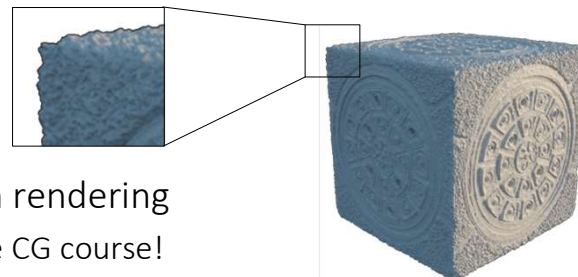
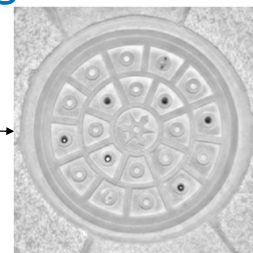
white = outwards
black = flat

Easy to paint and
manipulate!

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(scalar) Displacement map: Rendering – parallax mapping

- Technique used render a mesh with a Displacement Map
 - Bonus: the silhouette of the object can be affected




- See lecture on rendering
 - And Real time CG course!

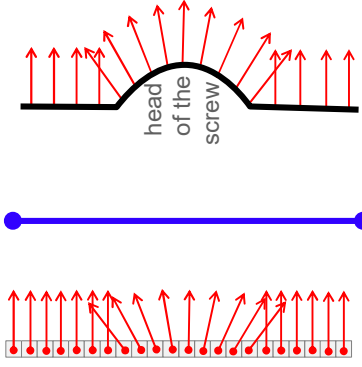
Image courtesy of <https://cgcookie.com/articles/normal-vs-displacement-mapping-why-games-use-normal>

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Normal Map: concept

Store the **Normals** of the detailed surfaces



- example -- a normal-map for a screw-head 



Detailed surface
(I would like to model)

low-poly mesh
(approximation of ^) (here: flat ☹)



normal map
(one normal per texel)



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Normal Map: notes

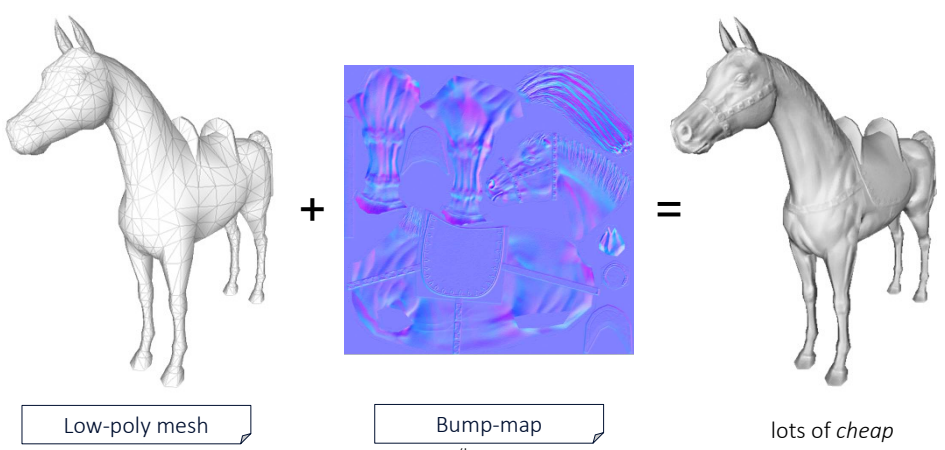
- Affects the lighting only
 - **not** the parallax
 - **not** the shape of the object
 - The lighting reflects the hi-freq detail of the object
 - dynamically (with variable lights!)
 - Total illusion: very convenient
 - If we are not trying to model a macro-structure
- In rendering: use the normal from the texture
 - (for lighting)
 - Instead of the interpolated per vertex normal
- Normals are expressed in cartesian coord
 - Often
 - But not always (\exists better ways to express unit vectors!)
 - Question: ok, but in which space???



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Normal-Mapping

see demo! 



Low-poly mesh
(uv-mapped!)


Bump-map
(here: a
tangent space normal map)

lots of *cheap*
geometric detail
(apparently)

assets courtesy of "Mount&Blade" (Talesworlds)

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Normal Maps: in which space are the normals encoded?



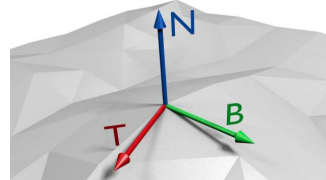
- Object space: **Object-Space Normal-Maps**
(The same in which I express the vertex pos)
 - ☺ the per-vertex normal becomes unnecessary!
 - The normal from texture substitute it
 - ☺ Trivial to apply (during rendering)
 - just use the normal fetched from the texture for lighting
 - ☹ normal-map is bound to a specific object
 - cannot be reused for different objects
 - ☹ Each region of the normal map is bounded to one specific area region of the object!
 - Injective UV-maps only!
 - e.g. no tiling, no exploitation of simmetries

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Tangent space (aka TBN space)

- A vector space defined \forall point of the surface:

- Z axis: **Normal**
 - orthogonal to surface
- X and Y axis: tangent vectors
 - parallel to the surface
 - X = **Tangent**
 - Y = "**Bi-Tangent**"
(sometimes, but inappropriately: *Bi-Normal)

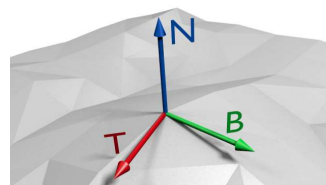


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Tangent space (aka TBN space)

- How to store them?

- As 3 vectors stored as (per-vertex) **attributes**
 - So, they are interpolated inside faces (like any other attribute)
- Optimizations are possible!
 - Not necessarily stored as 3 vectors (9 scalars)
 - E.g.: instead of storing B, we store N and T, then $B = N \times T$
- Note: they have discontinuities
 - seams (vertex duplications) are necessary
 - In first approximation, the same ones required by the UV-map (but non only! why?)

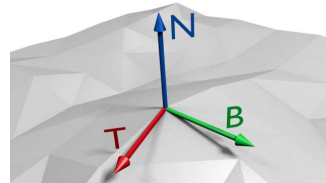


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Tangent space (aka TBN space)



- How to compute them?
 - Normal
 - as usual (see lecture on mesh)
 - Tangent & Bi-Tangent
 - determined by the UV-map!
 - T = gradient of U coordinate
 - B = gradient of V coordinate



- details:
 - All three are defined and constant inside faces, then averaged at vertices (see per-vertex normal computation)
 - T,B,N can be *only approximatively* orthogonal to each other
 - T,B,N reference frame can be left-handed or right-handed (even different “handedness” in different parts of the same mesh)

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Normal Maps: in which space are the normals encoded?



- Tangent space: Tangent Space Normal-Maps (the standard «bump-map», in games)

- ☹️ extra attributes are now needed per vertex:

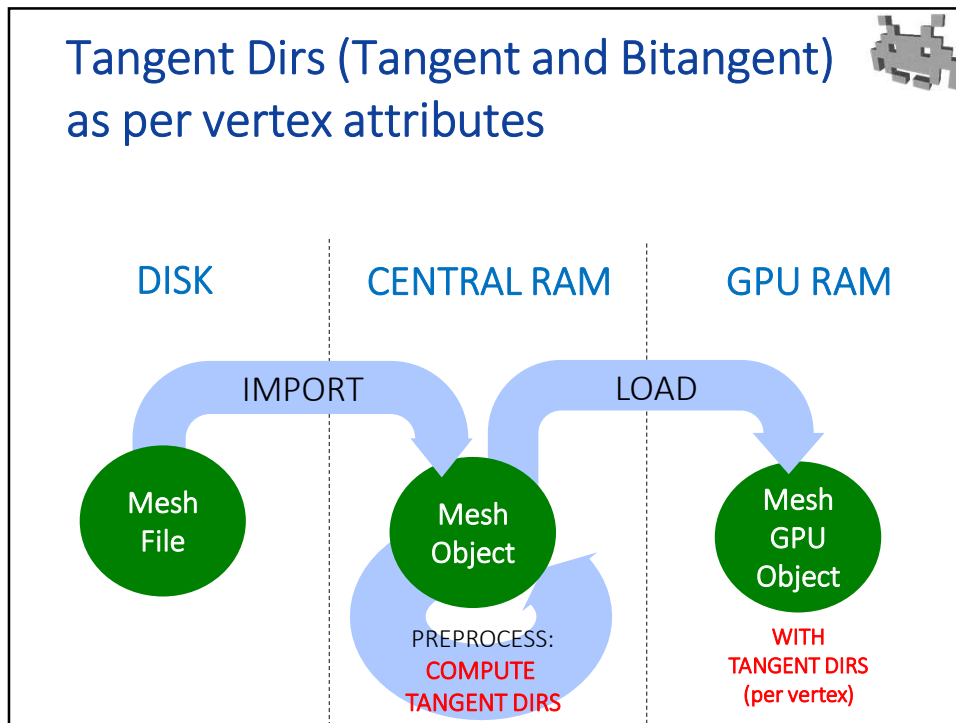
The tangent space

- Normal direction
- Tangent direction
- Bitangent direction

← basically, a TS normal map specifies how to **modify** the per-vertex normal instead of **replacing** it

- 😊 normal-map can be shared by different objects
- 😊 non injective UV-maps can be used
 - e.g., the normal-map can be tiled
 - e.g., symmetries can be exploited
- 😊 normal-map is independent from the mesh
 - e.g. can be constructed without knowing the mesh

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Normal-map: storage

The diagram is divided into three vertical sections: DISK, CENTRAL RAM, and GPU RAM. In the DISK section, a green circle labeled 'Image File' has an arrow labeled 'IMPORT' pointing to a green circle labeled 'Image Object' in the CENTRAL RAM section. An arrow labeled 'LOAD' points from the 'Image Object' to a green circle labeled 'Texture Sheet on GPU' in the GPU RAM section. Three red arrows point from the 'Image Object' and 'Texture Sheet on GPU' to the text below.

- Idea: store it as an RGB texture
 - $R \leftrightarrow X$
 - $G \leftrightarrow Y$
 - $B \leftrightarrow Z$
- but $X, Y, Z \in [-1, +1]$ and $R, G, B \in [0, +1]$
 thus a linear mapping is needed:

$X \in$

$\ni R$

$R = \frac{1}{2} (X + 1)$
 $X = 2 R - 1$
- Advantage: reuse compression of RGB textures/images
- Extra: store a (scalar) displacement map in 4th texture channel
- But, note: other, more efficient representations of versors exists

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Normal-maps: Storage

- Examples of tangent space normal-maps

\Rightarrow Prevailing normal: $X \sim 0, Y \sim 0, Z \sim 1$
 \Rightarrow Prevailing color: $R \sim 0.5, G \sim 0.5, B \sim 1$ (~light blue)

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Per e.g.: Tiled (tangent space) Normal Maps

← not possible with object-space NM!

Low-poly mesh
 UV-mapping (using tiling!)
 Tangent dirs.

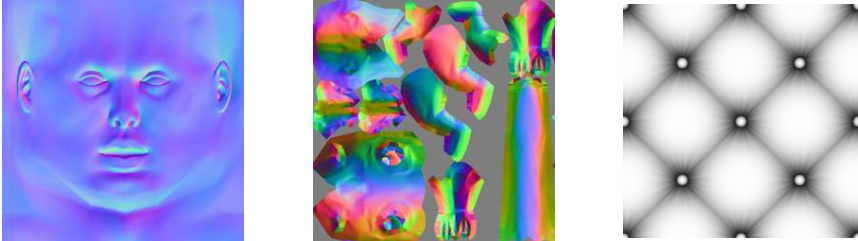
Normal-map
 Tileable!

assets courtesy of "Mount&Blade" (Talesworlds)

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Bump-maps assets at a glance

(can you tell which is which?)



Tangent Space Normal map

Object Space Normal map

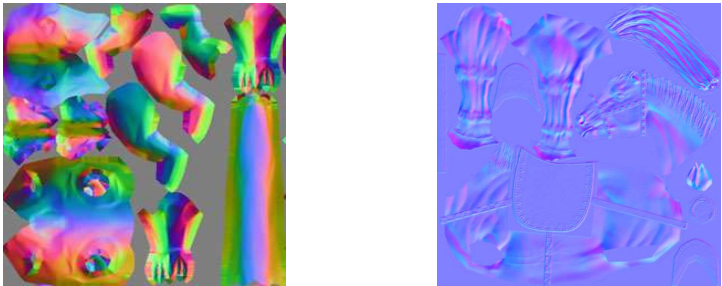
Displacement Map (scalar)

the default kind

This slide shows three different types of bump maps. The first is a 'Tangent Space Normal map' of a human face, showing a color gradient from blue to red. The second is an 'Object Space Normal map' of a character, showing a similar color gradient. The third is a 'Displacement Map (scalar)' showing a black and white diamond pattern. An arrow points from the text 'the default kind' to the Tangent Space Normal map.

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Observe



Object Space Normal map

1:1 UV-map
right leg != left leg

(Tangent Space) Normal map

UV-mapping NOT injective
Exploited symmetries!
Left side of head = right side of head

This slide compares two character bump maps. The left one is an 'Object Space Normal map' with a 1:1 UV-map, where the right leg is not the same as the left leg. The right one is a '(Tangent Space) Normal map' where UV-mapping is not injective, exploiting symmetries so that the left side of the head is the same as the right side.

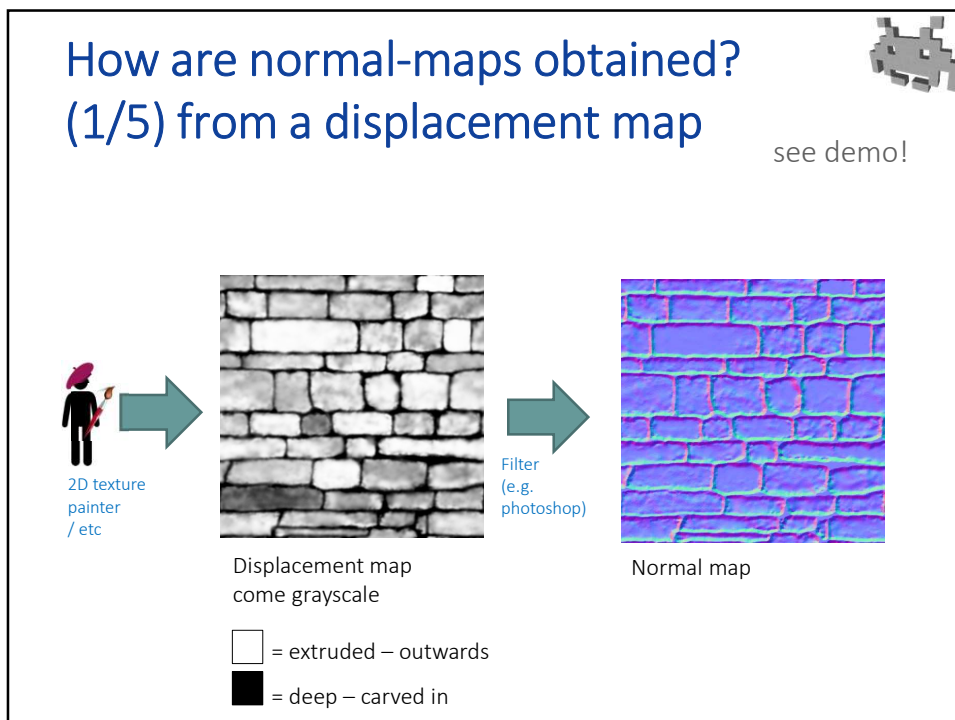
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Normal map comparison: a summary

Object Space Normal map:	Tangent Space Normal map:
Replaces the normal of the objects	Modifies the normal of the objects
No normal attribute required on the mesh any more	Requires two extra attributes on the mesh: T an B versors (in addition to the normal)
Constructing the texture requires to know the mesh it will be applied to	Textures can be constructed independently from the mesh (just like a color map!)
E.g. a normal map cannot be constructed from a displacement map (w/o the mesh)	E.g. a normal map can be constructed from a displacement map
E.g. difficult to share a normal map between models	Normal maps can be shared between different models
“ unwrapping ” UV-maps required (unless few lucky cases)	Can be applied to non-injective UV-maps Eg: tiling, symmetry exploitation
E.g. no tiled textures. E.g. no symmetry exploitation	E.g. tiled textures ok, E.g. symmetry exploitation ok
E.g. east-wall and south-wall of a castle: different normal maps required	E.g. east wall and south wall of a castle: Same normal map possible
Looks colorful (if encoded as RGB)	Looks azure-ish (if encoded as RGB)

MUCH MORE USED IN GAMES

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How are normal-maps obtained? (1/5) from a displacement map



- Input: a scalar displacement map ← a texel at coords u, v corresponds to a 3D point
Output: a normal map
- Algorithm (basic image processing): $(u, v, \text{height}[u, v])$
 - \forall texel \mathbf{t} of displacement map, compute **best fitting plane** around \mathbf{t}
 - Consider all 3D points in a 3×3 patch surrounding \mathbf{t} ← or 5×5 , or $7 \times 7 \dots$
 - Find plane minimizing the summed squared distance from them
 - It's a least-squares minimization problem
 - The normal of this plane is the normal for \mathbf{t}
- Resulting normal map is expressed in **tangent-space**
 - By definition! (one advantage of Tangent Space Normal Maps)
 - Can be converted into Object-Space if needed (for a given UV-mapped mesh – injective maps only of course)

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How are normal-maps obtained? (2/5) painting on 3D



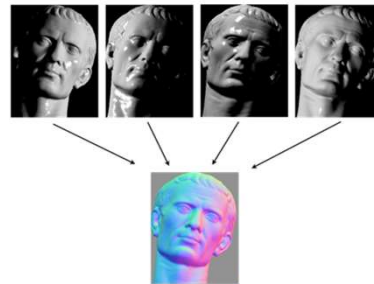
- Direct painting of normal- on the model
 - (can be done, e.g., with Z-brush, Sculpttris Alpha...)
 - Similar to a painting of color-maps
 - but artist paints geometric details not colors
 - Similar to mesh sculpting too
 - but, for each stroke, the system directly updates the normal on the texture-map, not the geometry on the mesh

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How are normal-maps obtained? (3/5) captured from reality



- Captured from reality, using photos
- Example: “**Photometric Stereo**”
 - a form of “inverse lighting”
 - a **computer vision** technique
- Input: n real images
 - Same viewpoint
 - Different illumination
 - possibly, controlled and known
- Output: a Normal Map
 - expressed in image space
 - can be converted in object space, or in tangent space



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How are normal-maps obtained? (3/5) captured from reality



- Normal map estimation from images
 - Traditionally, many pictures are required in input
 - Traditionally, controlled illumination is required (I must place lights in known position)
 - With Machine Learning, it's becoming possible to use a single image with natural illumination
- Idea:
 - input: a photo of a brickwall
 - output: a diffuse map + a normal map + a specular map
- It's an active area of research!

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